

SOLARNET

Radiative transfer

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- Basic concepts
- Formal solution
 - Numerical integration, scattering problem, lambda iteration, shooting, finite difference methods, Feautrier's method, accelerated lambda iteration, convergence acceleration
- non-LTE
 - Linearization, rate equations, Scharmer operator, local operator
- 3D
 - Long characteristics, short characteristics
- Energy equation
 - ODF, multi-group opacities

Examples

- Contribution & response functions
- non-Statistical equilibrium
- 3D simulations from convection zone to corona
- 3D radiative transfer
- IRIS
- Mg II diagnostics

- MULTI non-LTE code
- working with IRIS data
- public release of 3D models

- Hands on Session, radiative transfer
 - Na-D, Mg-b, Ca-H, Hinode BFI continua
 - getting input data - building atomic models
 - non-LTE effects for abundance determinations of stars
 - 3D column-by-column with MULTI
- Hands on Session, IRIS

Basic concepts

Basic definitions

I_ν Intensity. $\text{erg cm}^{-2}\text{s}^{-1}\text{sr}^{-1}\text{Hz}^{-1}$

η_ν Emissivity

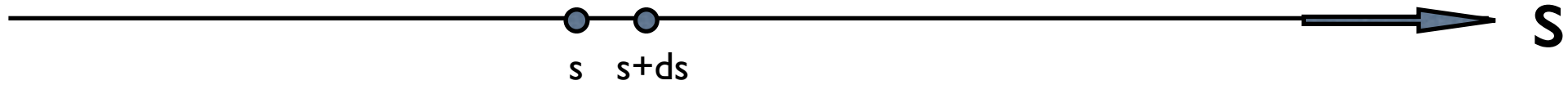
χ_ν Opacity

Intensity gives the amount of energy per unit area perpendicular to the ray in a given direction per unit time per solid angle and per frequency bin. The intensity is constant with distance in the absence of emission and absorption/scattering processes.

Emissivity gives the addition of energy to the ray through emission processes.

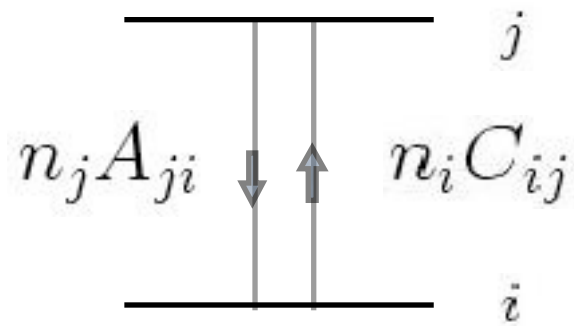
Opacity gives the removal of energy from the ray through absorption and scattering processes.

Transfer equation



$$dI_\nu = -\chi_\nu I_\nu ds + \eta_\nu ds$$

Coronal approximation: $\chi_\nu = 0$

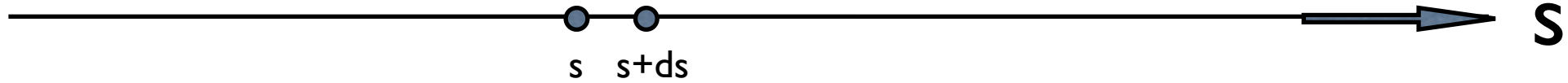


$$\eta_\nu = \frac{h\nu}{4\pi} n_j A_{ji}$$

$$n_j A_{ji} = n_i C_{ij}$$

Emissivity and rates set by local conditions.

Transfer equation



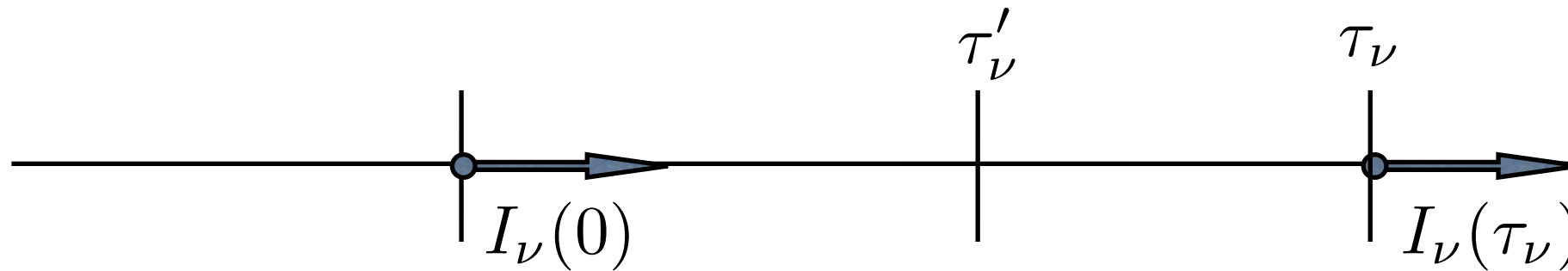
$$dI_\nu = -\chi_\nu I_\nu ds + \eta_\nu ds$$

Opacity non-zero case

$$d\tau_\nu \equiv \chi_\nu ds \quad S_\nu \equiv \frac{\eta_\nu}{\chi_\nu}$$

$$\frac{dI_\nu}{d\tau_\nu} = S_\nu - I_\nu$$

Transfer equation



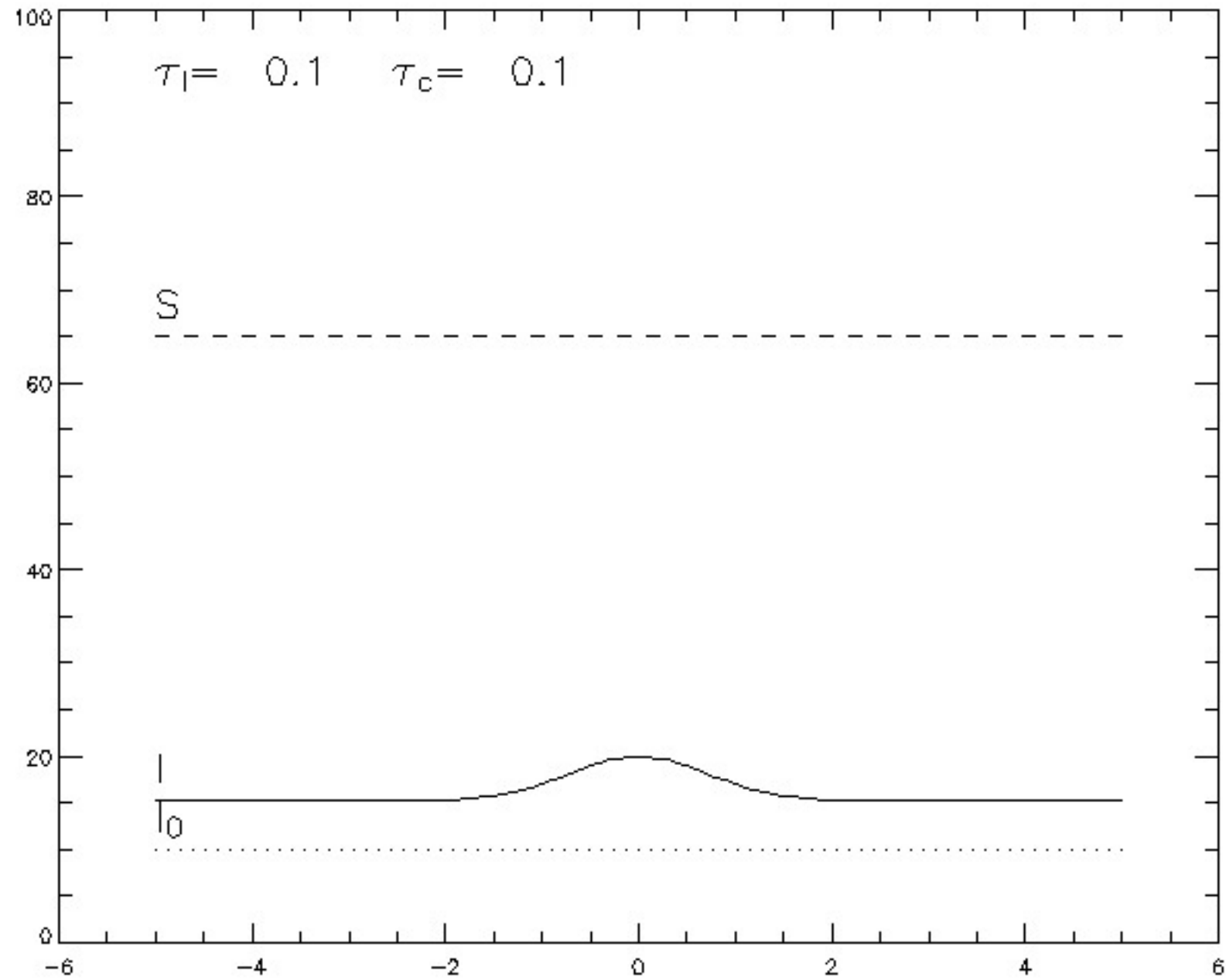
$$I_\nu(\tau_\nu) = I_\nu(0)e^{-\tau_\nu} + \int_0^{\tau_\nu} S_\nu(\tau'_\nu)e^{-(\tau_\nu - \tau'_\nu)} d\tau'_\nu$$

Homogeneous slab, small optical depth:

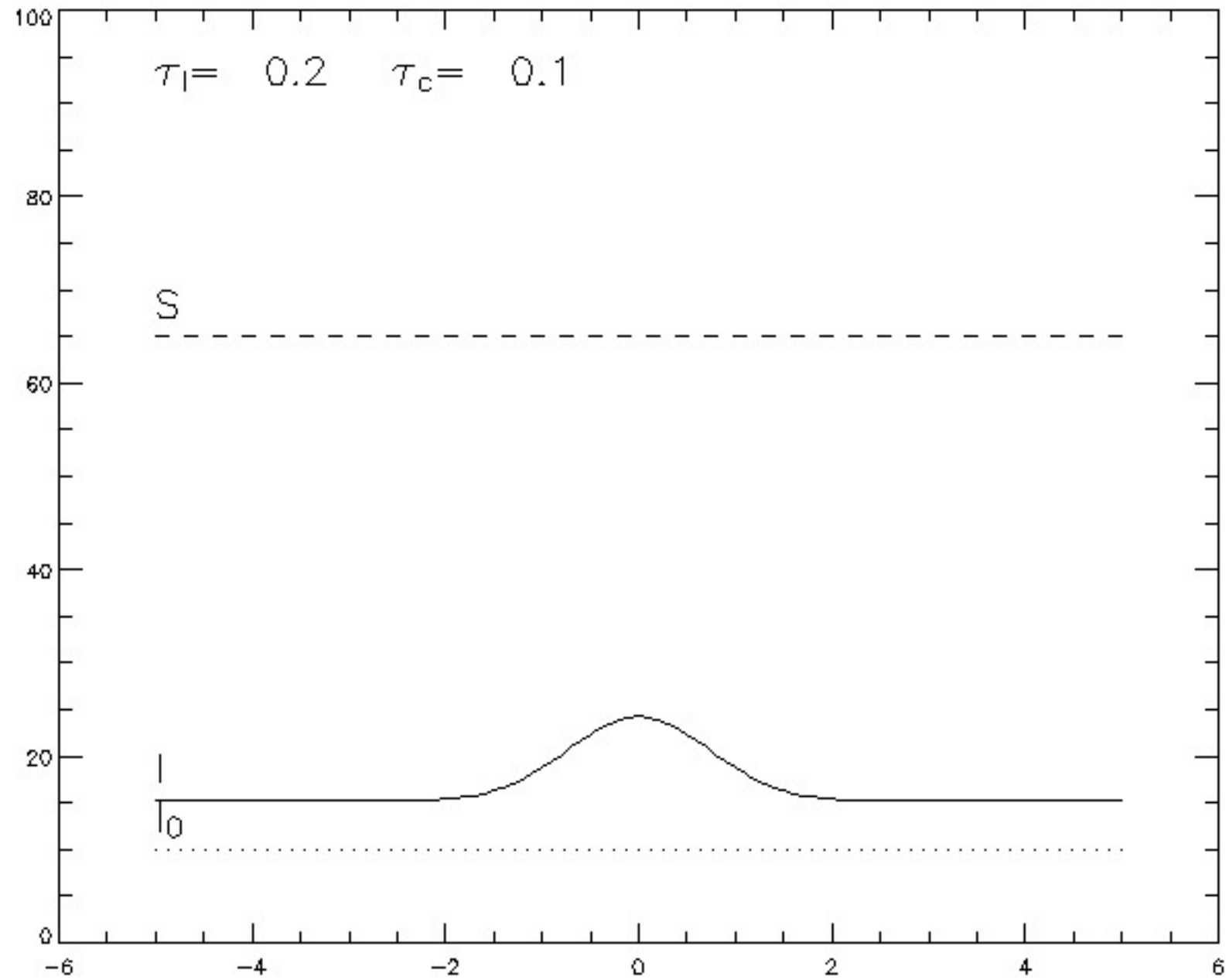
$$I_\nu(\tau_\nu) = I_\nu(0) + \tau_\nu(S_\nu - I_\nu(0))$$

Intensity (wavelength dependent!) is then an interpolation between the incoming intensity and the source function and thus always between the two. For $I(0) > S$ we get an absorption line, for $I(0) < S$ we get an emission line.

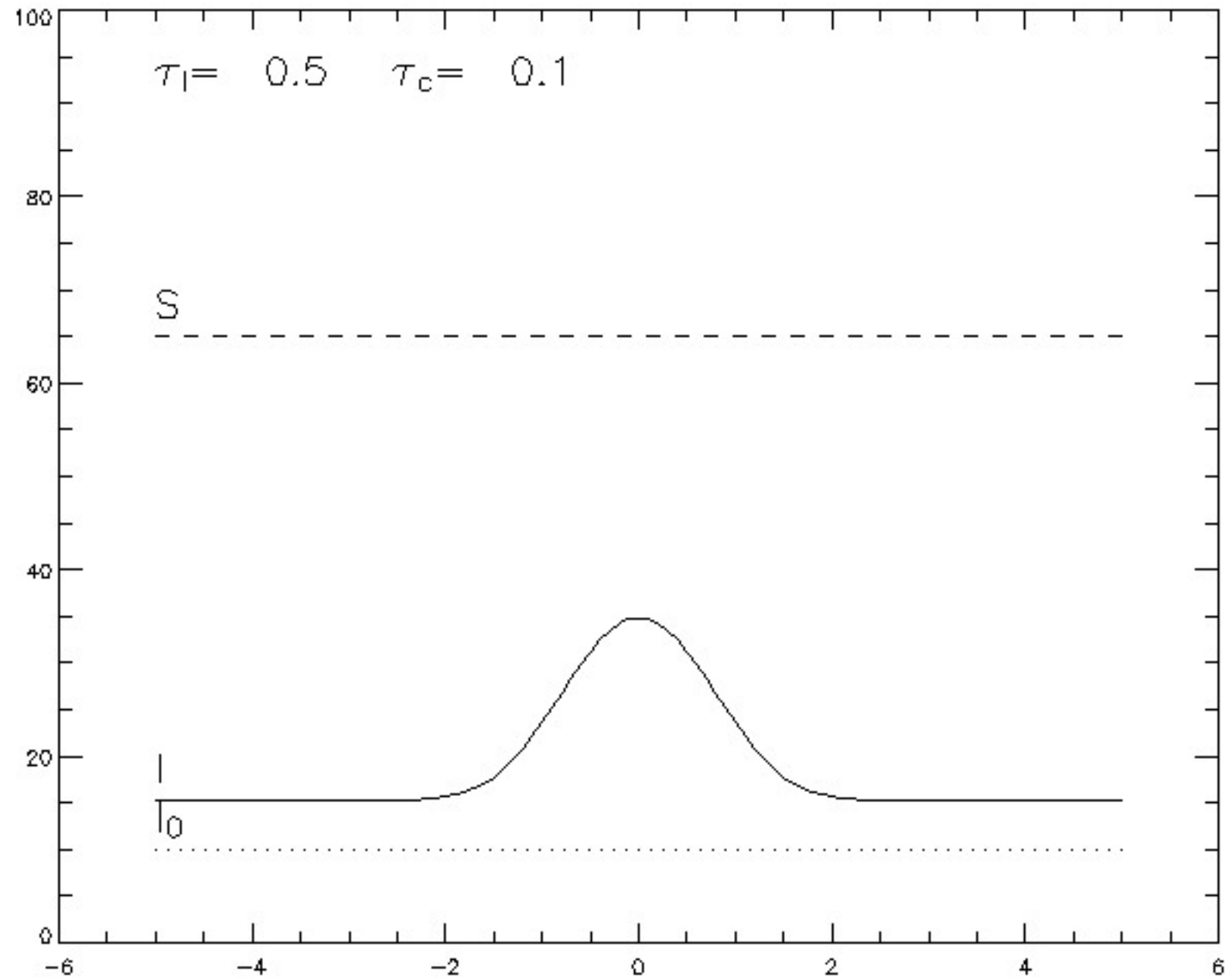
Homogeneous slab



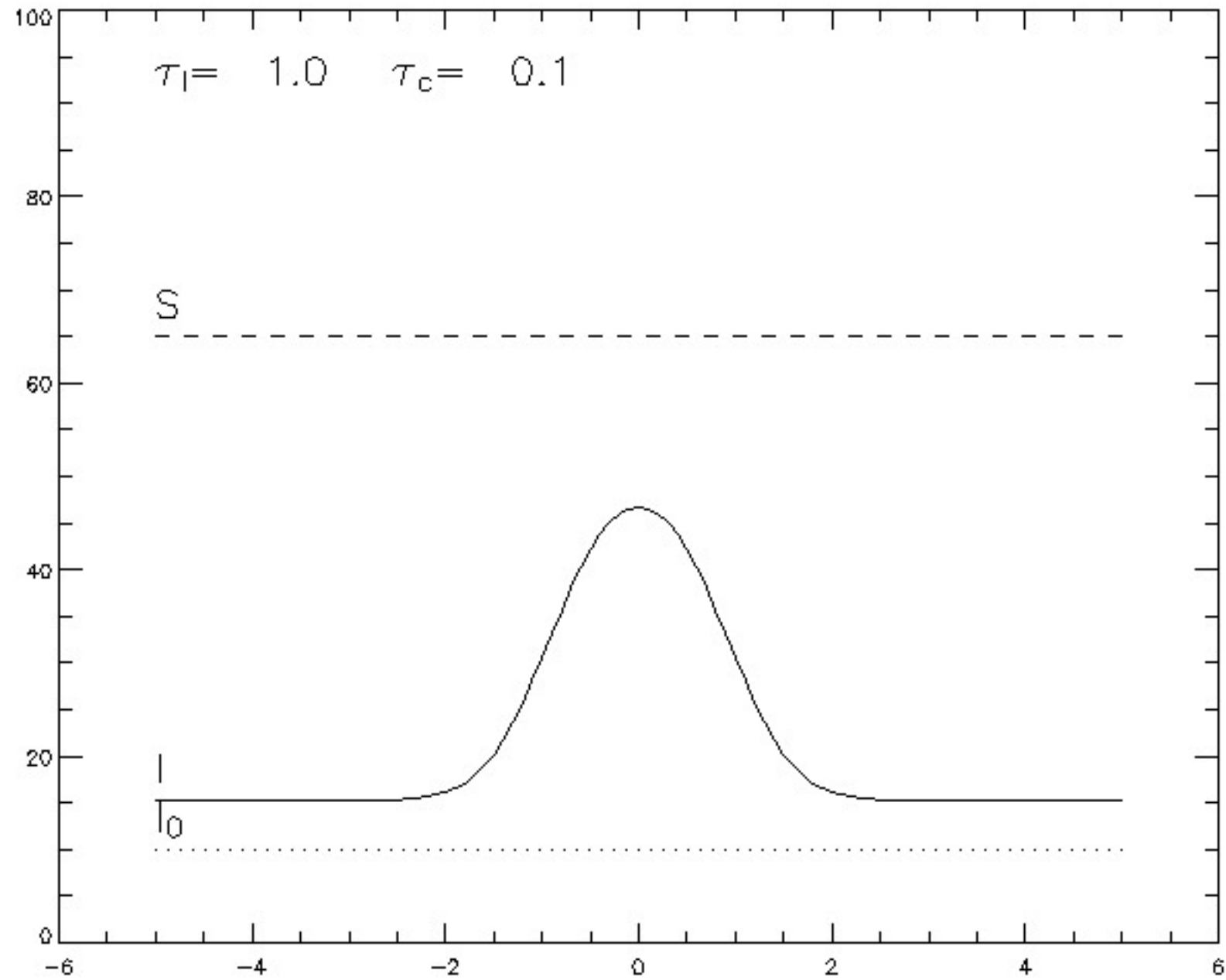
Homogeneous slab



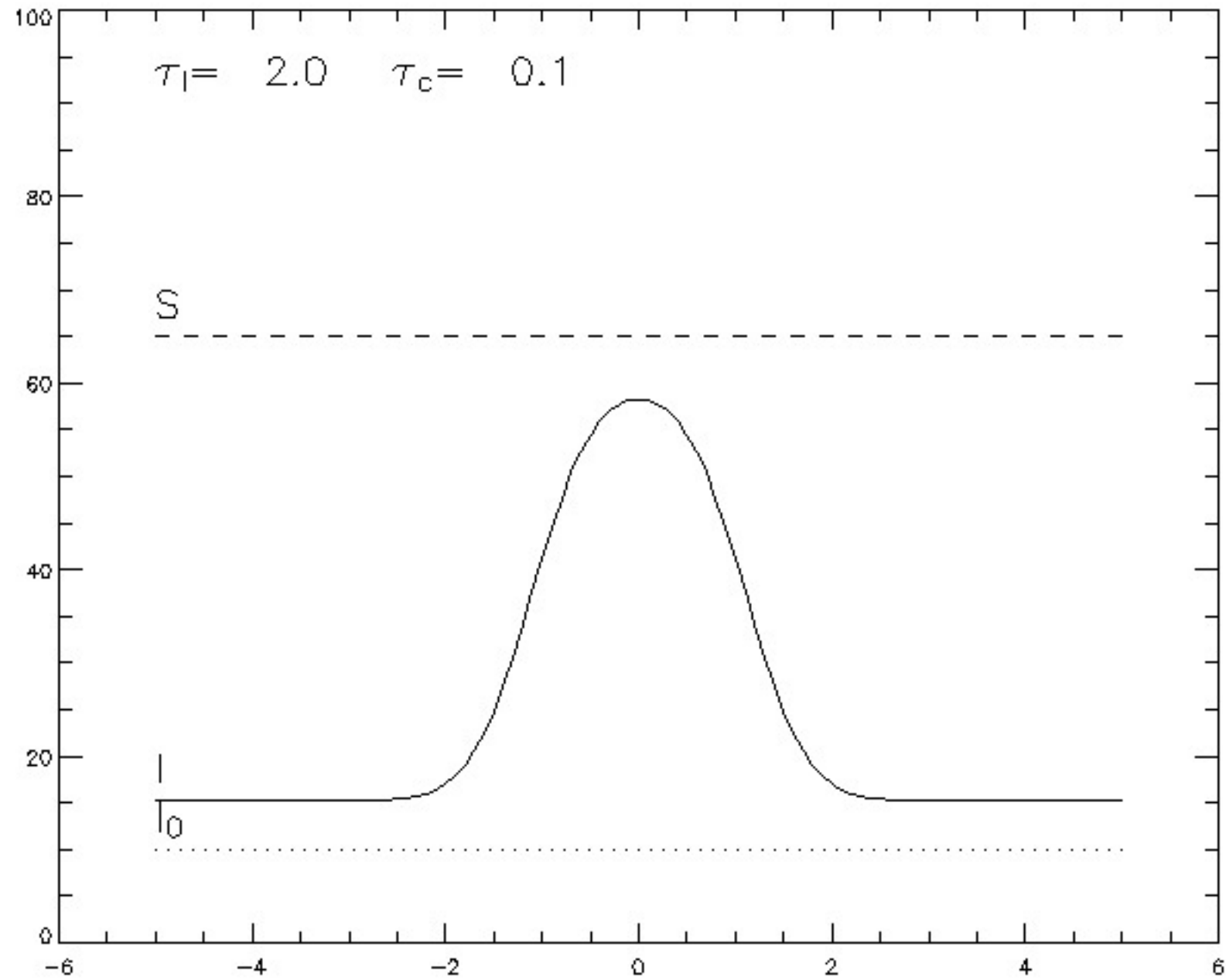
Homogeneous slab



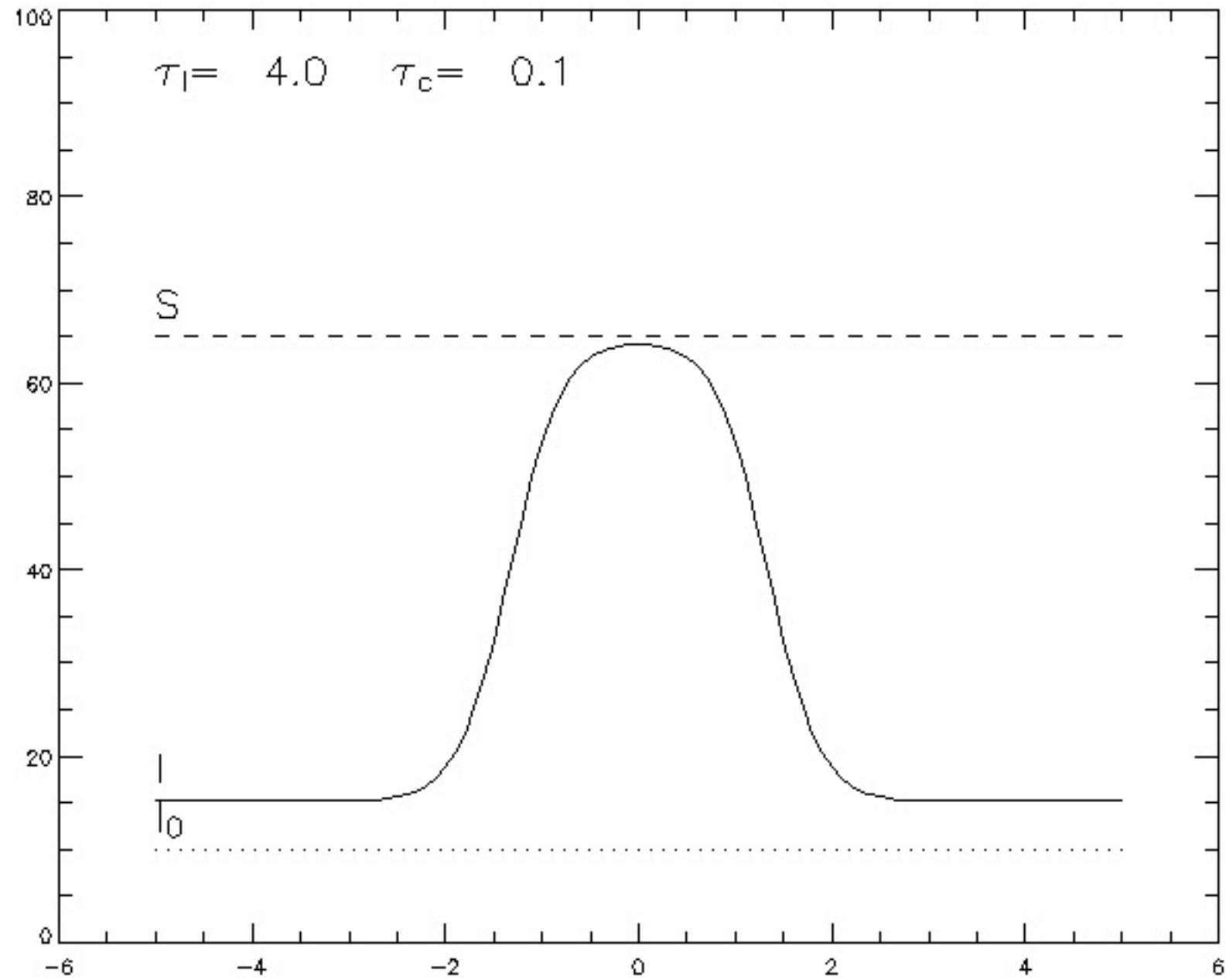
Homogeneous slab



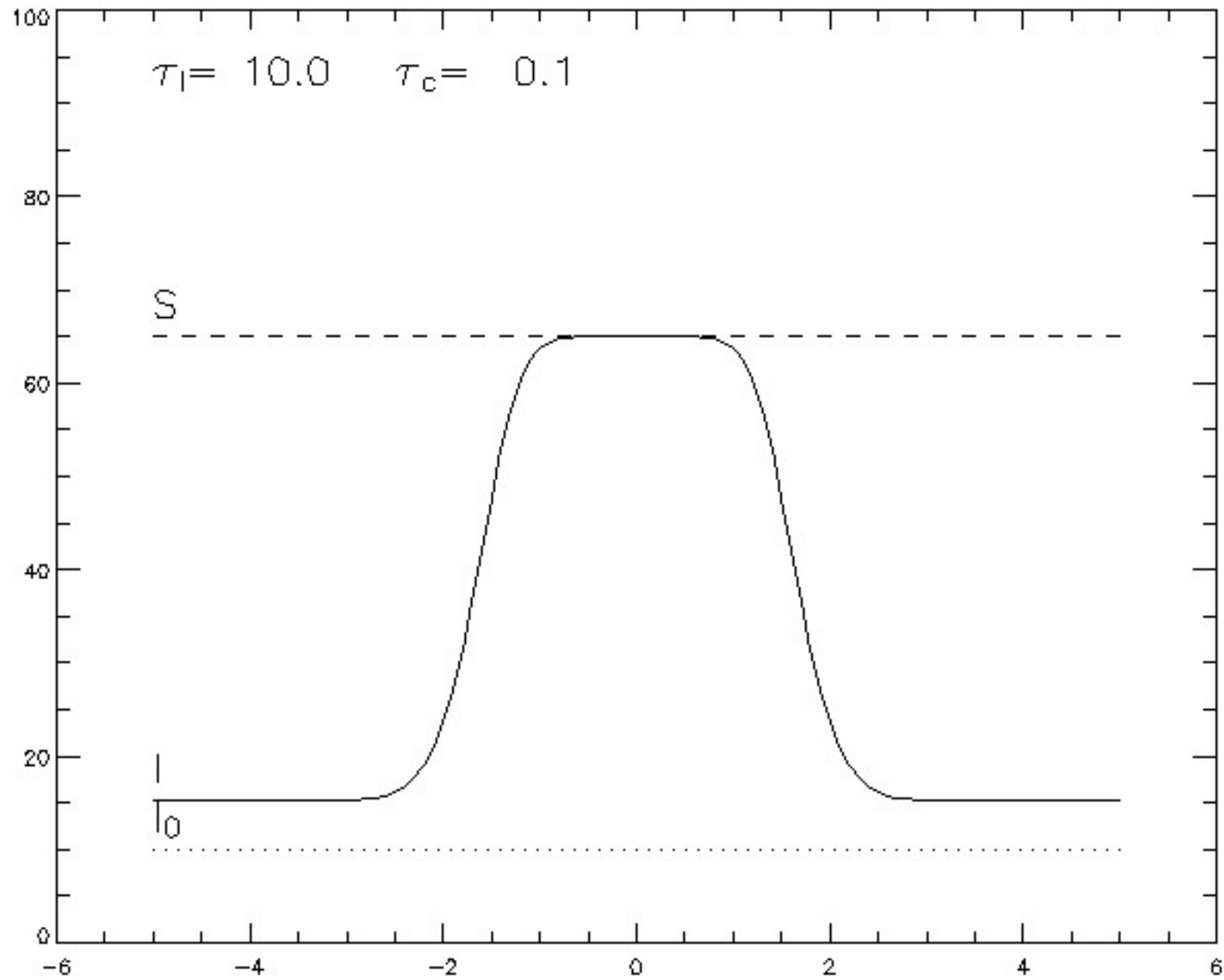
Homogeneous slab



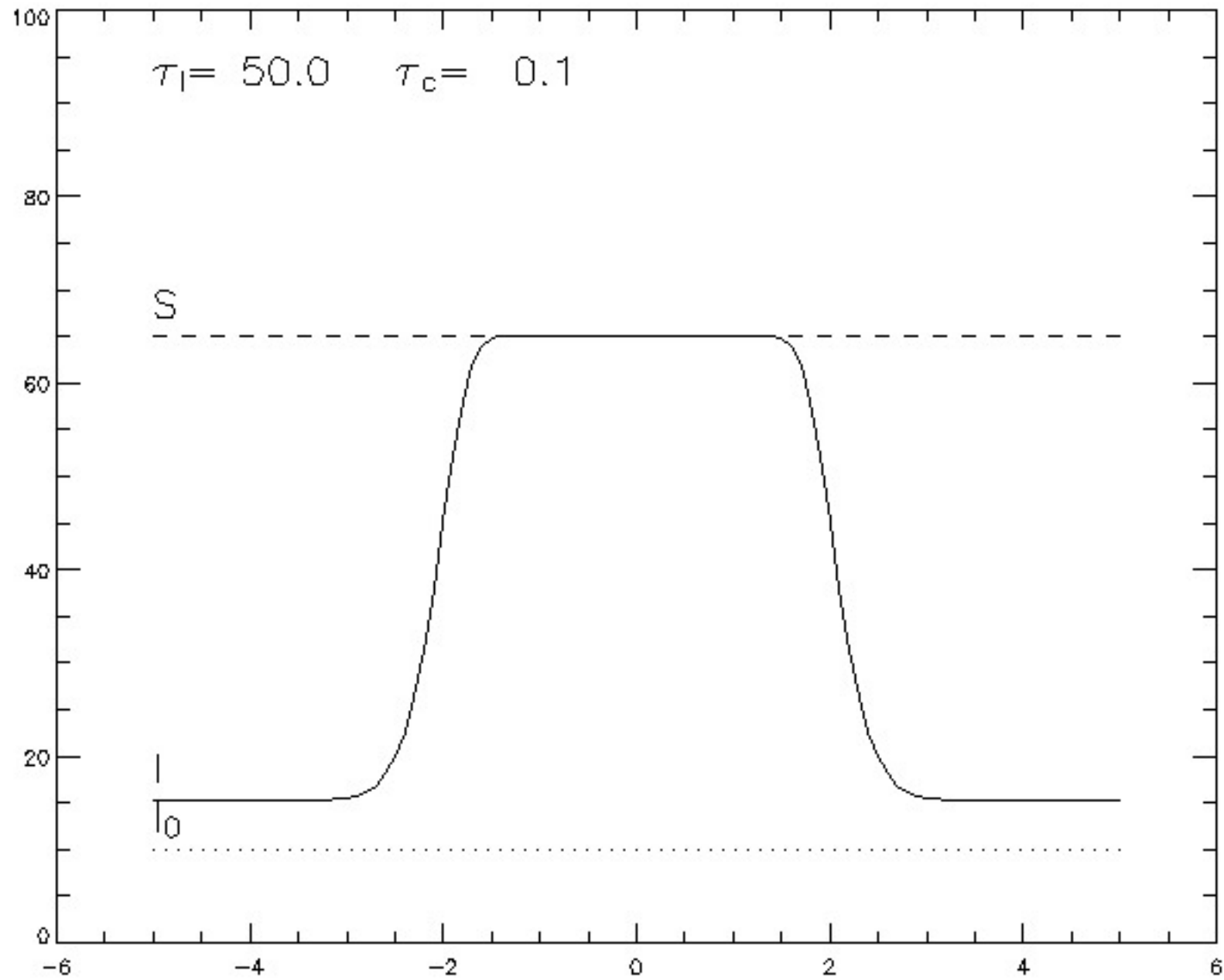
Homogeneous slab



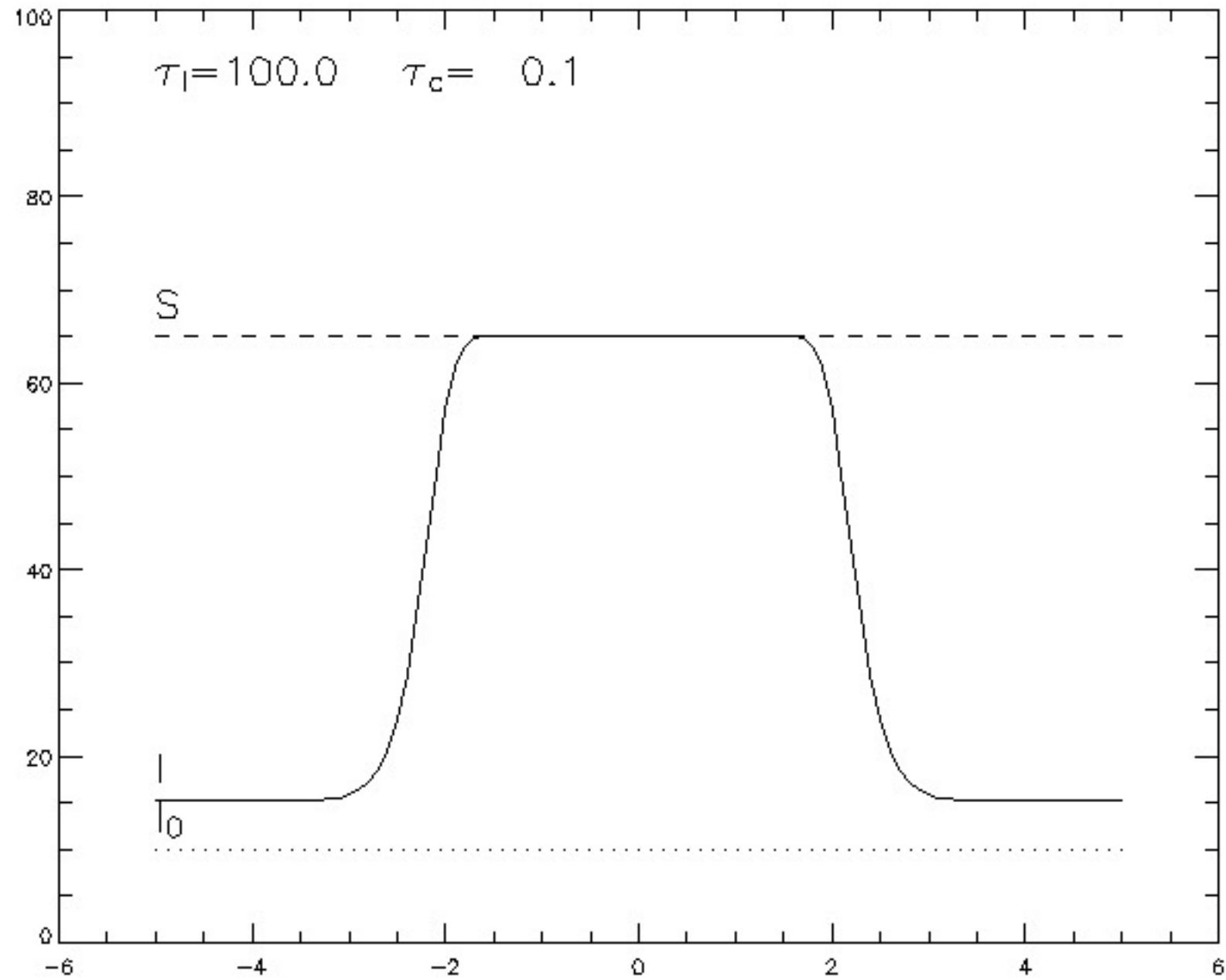
Homogeneous slab



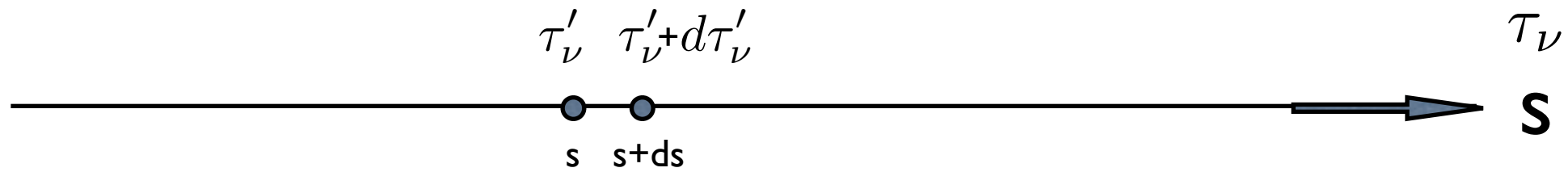
Homogeneous slab



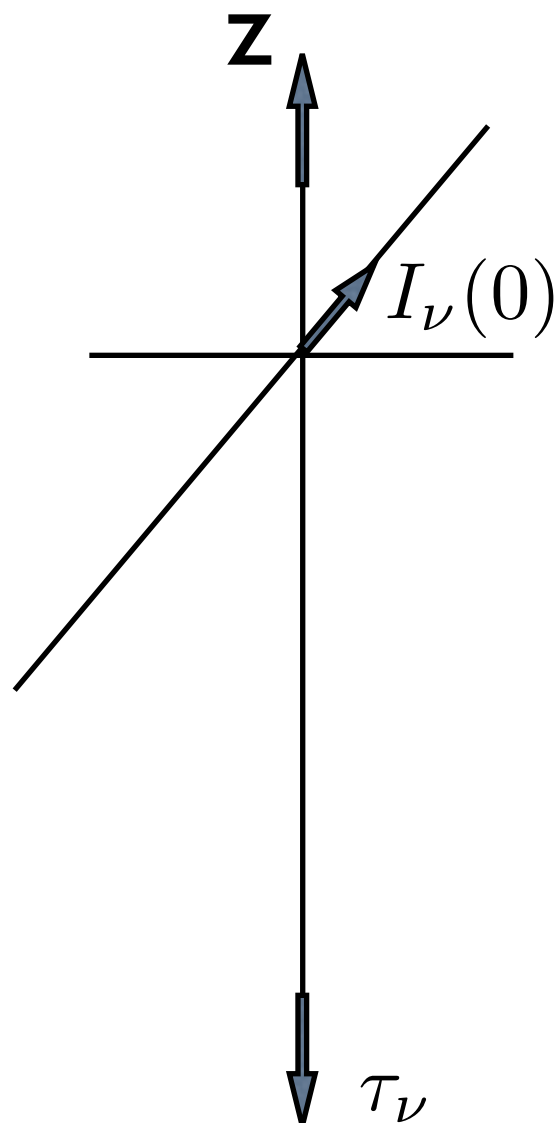
Homogeneous slab



Transfer equation



$$I_\nu(\tau_\nu) = I_\nu(0)e^{-\tau_\nu} + \int_0^{\tau_\nu} S_\nu(\tau'_\nu)e^{-(\tau_\nu - \tau'_\nu)} d\tau'_\nu$$



Semi-infinite atmosphere, 1D:

$$I_\nu(0) = \frac{1}{\mu} \int_0^\infty S_\nu(\tau'_\nu) e^{-\tau'_\nu / \mu} d\tau'_\nu$$

where μ is the cosine of the angle between the ray and the normal of the atmosphere

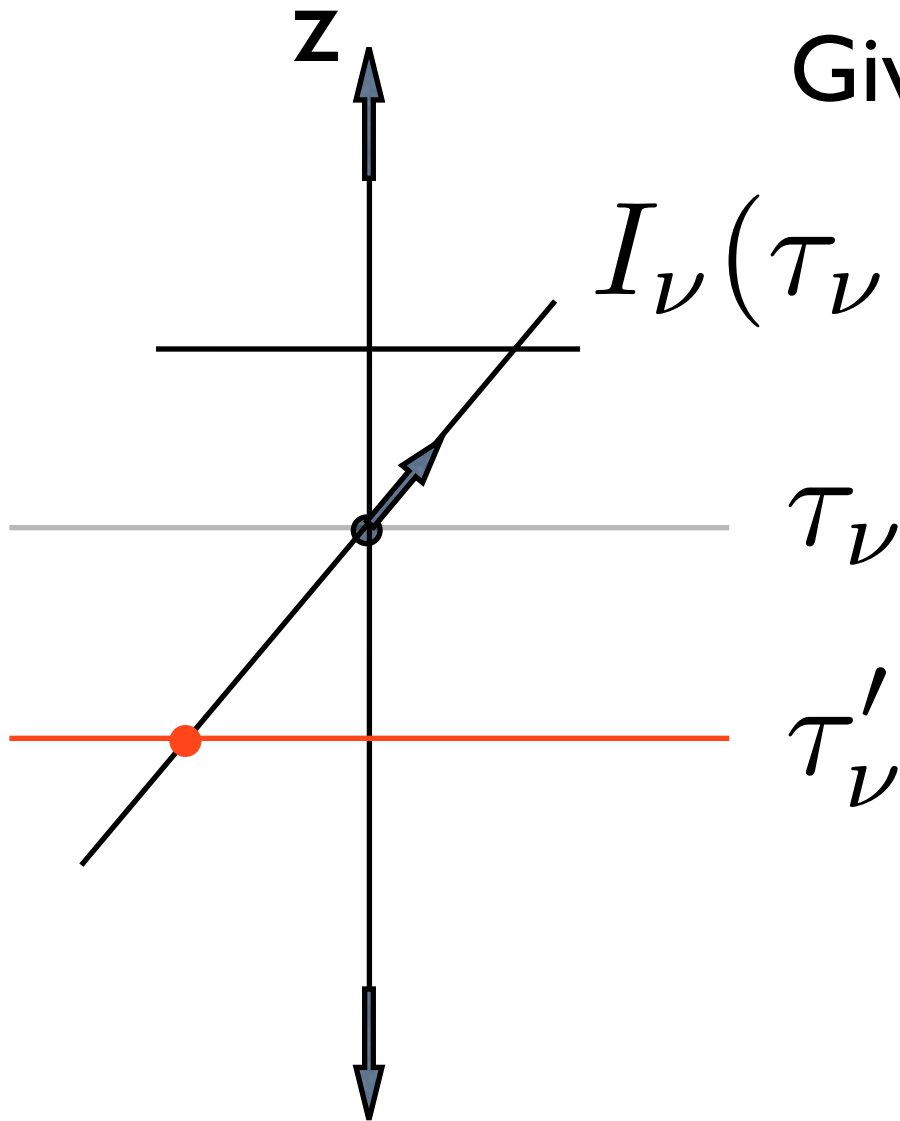
Eddington Barbier relation

Assuming a linear source function:

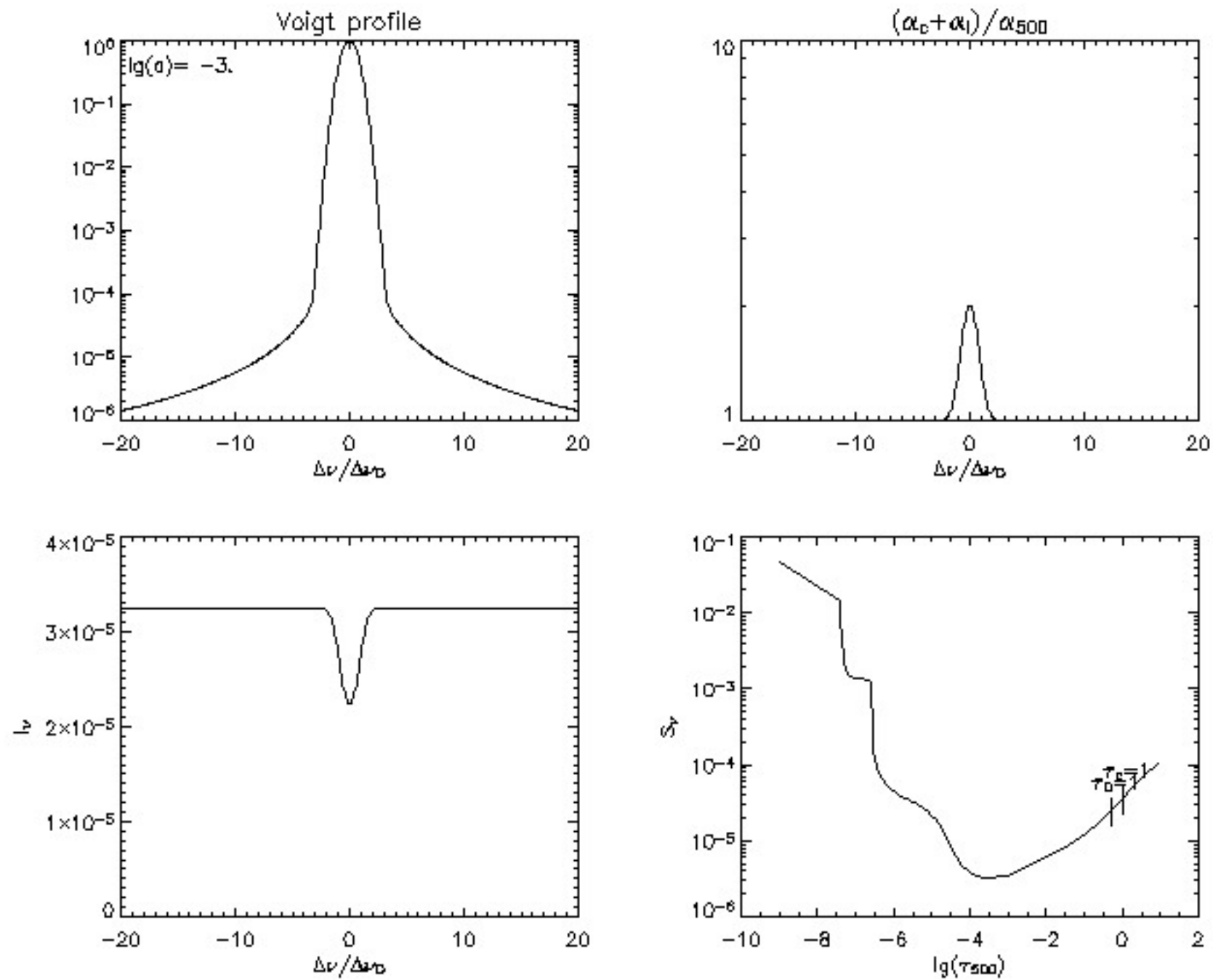
$$S_{\nu}(\tau'_{\nu}) = a + b\tau'_{\nu}$$

Gives a formal solution:

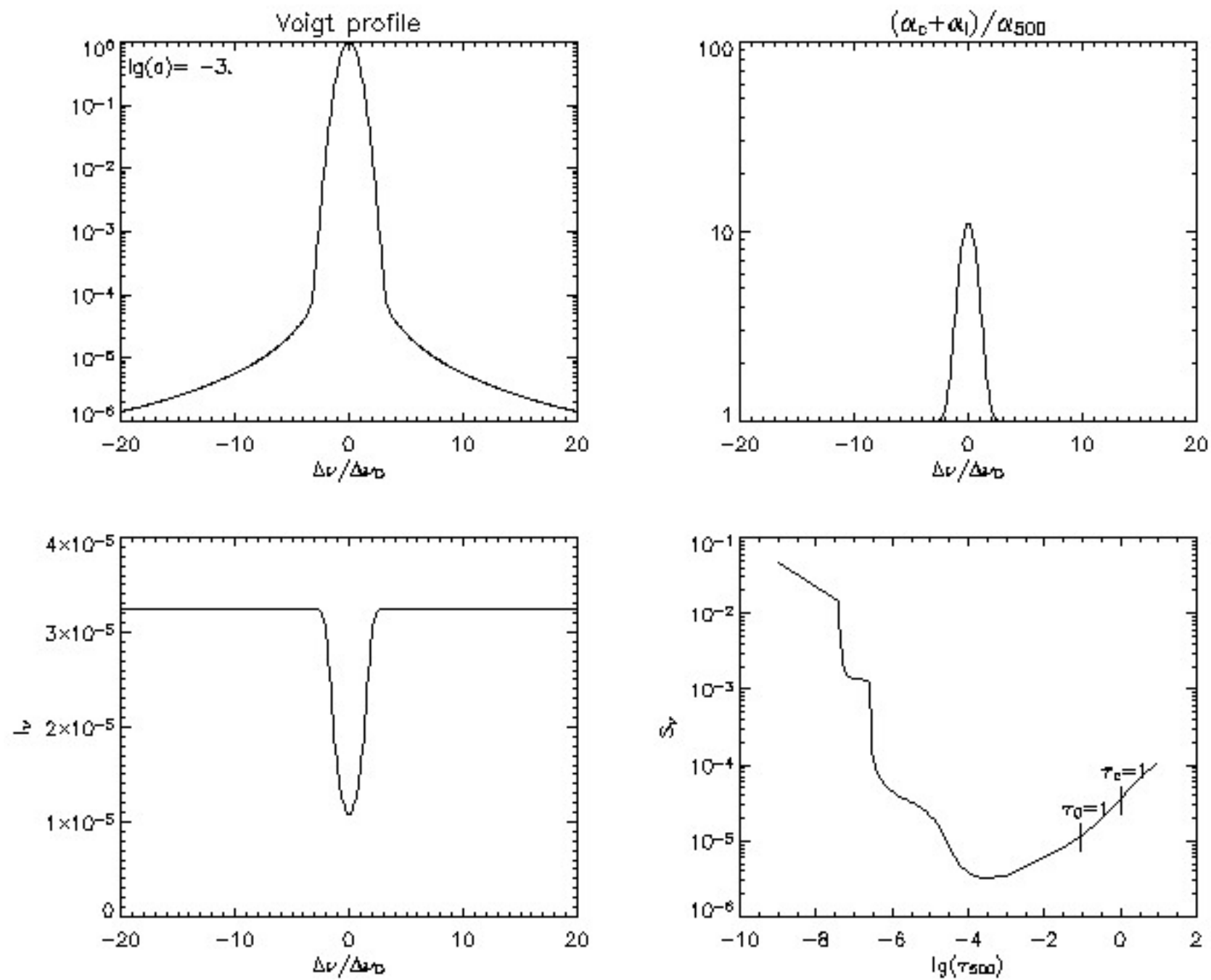
$$I_{\nu}(\tau_{\nu}, \mu) = S_{\nu}(\tau'_{\nu} = \tau_{\nu} + \mu)$$



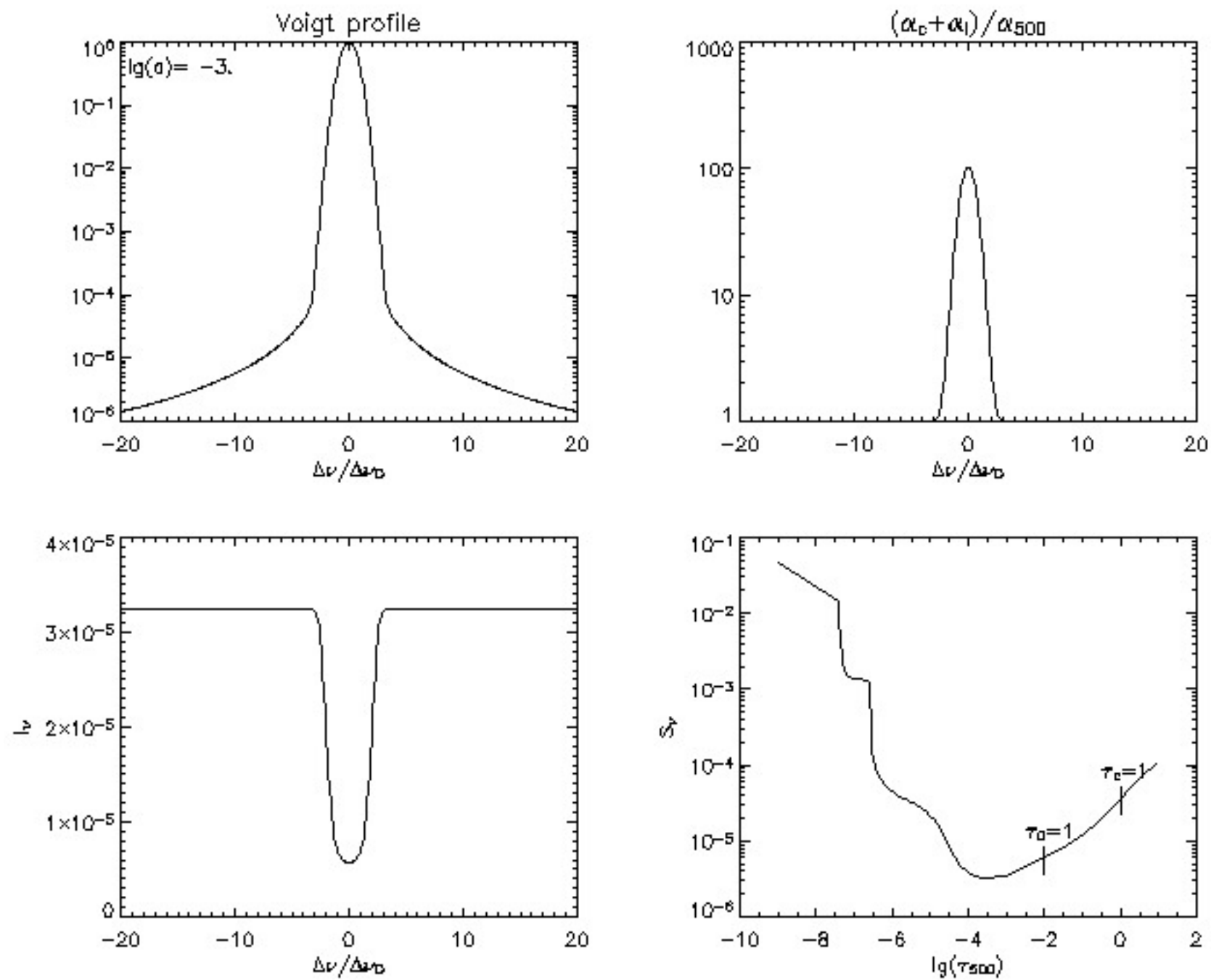
Optically thick line formation I



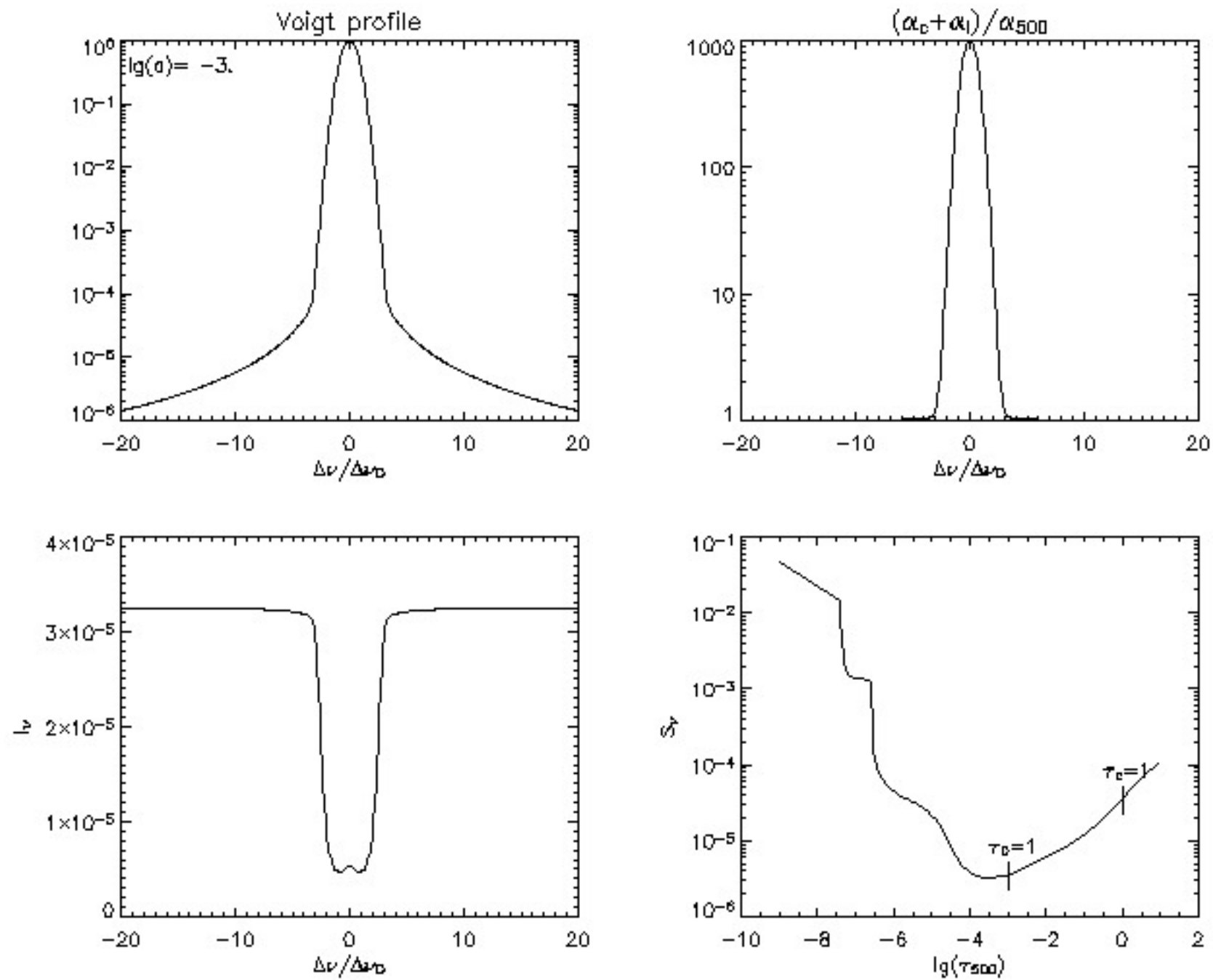
Optically thick line formation



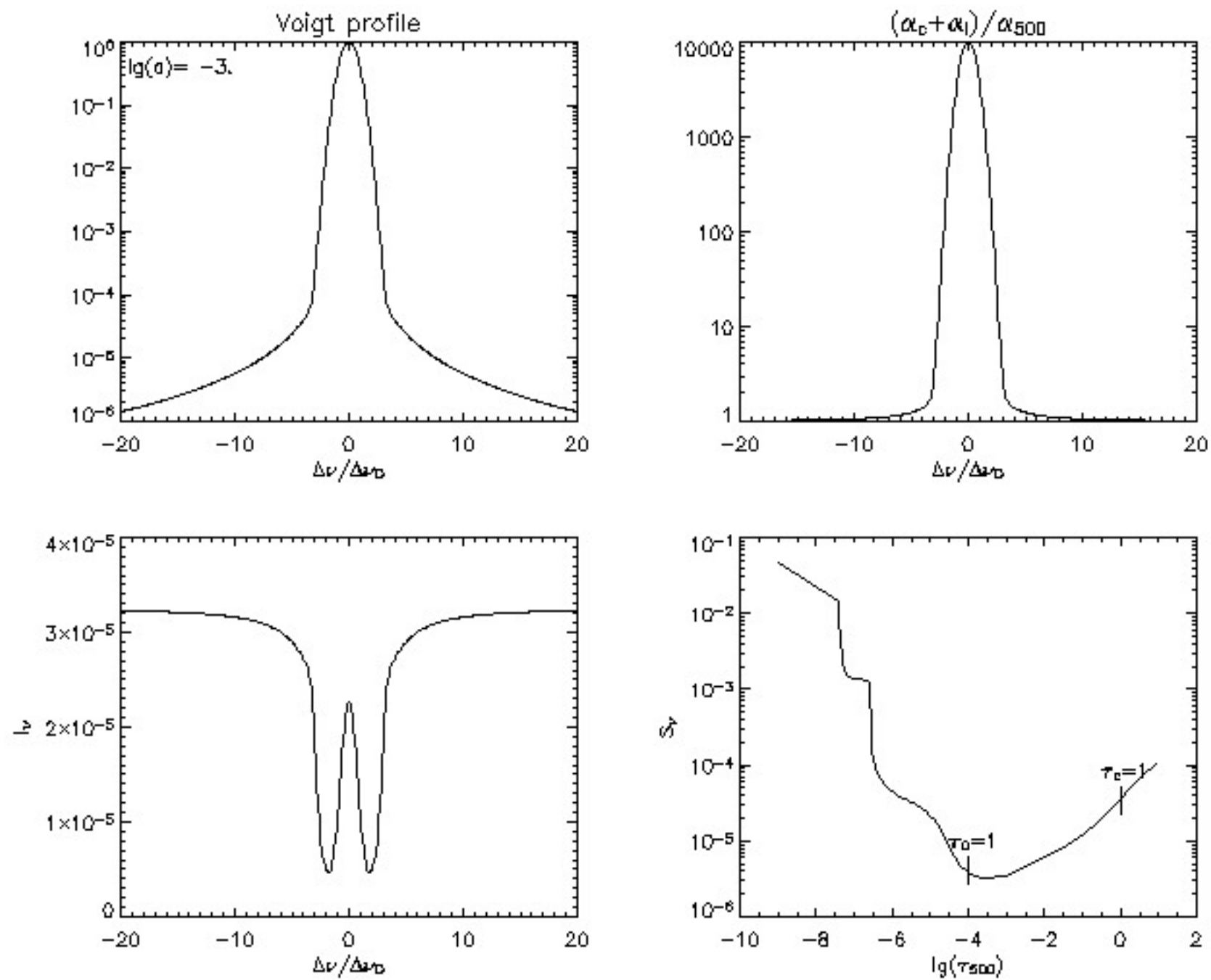
Optically thick line formation



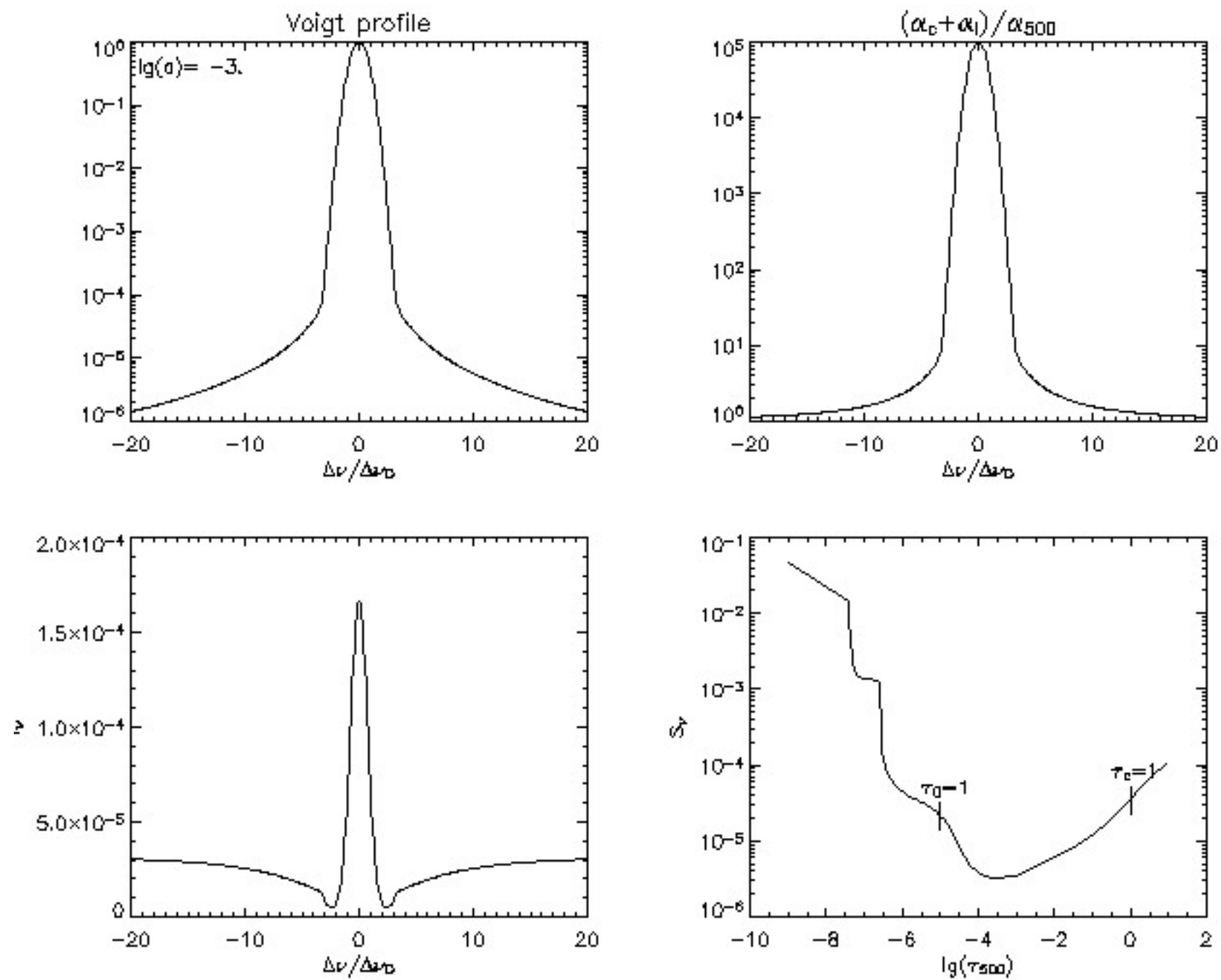
Optically thick line formation



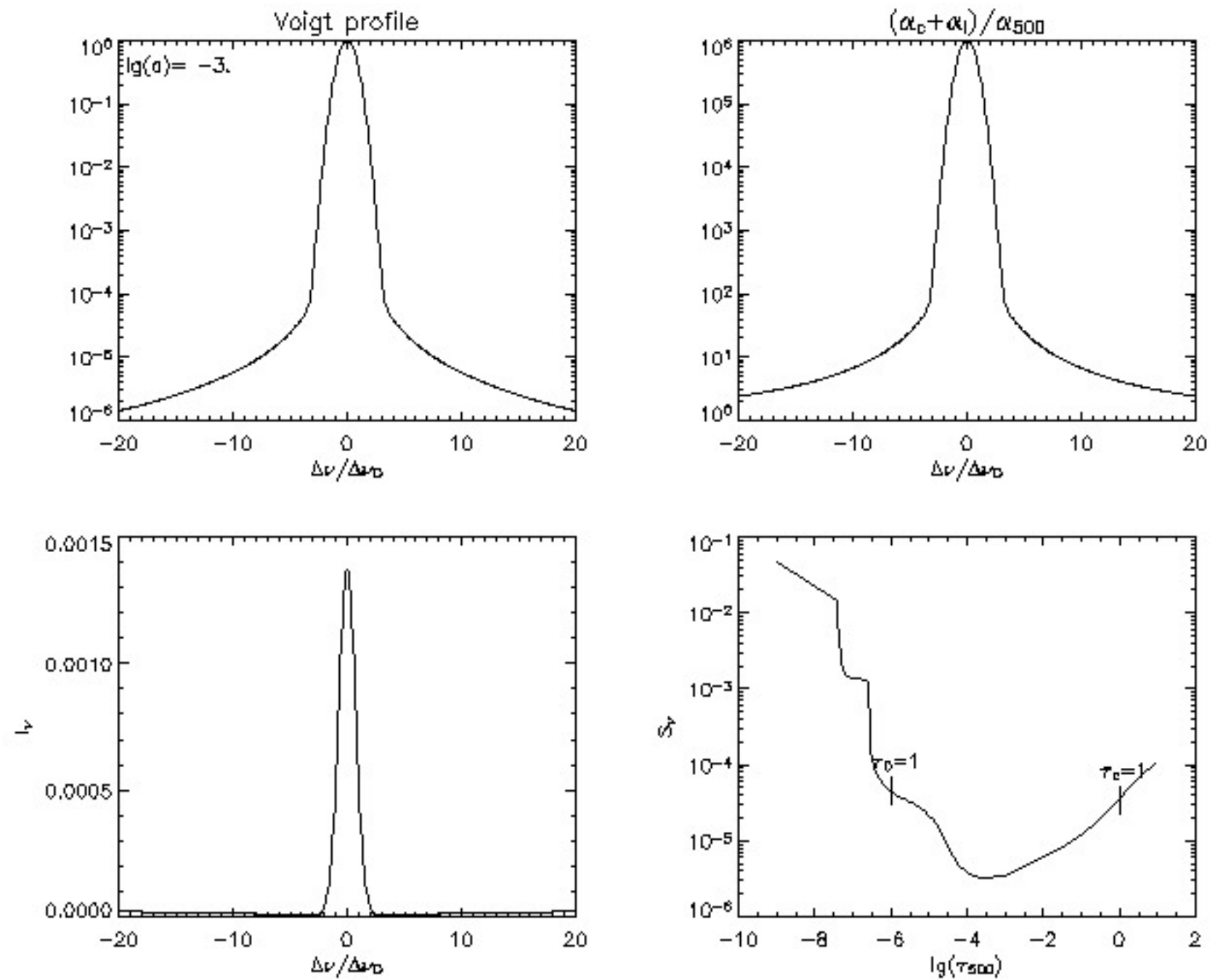
Optically thick line formation



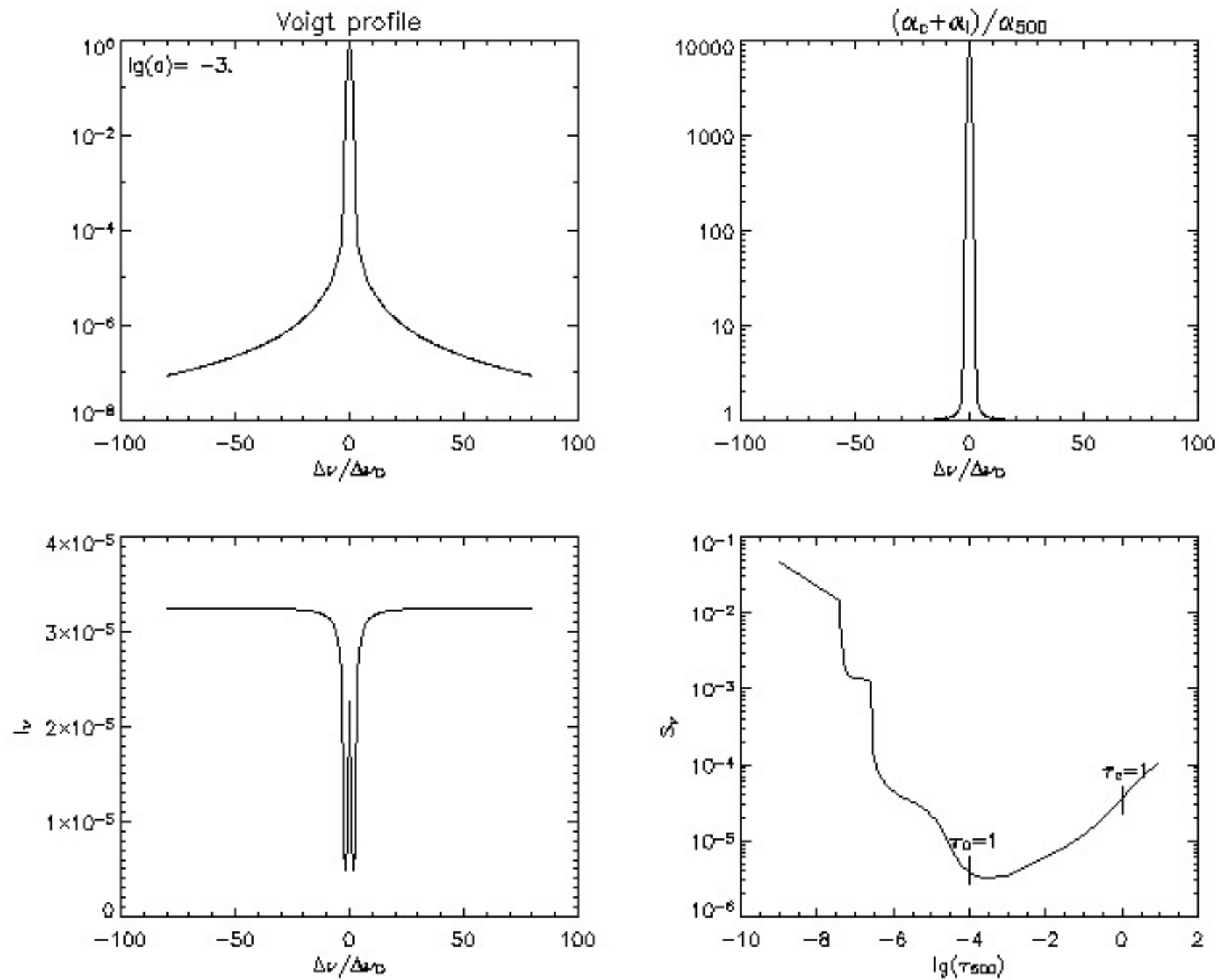
Optically thick line formation



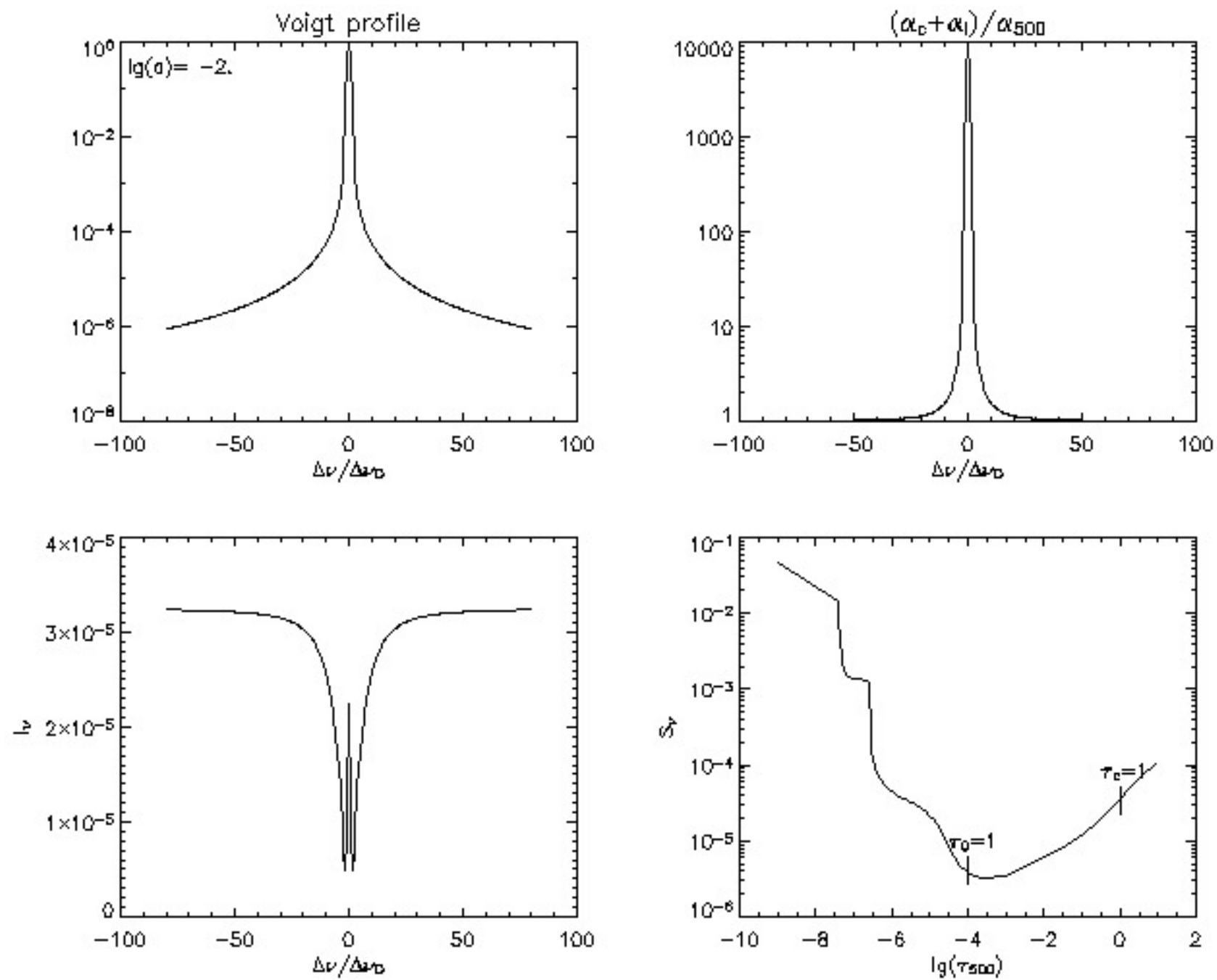
Optically thick line formation



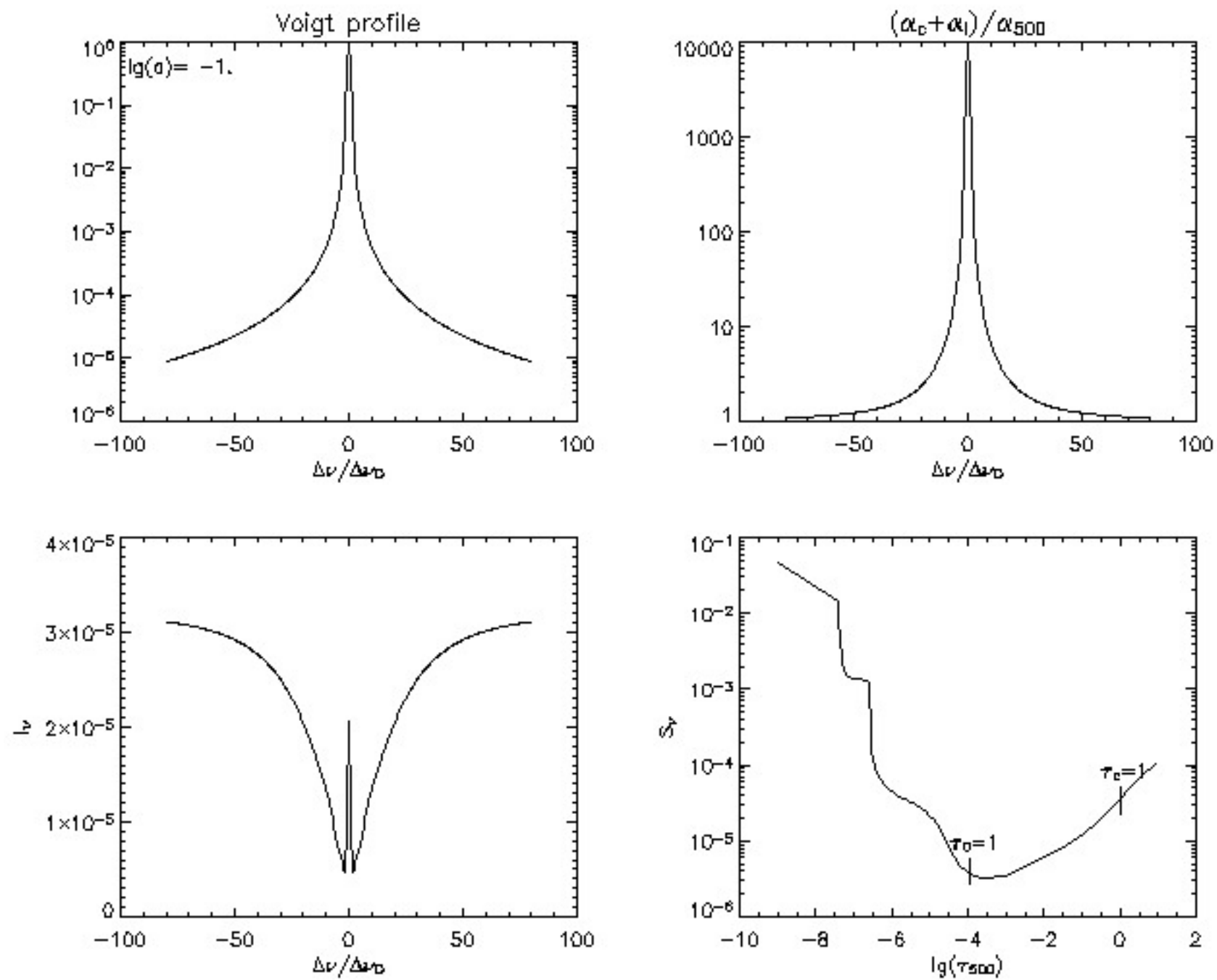
Optically thick line formation 2



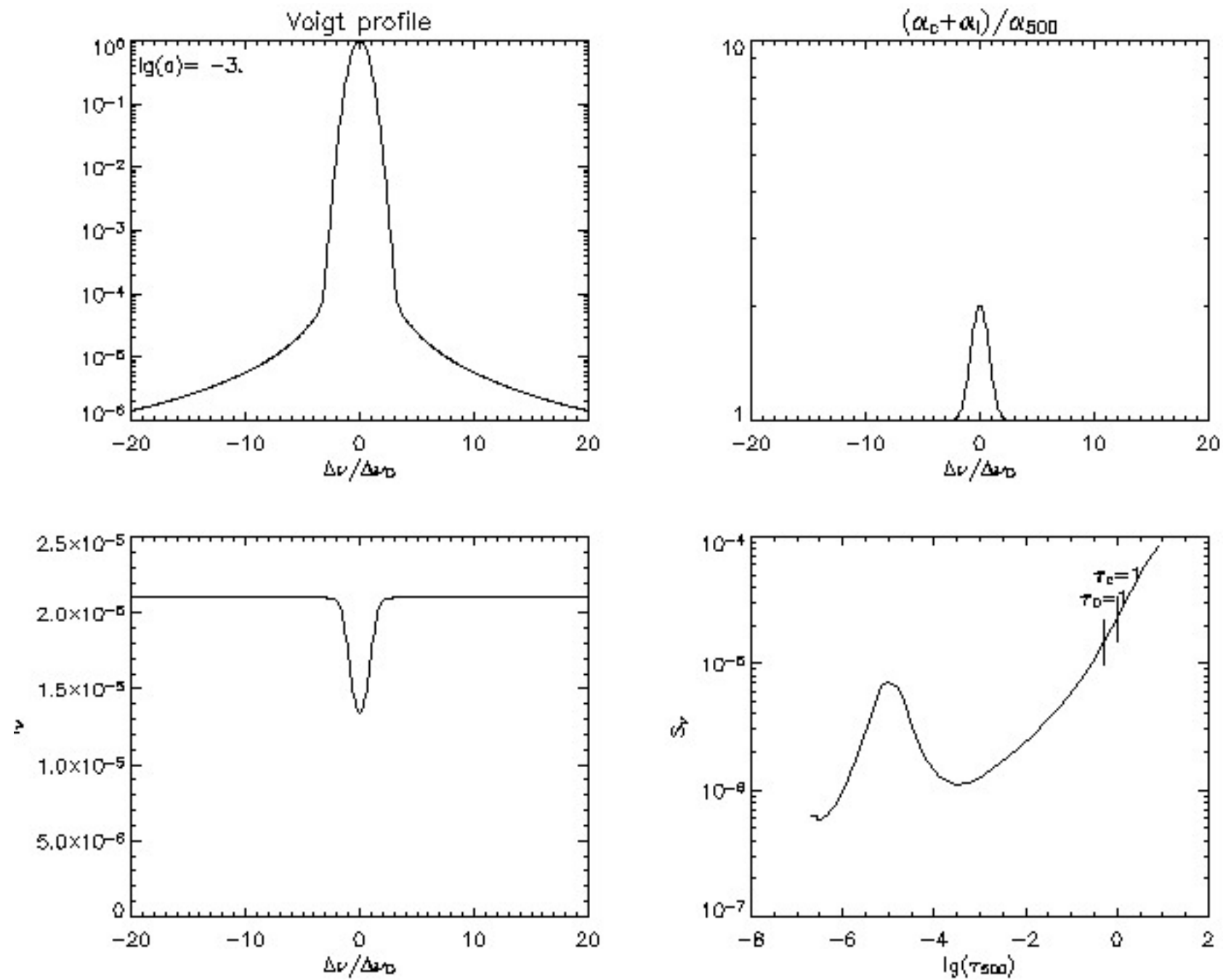
Optically thick line formation



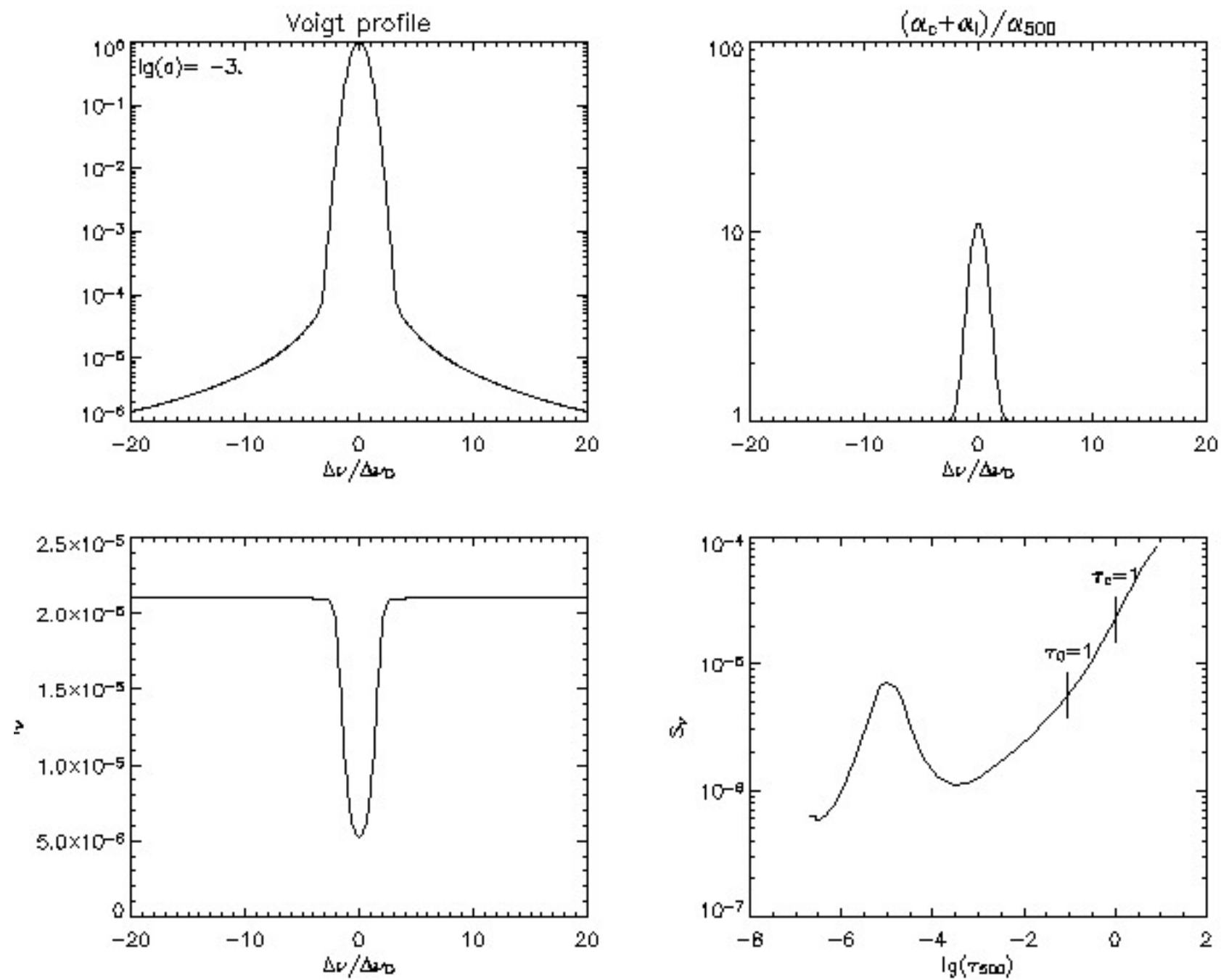
Optically thick line formation



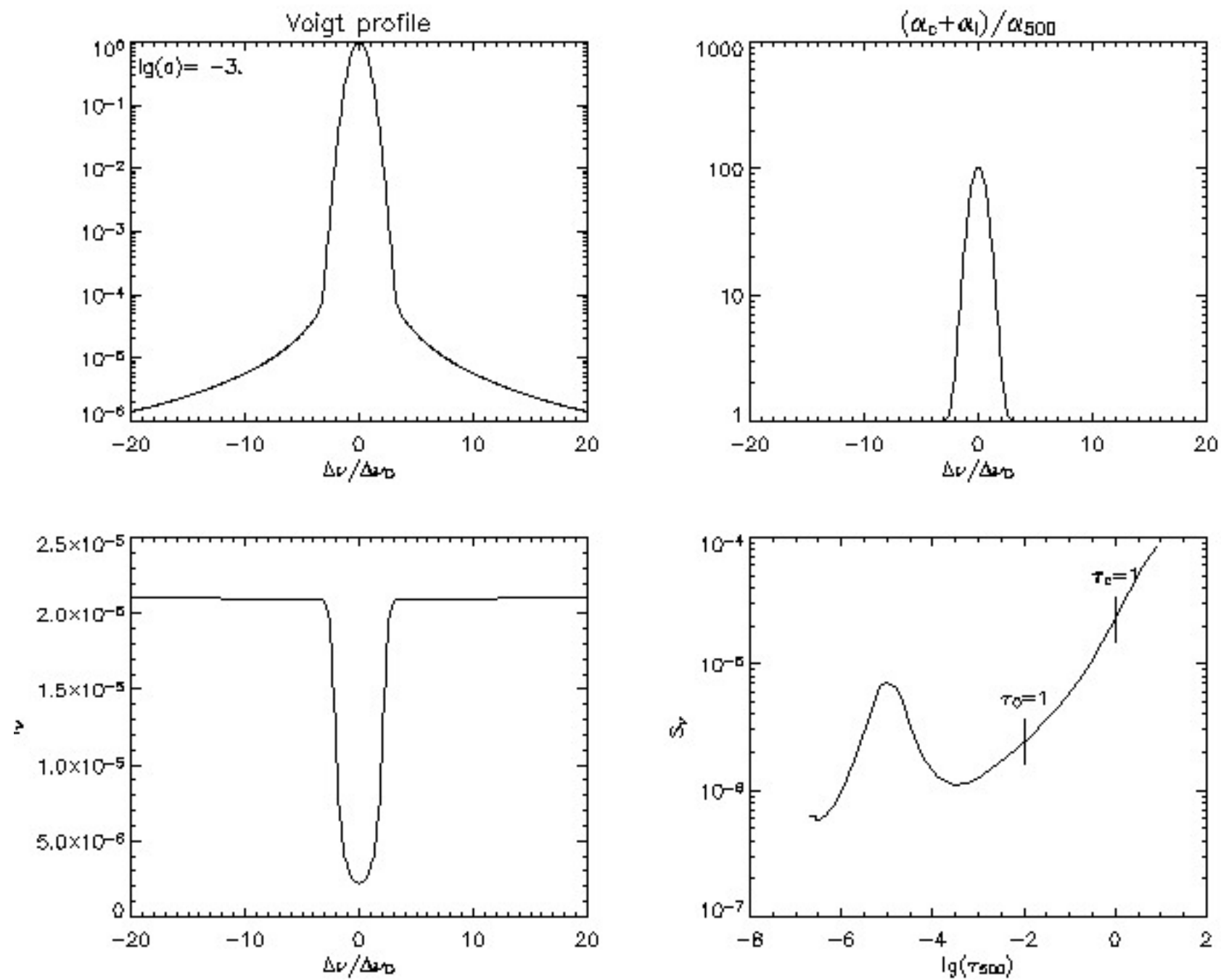
Optically thick line formation 3



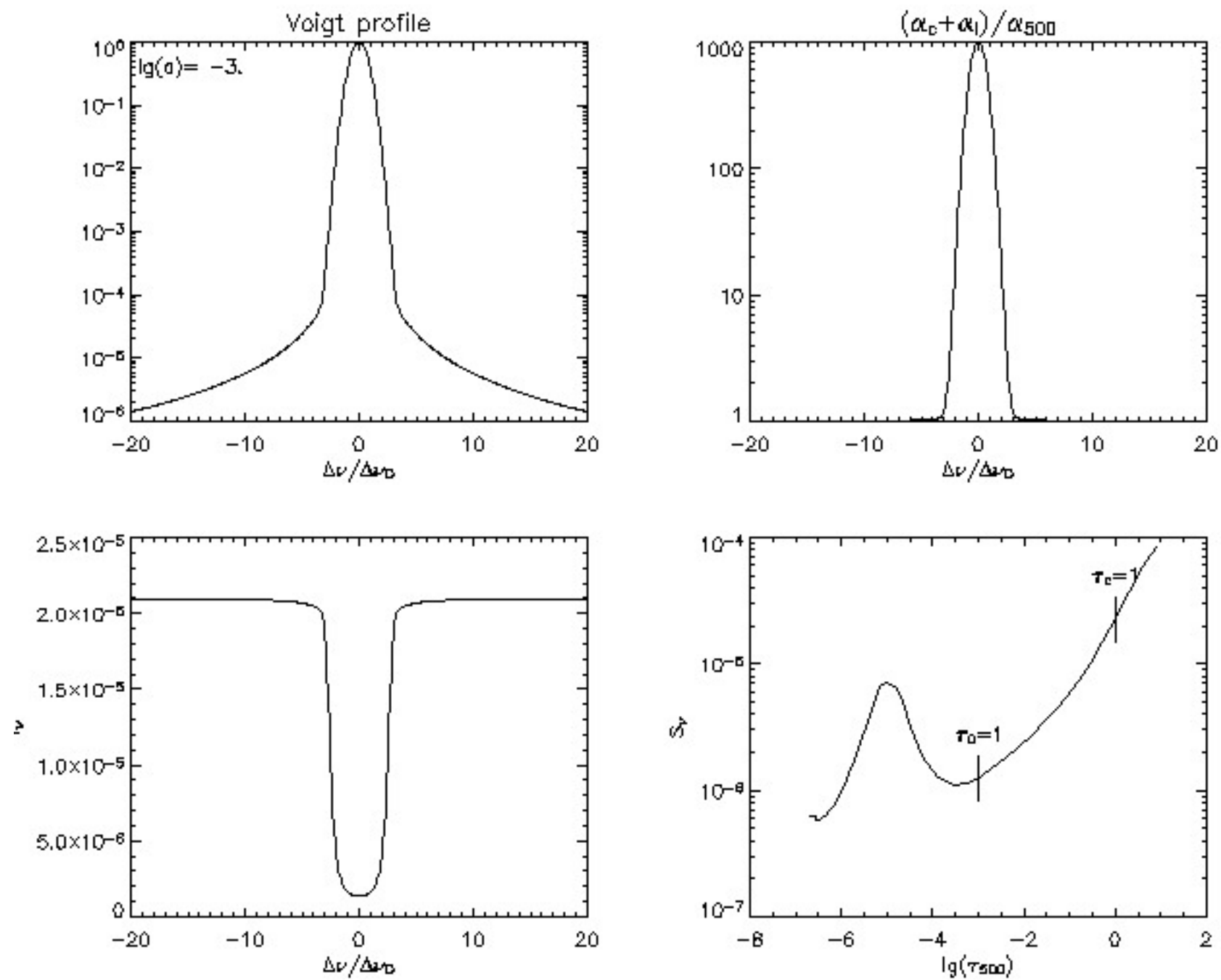
Optically thick line formation



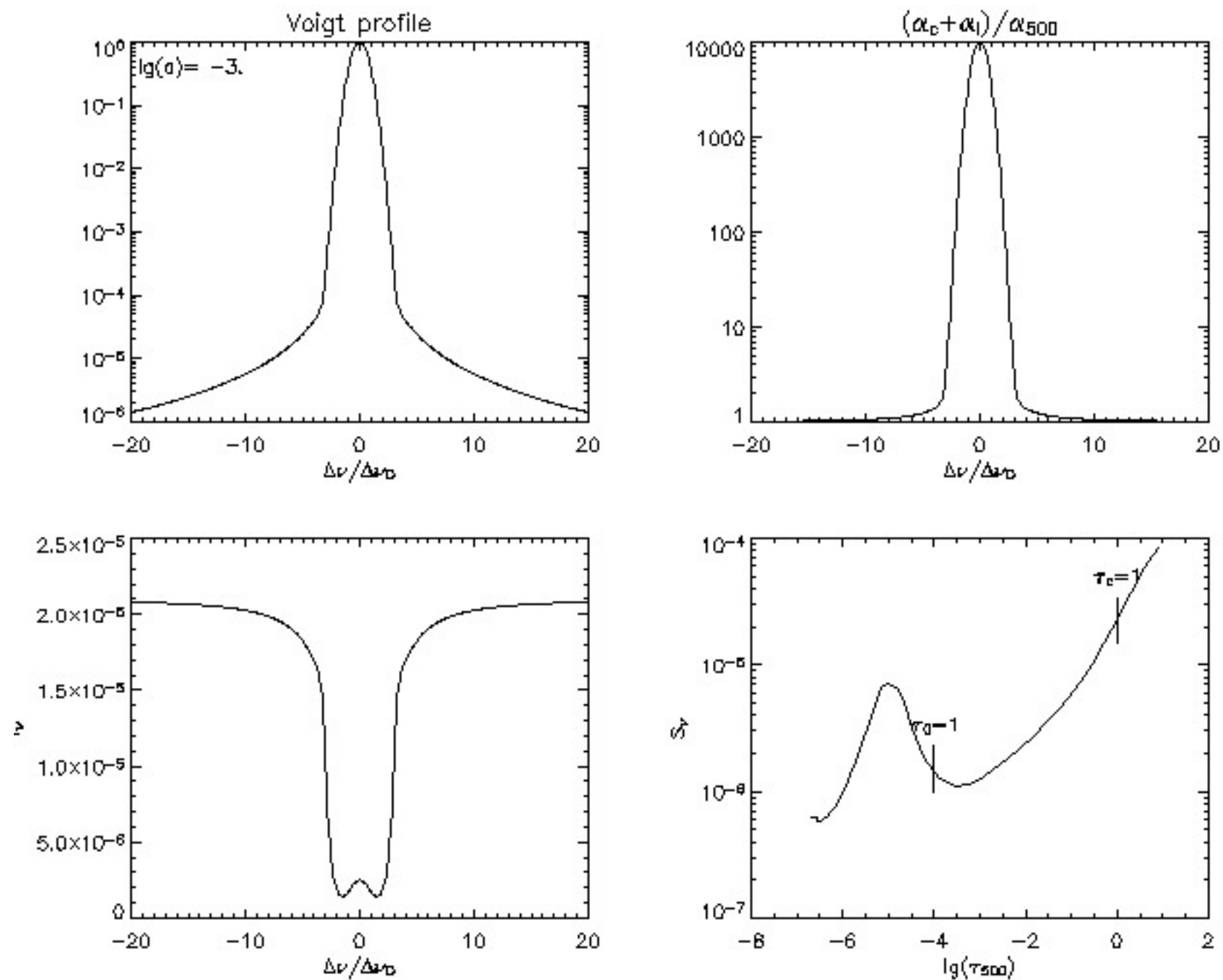
Optically thick line formation

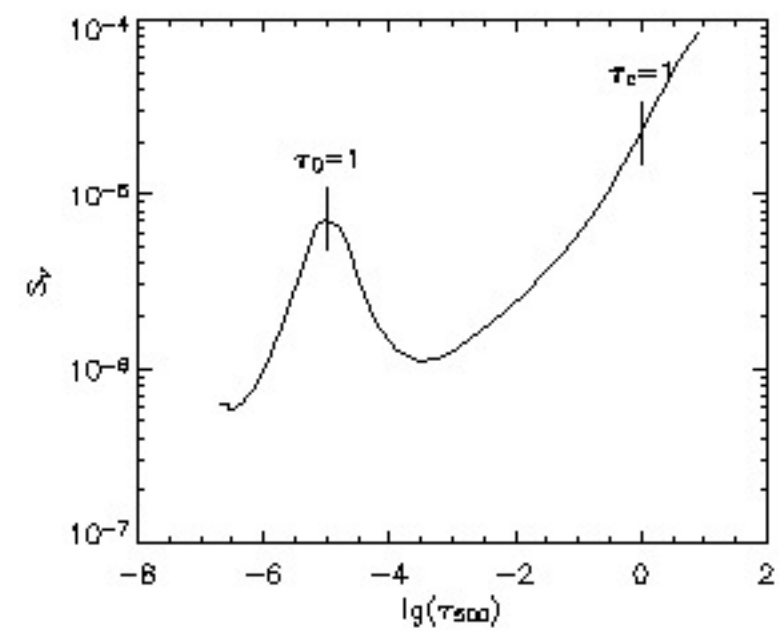
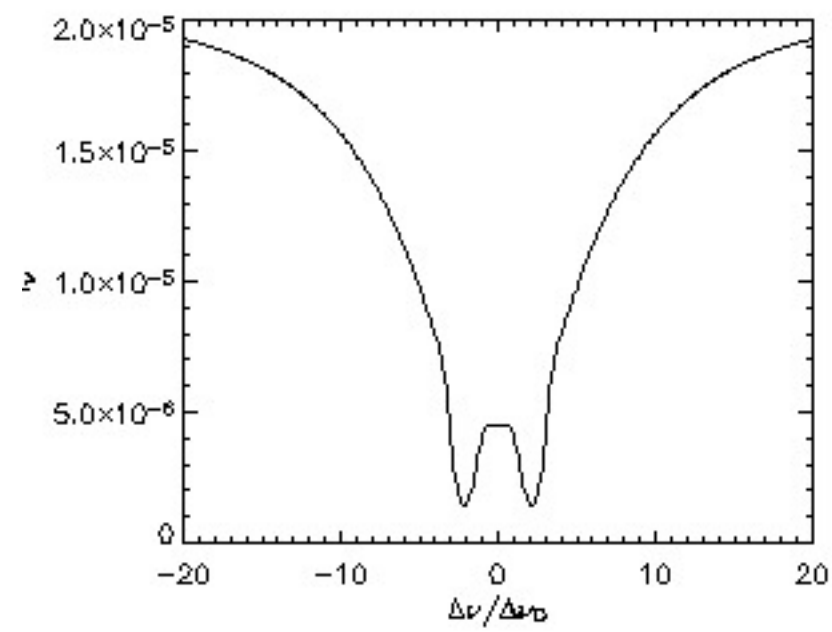
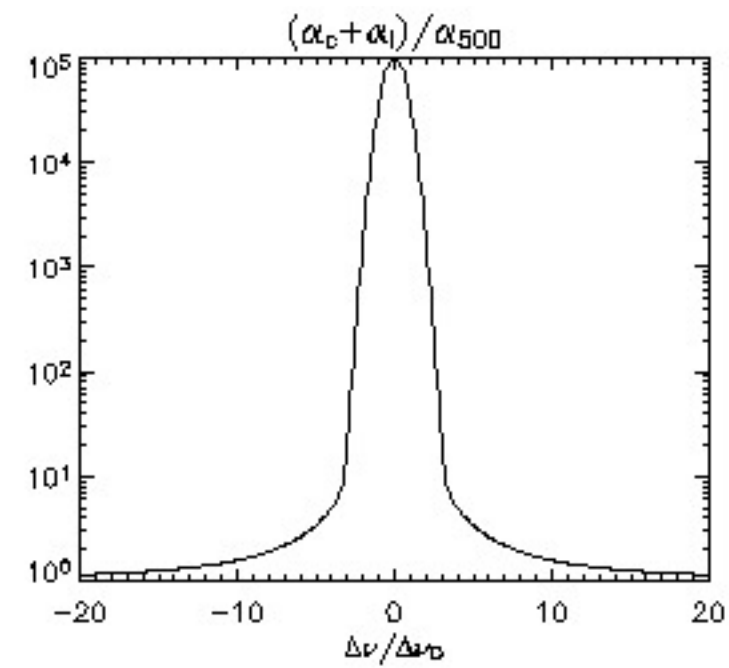
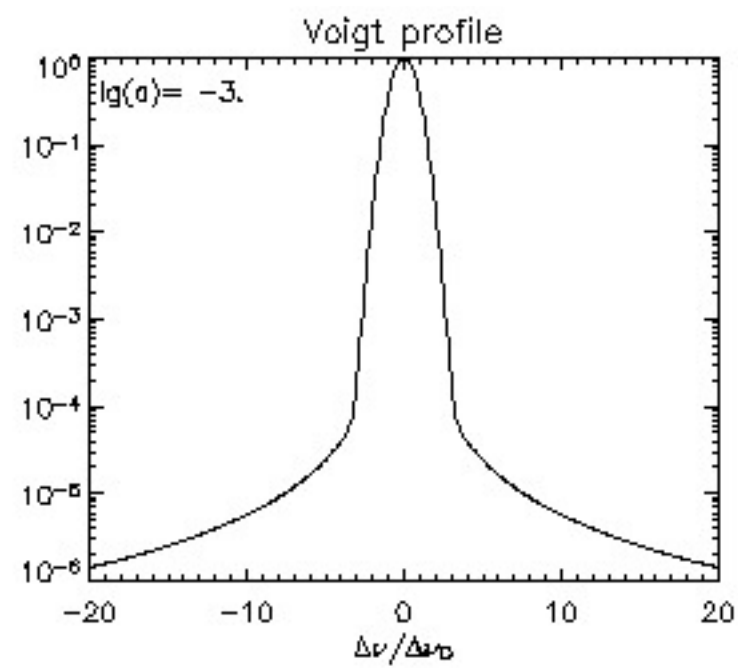


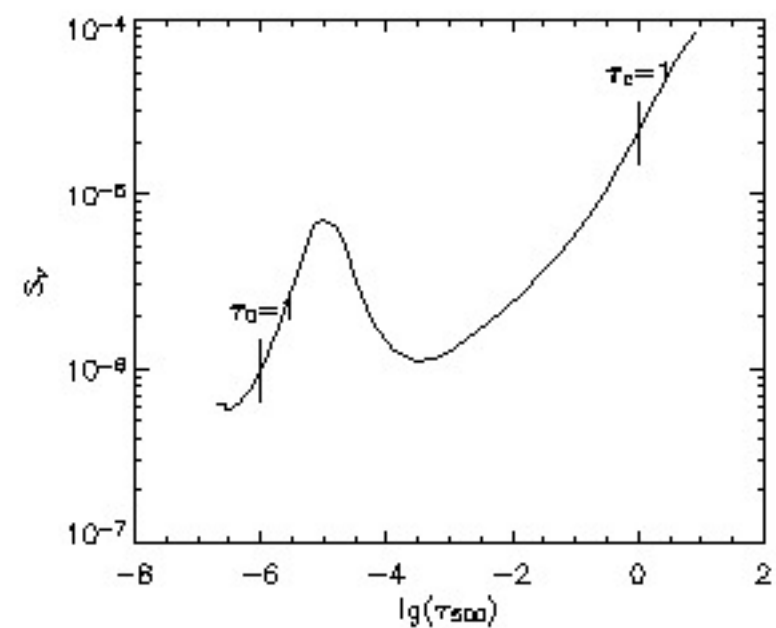
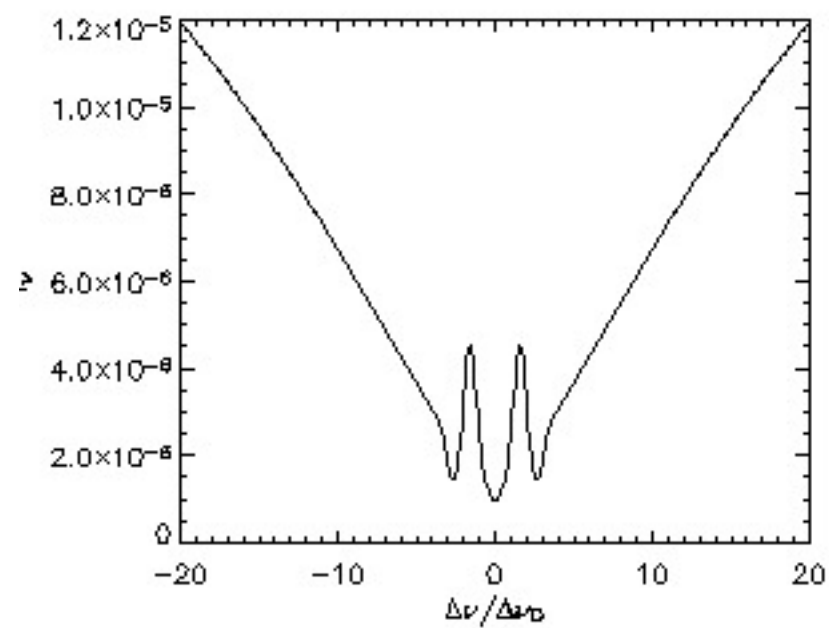
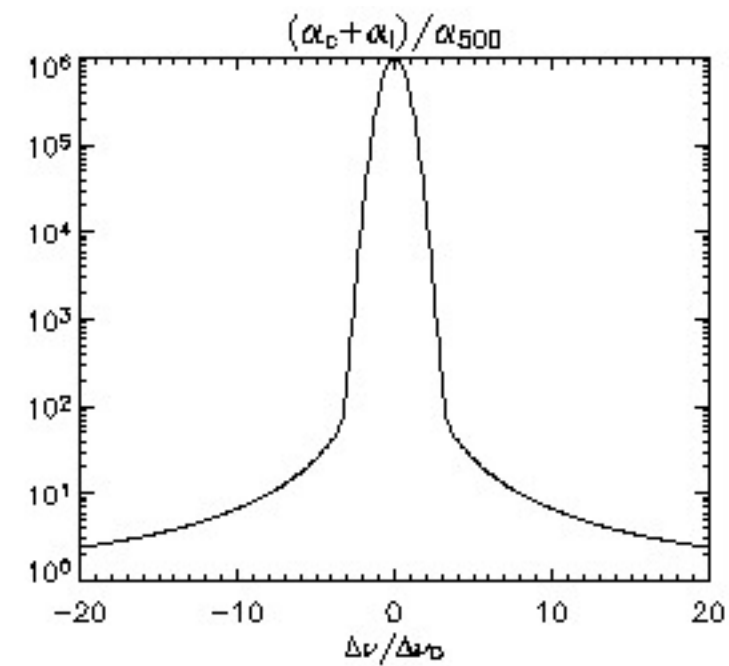
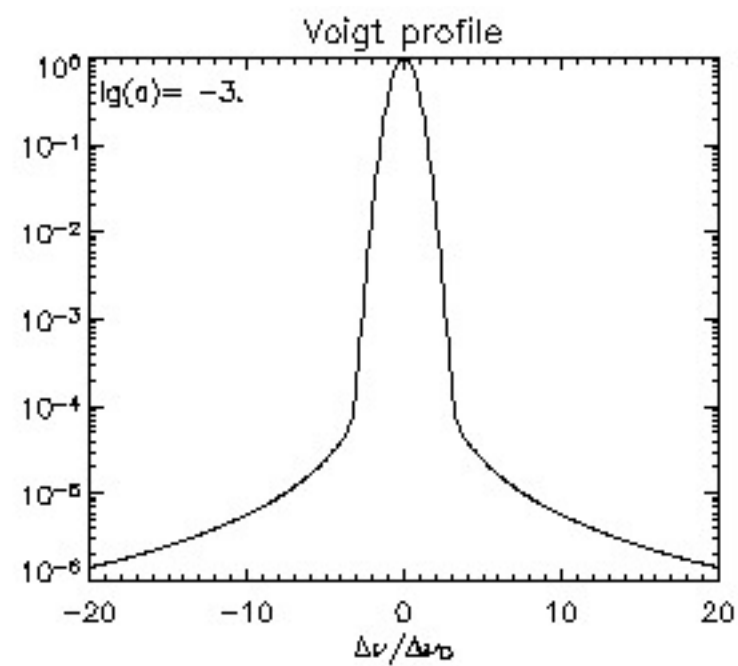
Optically thick line formation



Optically thick line formation

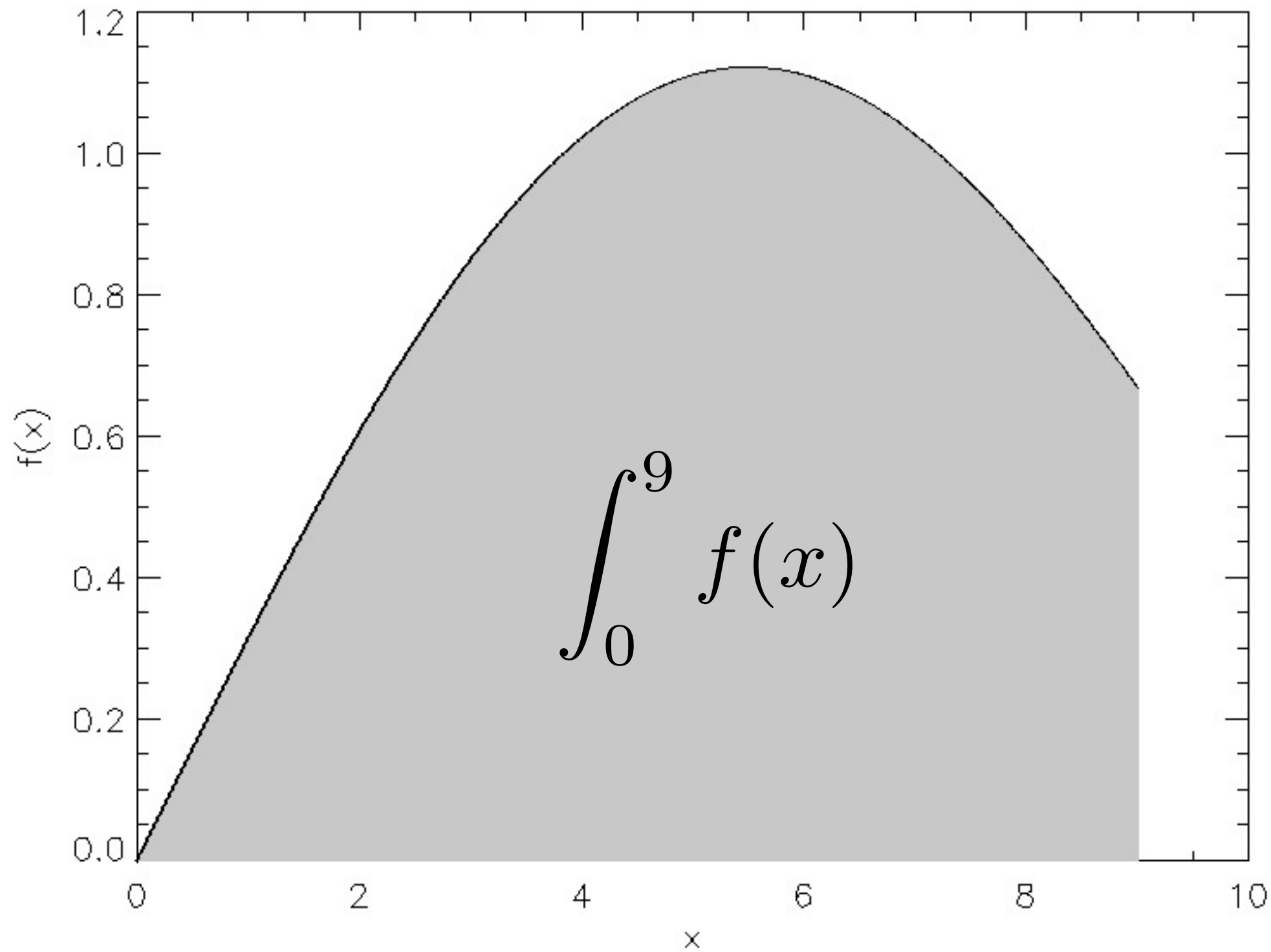


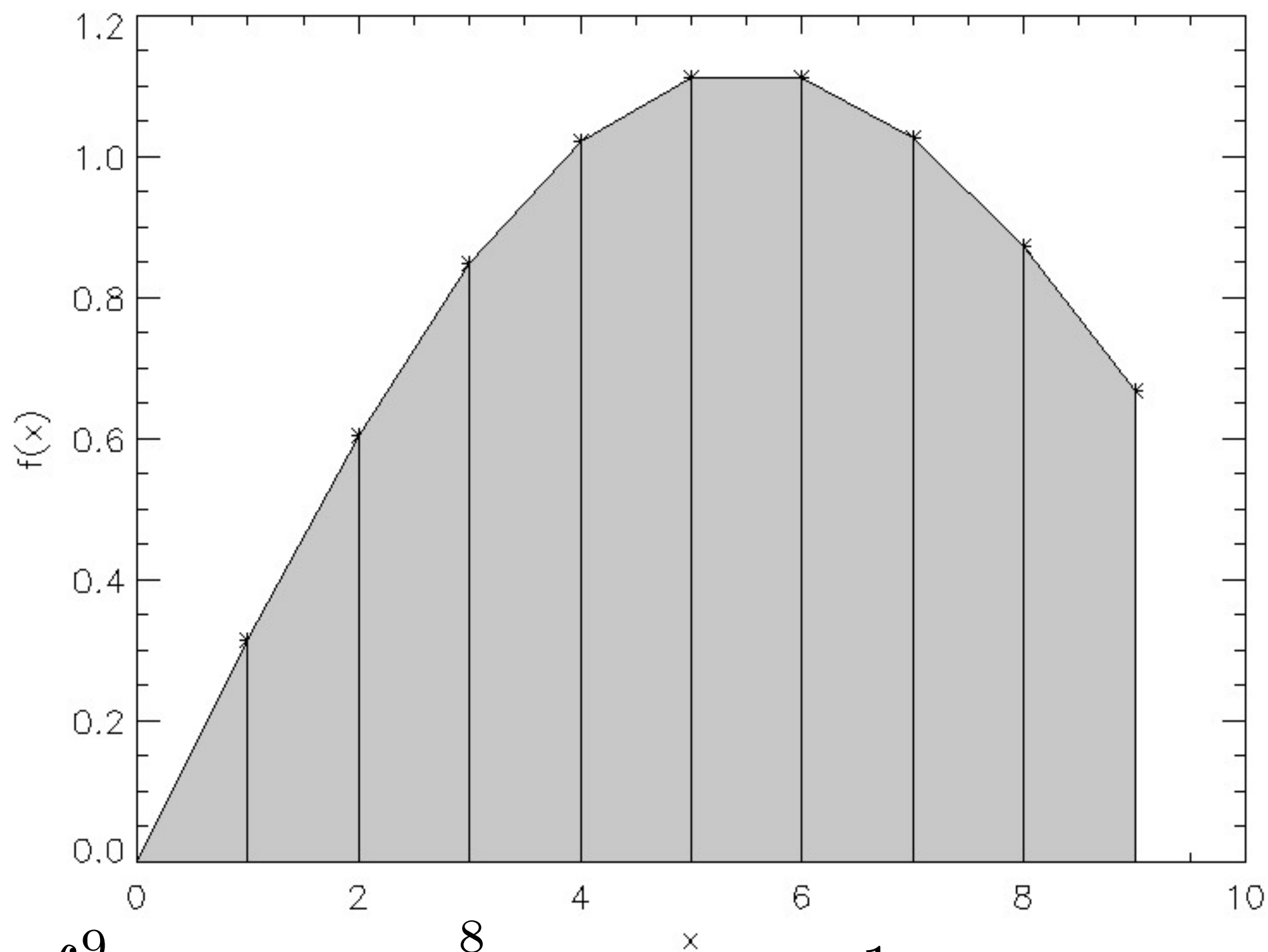




Numerical integration

Numerical integration (quadrature)





$$\int_0^9 f(x) dx \sim \sum_{i=0}^8 (x_{i+1} - x_i) \frac{1}{2} (f(x_{i+1}) + f(x_i))$$

$$\int_0^9 f(x)dx \sim \sum_{i=0}^8 (x_{i+1} - x_i) \frac{1}{2} (f(x_{i+1}) + f(x_i)) =$$

$$\frac{1}{2}(x_1 - x_0)f(x_0) + \sum_{i=1}^7 \frac{1}{2}(x_{i+1} - x_{i-1})f(x_i) +$$

$$\frac{1}{2}(x_9 - x_8)f(x_9)$$

In general:

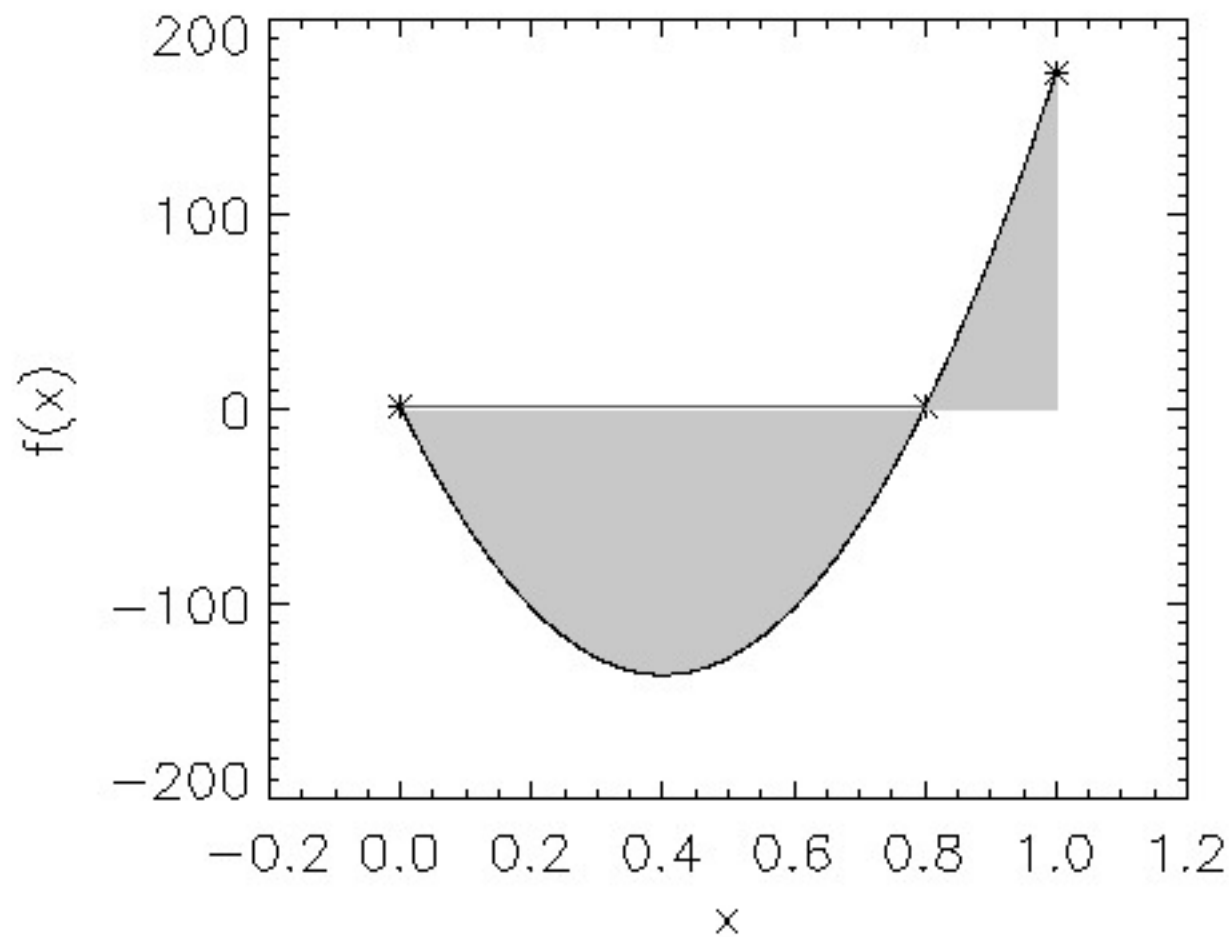
$$\int_a^b f(x)dx \sim \sum_{i=0}^{N-1} w_i f(x_i)$$

I. Grid points given

Trapezoidal: linear approximation between points

Simpson: parabolic between points

Higher accuracy but risk of overshoot



2. Integration method can determine points:

Gaussian quadratures

$$\int_a^b f(x)g(x)dx \sim \sum_{i=0}^{N-1} w_i f(x_i)$$

$$g(x) = 1 \quad \text{Gauss (-Legendre)}$$

$$g(x) = e^{-x}; a = 0; b = \infty \quad \text{Gauss-Laguerre}$$

Mean intensity: Gaussian quadrature

$$J_\nu(\tau_\nu) = \frac{1}{2} \int_{-1}^1 I_\nu(\tau_\nu, \mu) d\mu = \int_0^1 \frac{1}{2} (I_\nu^+(\tau_\nu, \mu) + I_\nu^-(\tau_\nu, \mu)) d\mu =$$
$$\sum_{i=0}^{N_\mu-1} w_i \frac{1}{2} (I_\nu^+(\tau_\nu, \mu_i) + I_\nu^-(\tau_\nu, \mu_i))$$

$$N_\mu = 3$$

w_i	μ_i
0.277778	0.112702
0.444444	0.500000
0.277778	0.887298

Intensity: Gauss-Laguerre quadrature

$$I_\nu(0) = \frac{1}{\mu} \int_0^\infty S_\nu(\tau_\nu) e^{-\tau_\nu/\mu} d\tau_\nu$$

$$d\tau_{\nu\mu} \equiv \frac{1}{\mu} d\tau_\nu \quad \tau_{\nu\mu} = \frac{1}{\mu} \tau_\nu$$

$$I_\nu(0) = \int_0^\infty S_\nu(\tau_{\nu\mu}) e^{-\tau_{\nu\mu}} d\tau_{\nu\mu}$$

	$(\tau_{\nu\mu})_i$	w_i	
$N_{\tau_{\nu\mu}} = 1$	1.0	1.0	=Eddington-Barbier

$N_{\tau_{\nu\mu}} = 2$	0.58579	0.85355
	3.41421	0.14645

Source function with scattering

Source function with scattering

$$\eta_\nu = \kappa_\nu B_\nu + \sigma_\nu J_\nu$$

$$\chi_\nu = \kappa_\nu + \sigma_\nu$$

$$S_\nu \equiv \frac{\eta_\nu}{\chi_\nu} = \frac{\kappa_\nu}{\kappa_\nu + \sigma_\nu} B_\nu + \frac{\sigma_\nu}{\kappa_\nu + \sigma_\nu} J_\nu$$

$$S_\nu = B_\nu + \frac{\sigma_\nu}{\kappa_\nu + \sigma_\nu} (J_\nu - B_\nu)$$

$$\rho_\nu \equiv \frac{\sigma_\nu}{\kappa_\nu + \sigma_\nu}$$

$$S_\nu = B_\nu + \rho_\nu (J_\nu - B_\nu)$$

Transfer equation, plane parallel atmosphere

$$\mu \frac{dI_\nu}{d\tau_\nu} = I_\nu - S_\nu$$

Boundary conditions:

$$\lim_{\tau_\nu \rightarrow \infty} (I_\nu e^{-\tau_\nu/\mu}) = 0 \quad I_\nu^-(0) = 0$$

$$I_\nu^+(\tau_\nu) = \frac{1}{\mu} \int_{\tau_\nu}^{\infty} S_\nu(\tau'_\nu) e^{-(\tau'_\nu - \tau_\nu)/\mu} d\tau'_\nu$$

$$I_\nu^-(\tau_\nu) = \frac{1}{\mu} \int_0^{\tau_\nu} S_\nu(\tau'_\nu) e^{-(\tau_\nu - \tau'_\nu)/\mu} d\tau'_\nu$$

$$J_\nu(\tau_\nu) = \frac{1}{2} \int_{-1}^1 I_\nu(\tau_\nu, \mu) d\mu = \int_0^1 \frac{1}{2} (I_\nu^+(\tau_\nu, \mu) + I_\nu^-(\tau_\nu, \mu)) d\mu \equiv \Lambda_\nu[S_\nu]$$

$$J_\nu(\tau_\nu) = \Lambda_\nu[S_\nu] = \Lambda_\nu[B_\nu] + \Lambda_\nu[\rho_\nu(J_\nu - B_\nu)]$$

Λ -iteration:

$$\begin{cases} J_\nu^{(n+1)}(\tau_\nu) &= \Lambda_\nu[B_\nu] + \Lambda_\nu[\rho_\nu(J_\nu^{(n)} - B_\nu)] \\ J^{(0)}(\tau_\nu) &= B_\nu \end{cases}$$

If $\rho_\nu \sim 1$ this scheme won't work

Cases when scattering dominates:

Hot stars, opacity dominated by electron scattering

Cool stars, low [Fe/H]: Rayleigh scattering dominates

Spectral lines: $1 - \rho_\nu \sim 10^{-8}$

Alternative form

$$S_\nu = (1 - \epsilon_\nu)J_\nu + \epsilon_\nu B_\nu$$

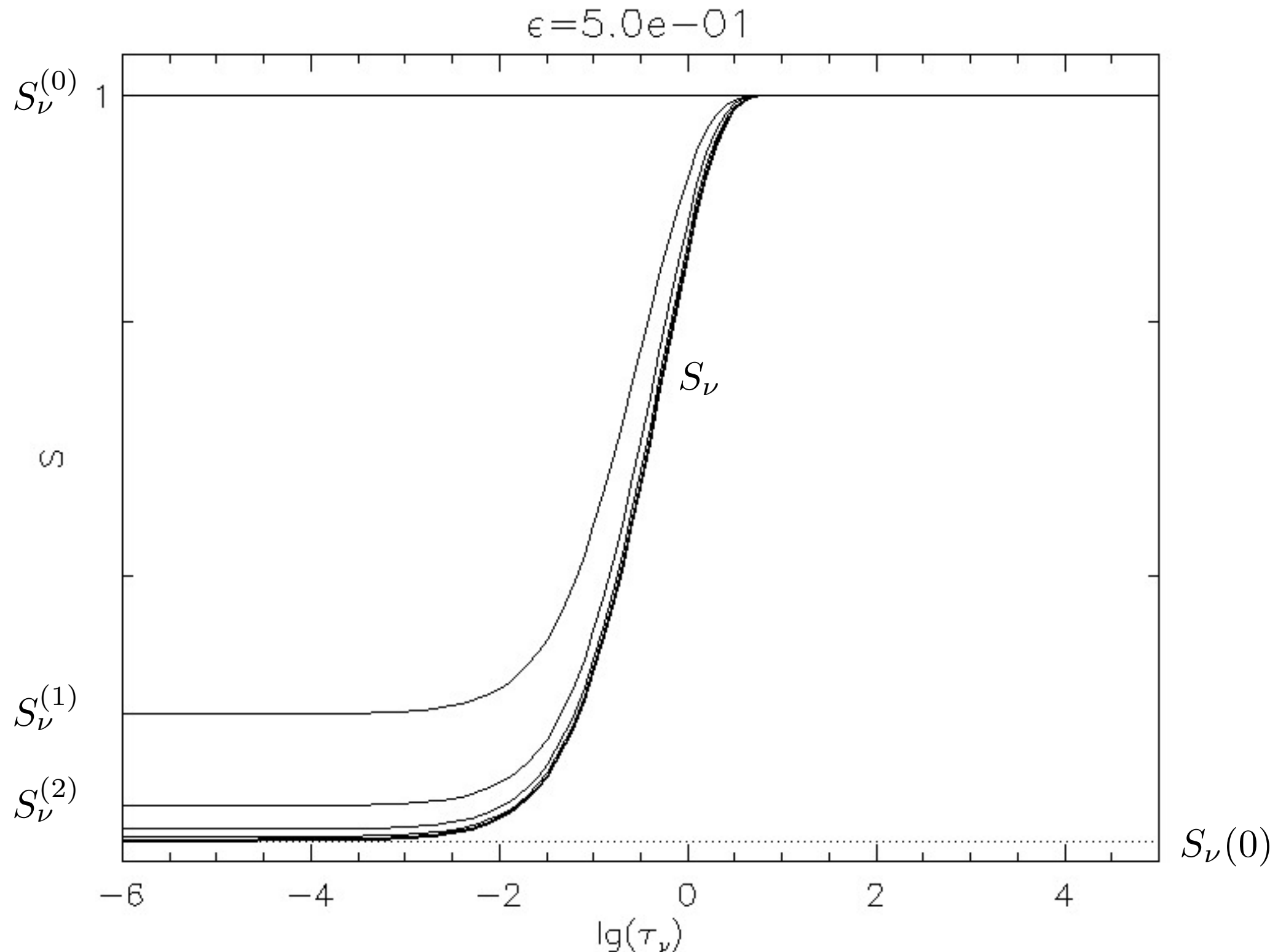
$$S_\nu = (1 - \epsilon_\nu)\Lambda_\nu[S_\nu] + \epsilon_\nu B_\nu$$

Λ -iteration:

$$\begin{cases} S_\nu^{(n+1)} &= (1 - \epsilon_\nu)\Lambda_\nu[S_\nu^{(n)}] + \epsilon_\nu B_\nu \\ S_\nu^{(0)} &= B_\nu \end{cases}$$

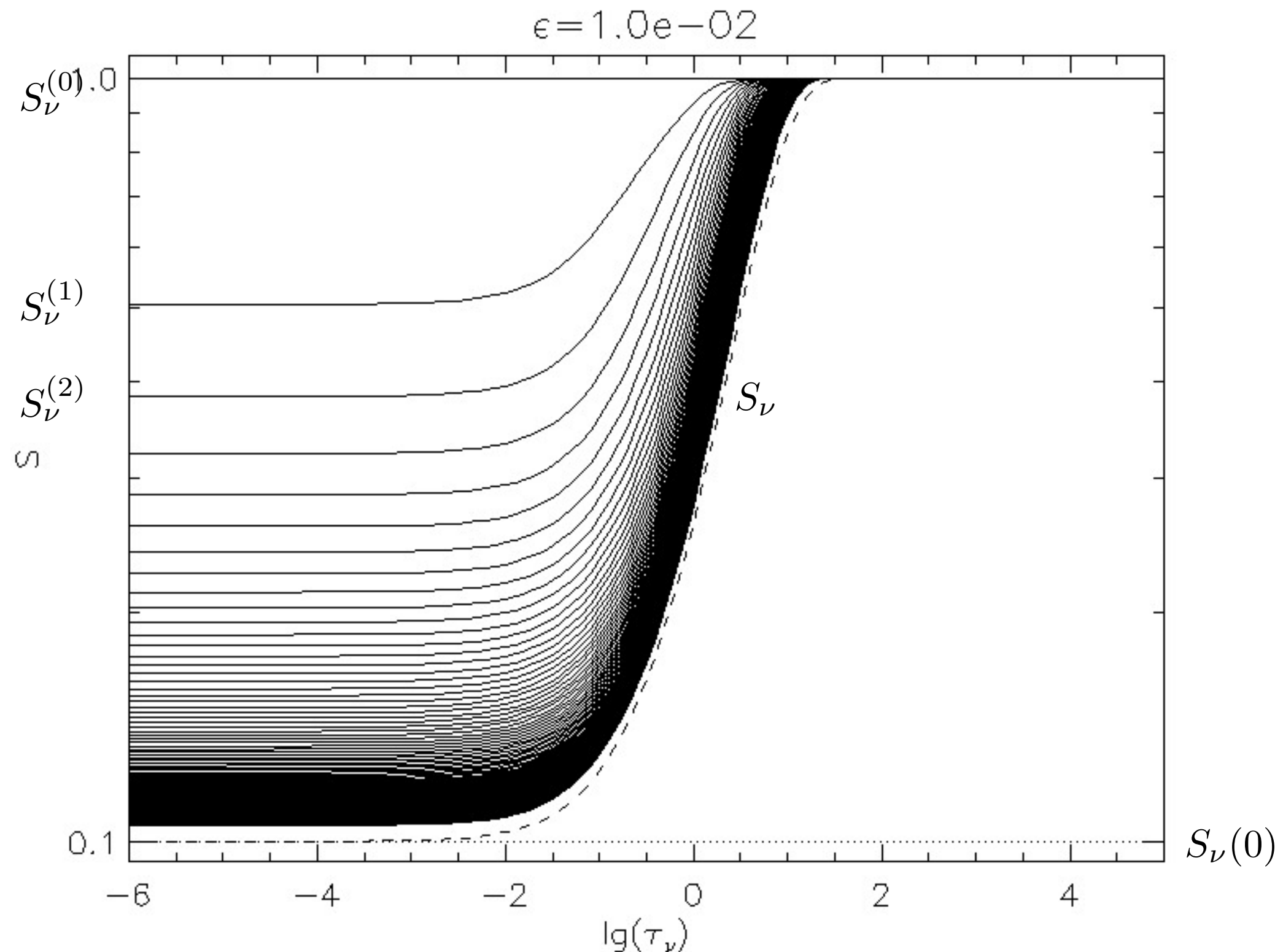
Lambda-iteration in practice, 100 iterations

$$S_\nu = \epsilon_\nu B_\nu + (1 - \epsilon_\nu) J_\nu \quad ; \quad B_\nu = 1$$



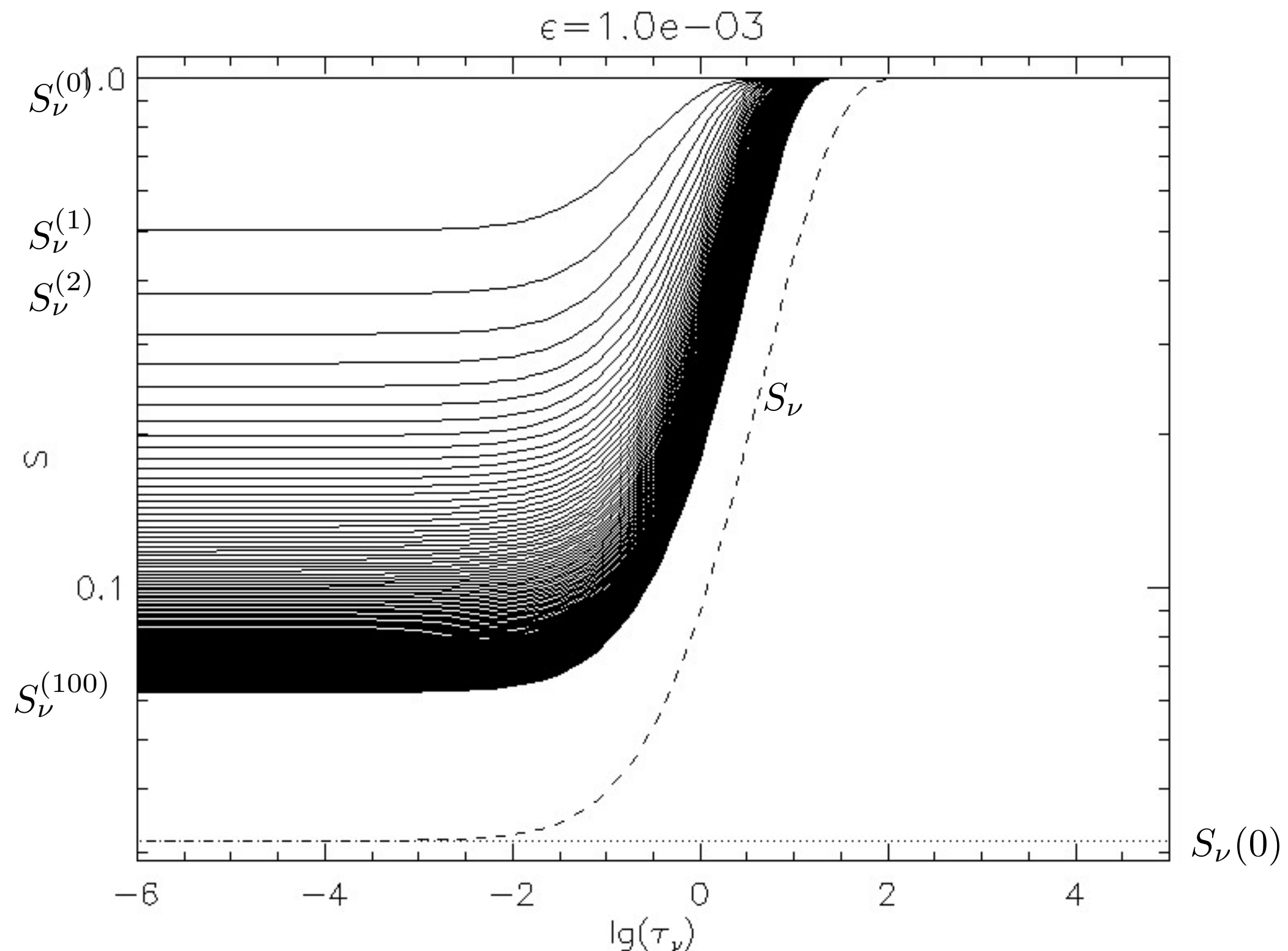
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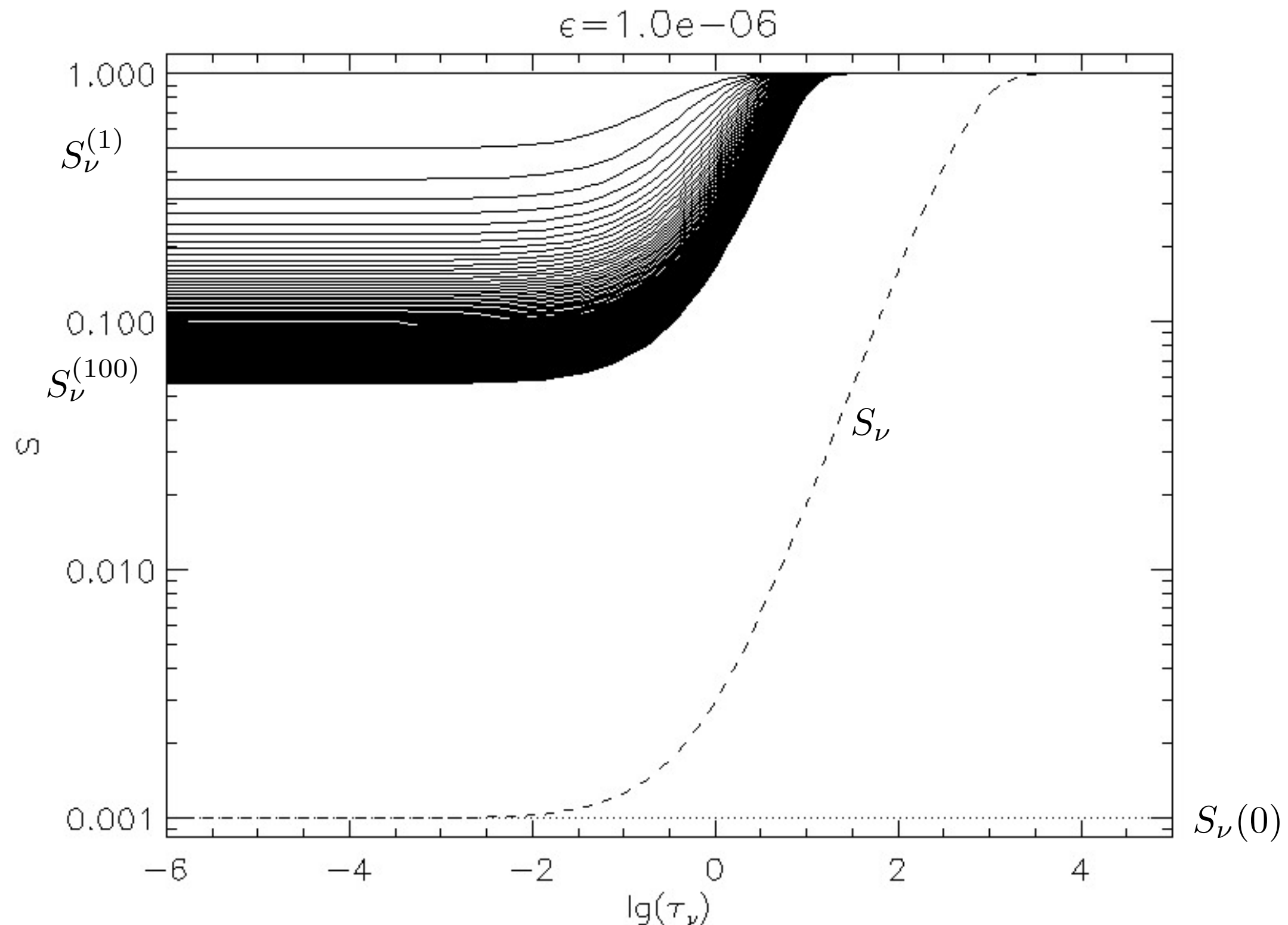
Lambda-iteration in practice, 100 iterations

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Lambda-iteration in practice, 100 iterations

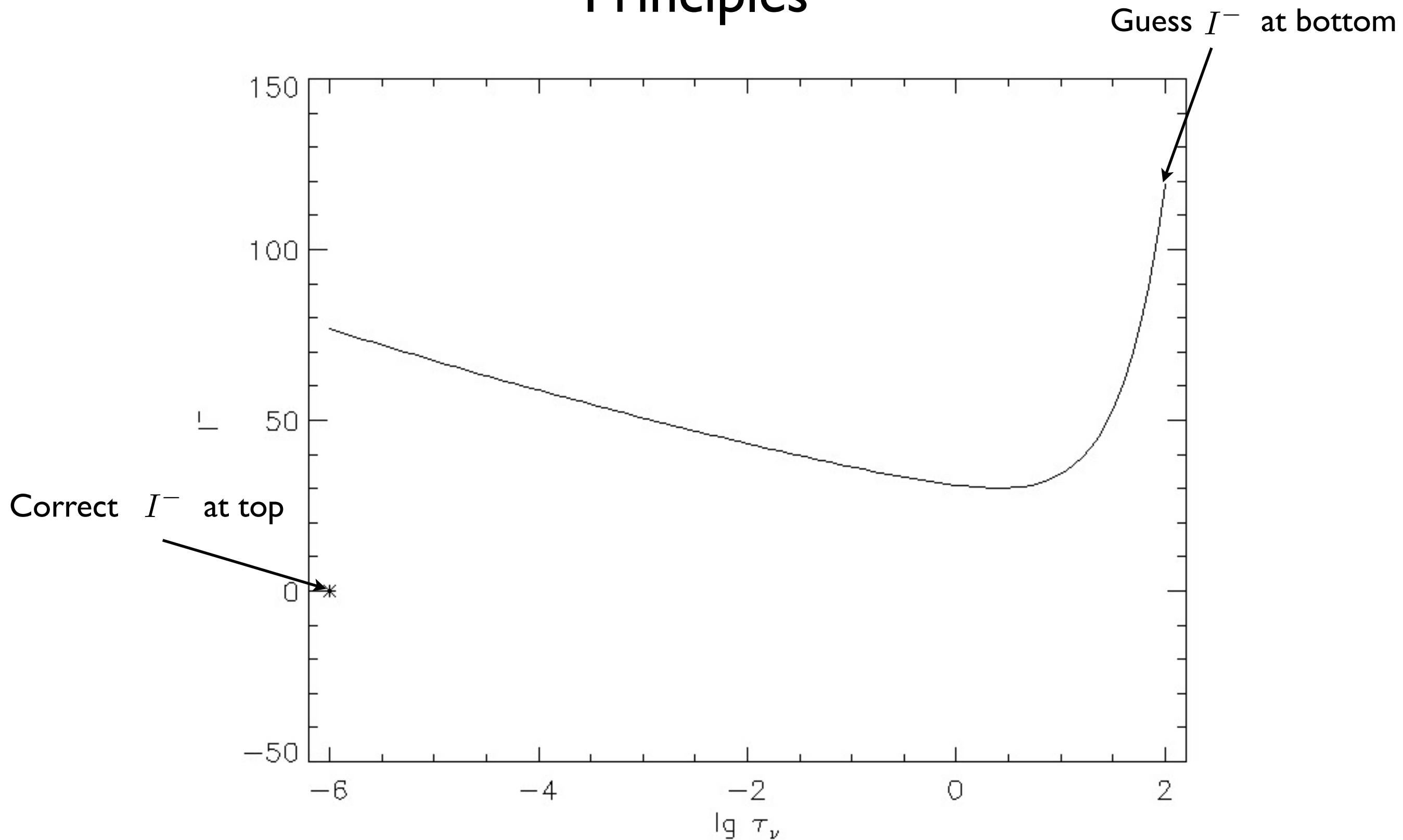
$$S_\nu = \epsilon_\nu B_\nu + (1 - \epsilon_\nu) J_\nu \quad ; \quad B_\nu = 1$$



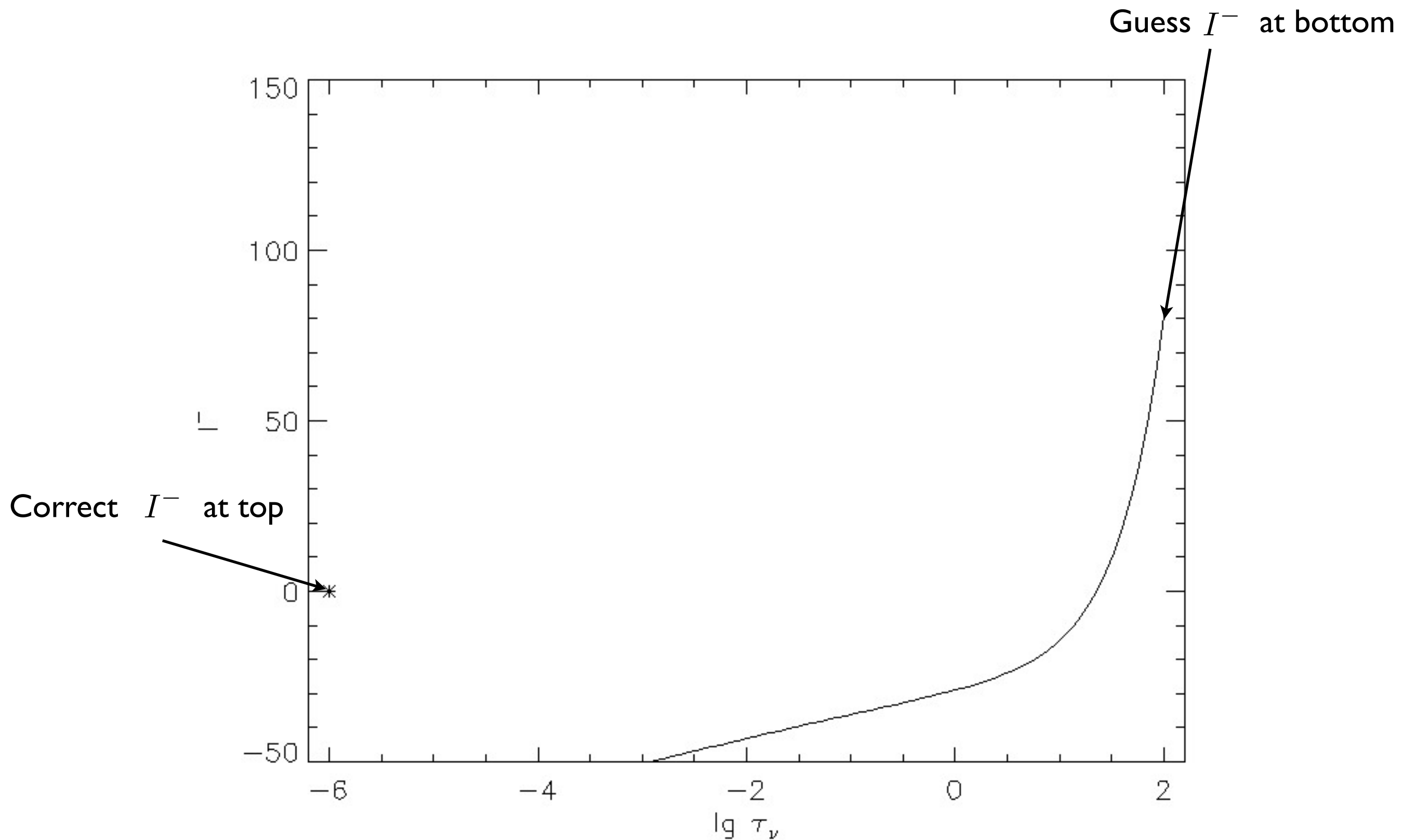
Lambda-iteration in practice

- OK if scattering is small
- Disaster for small epsilon
- Stabilizes instead of converging when epsilon is small (0.5% correction at iteration 100 for $\epsilon=10^{-6}$ when solution is a factor of 55 from correct solution)

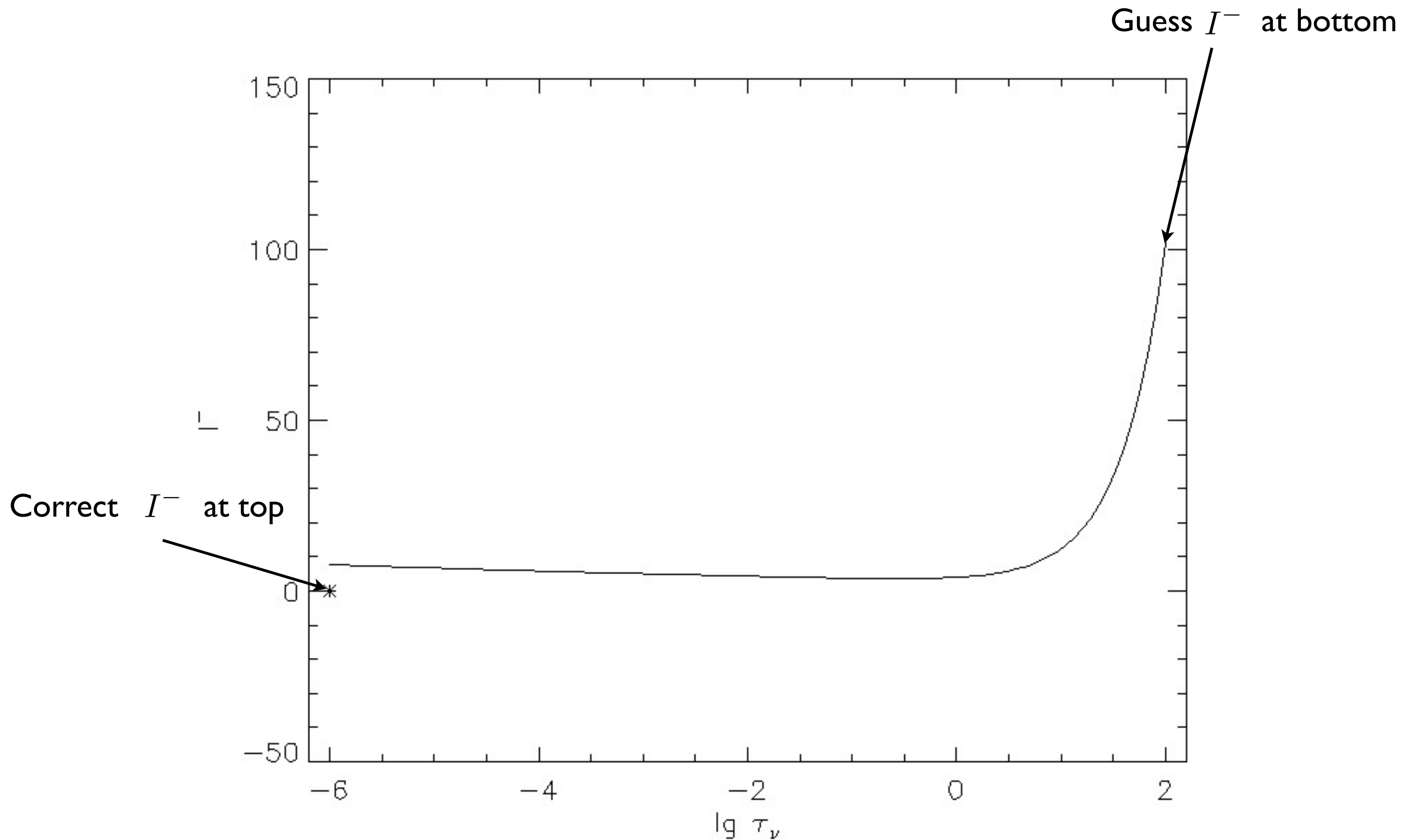
Shooting Principles



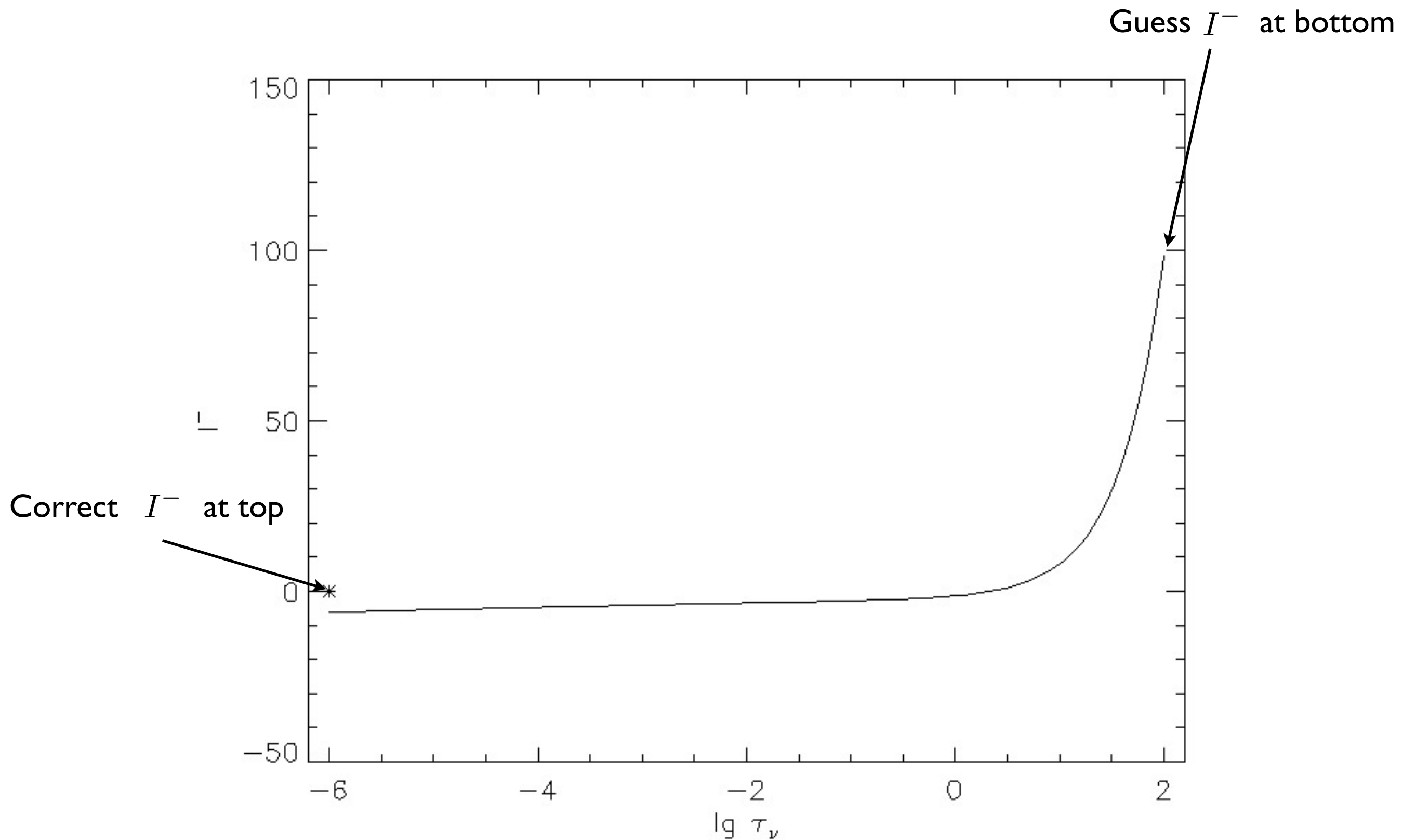
Shooting



Shooting

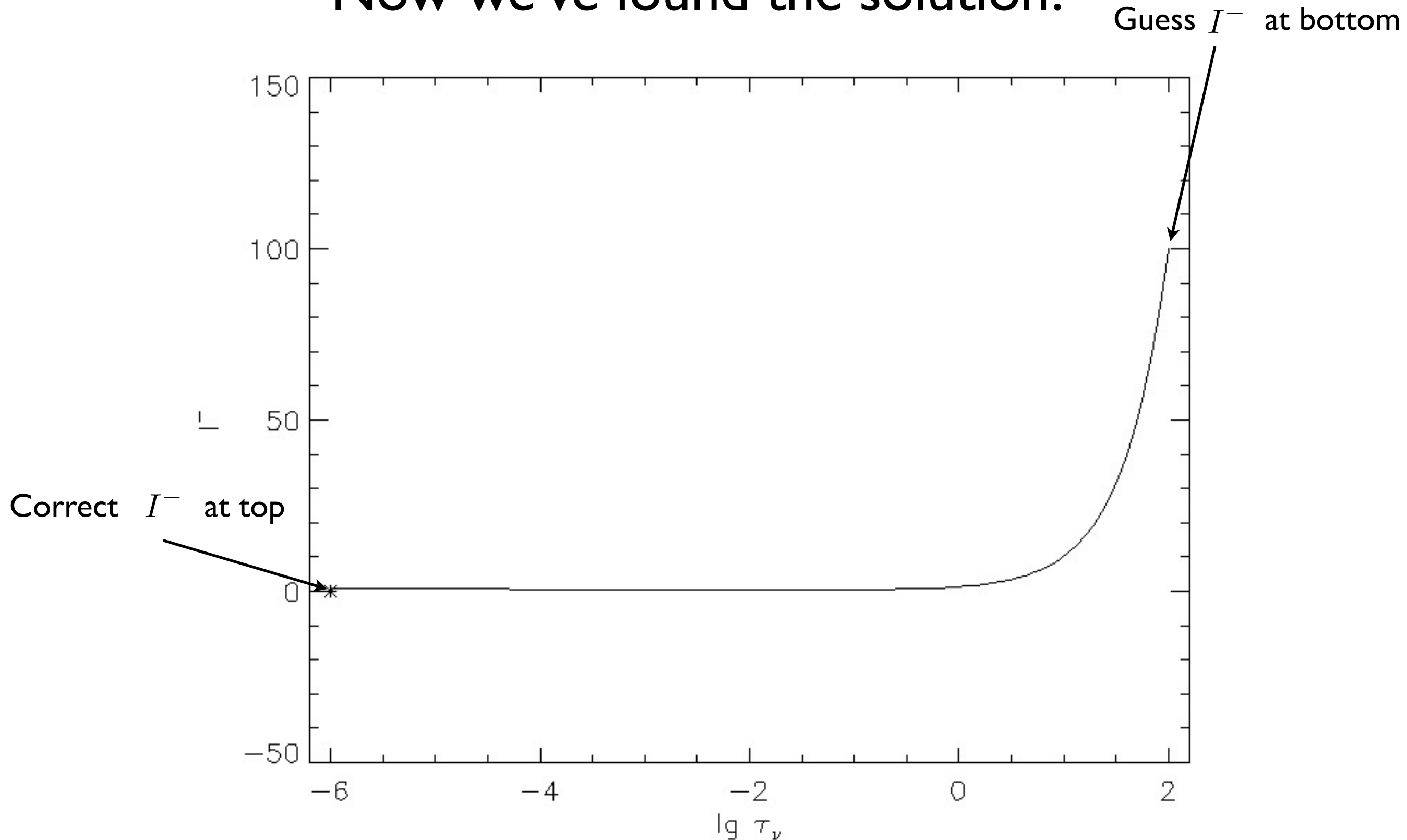


Shooting



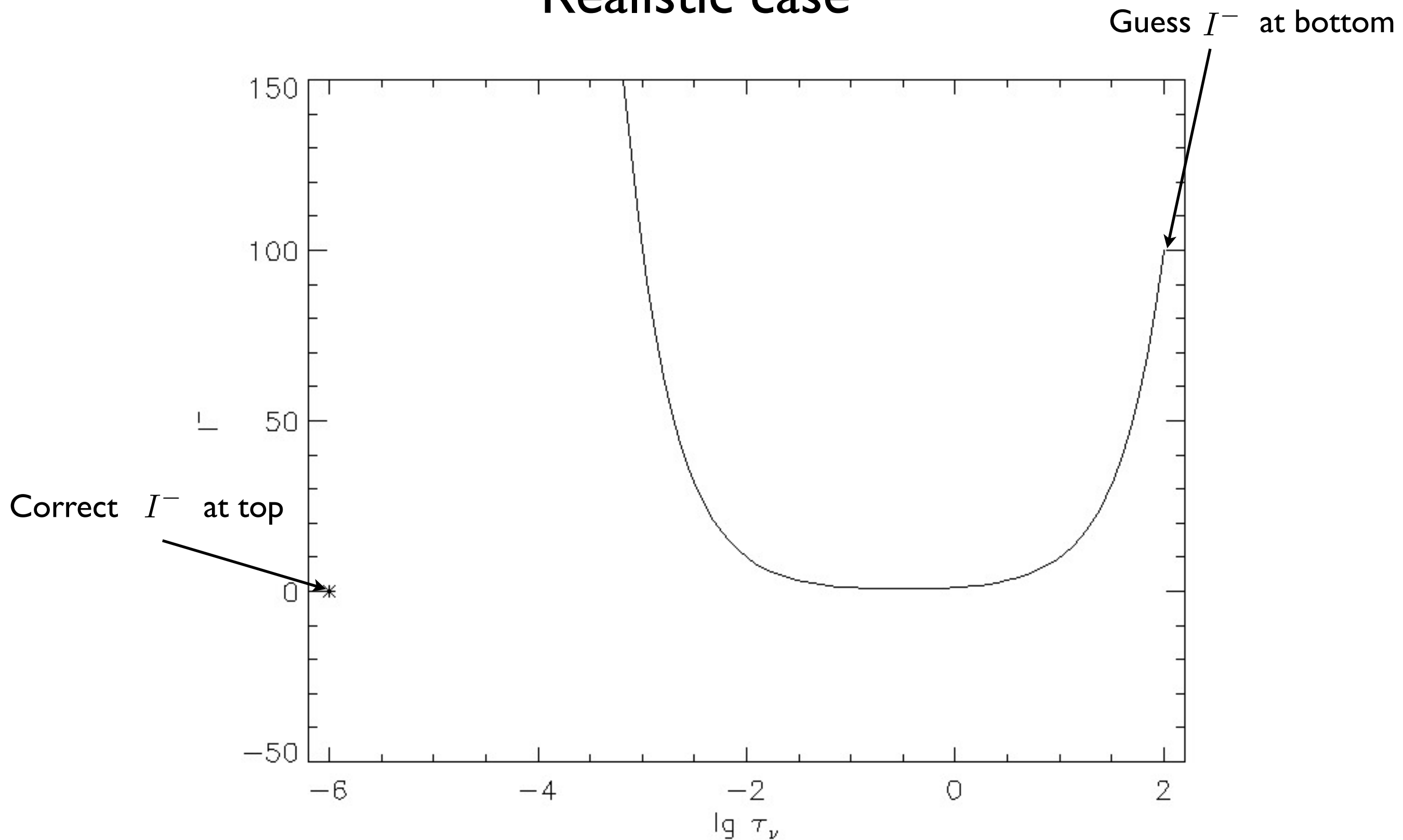
Shooting

Now we've found the solution!

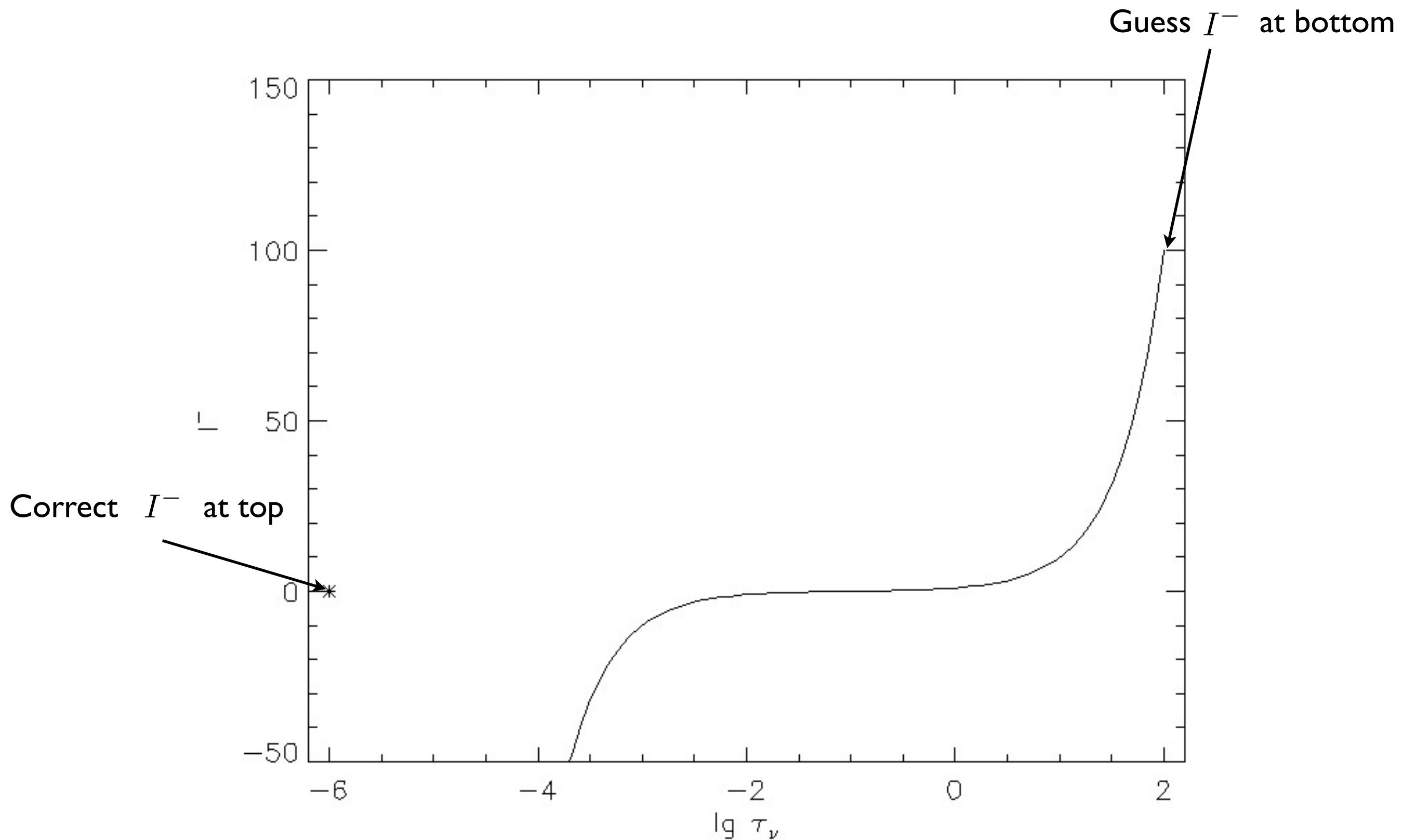


Shooting

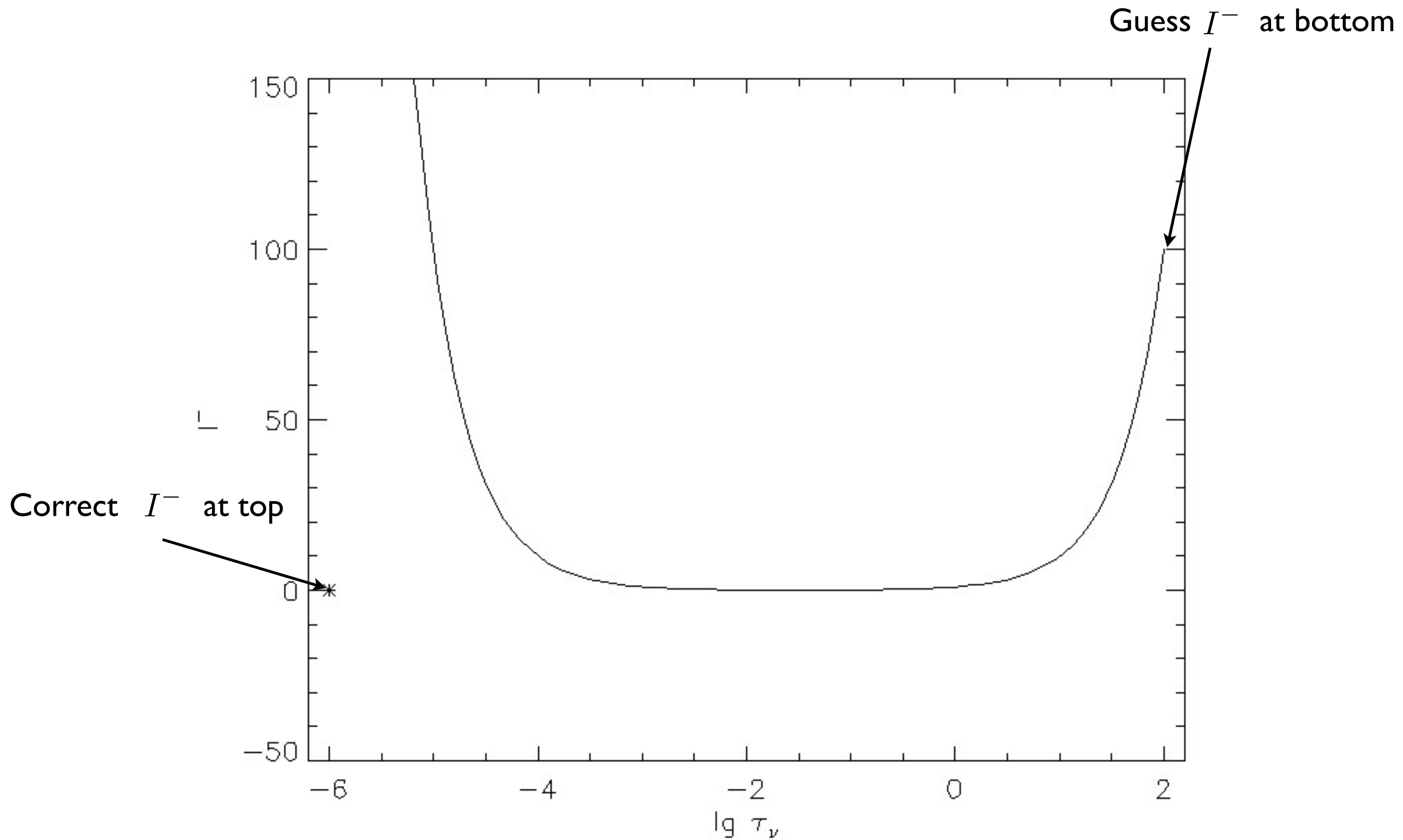
Realistic case



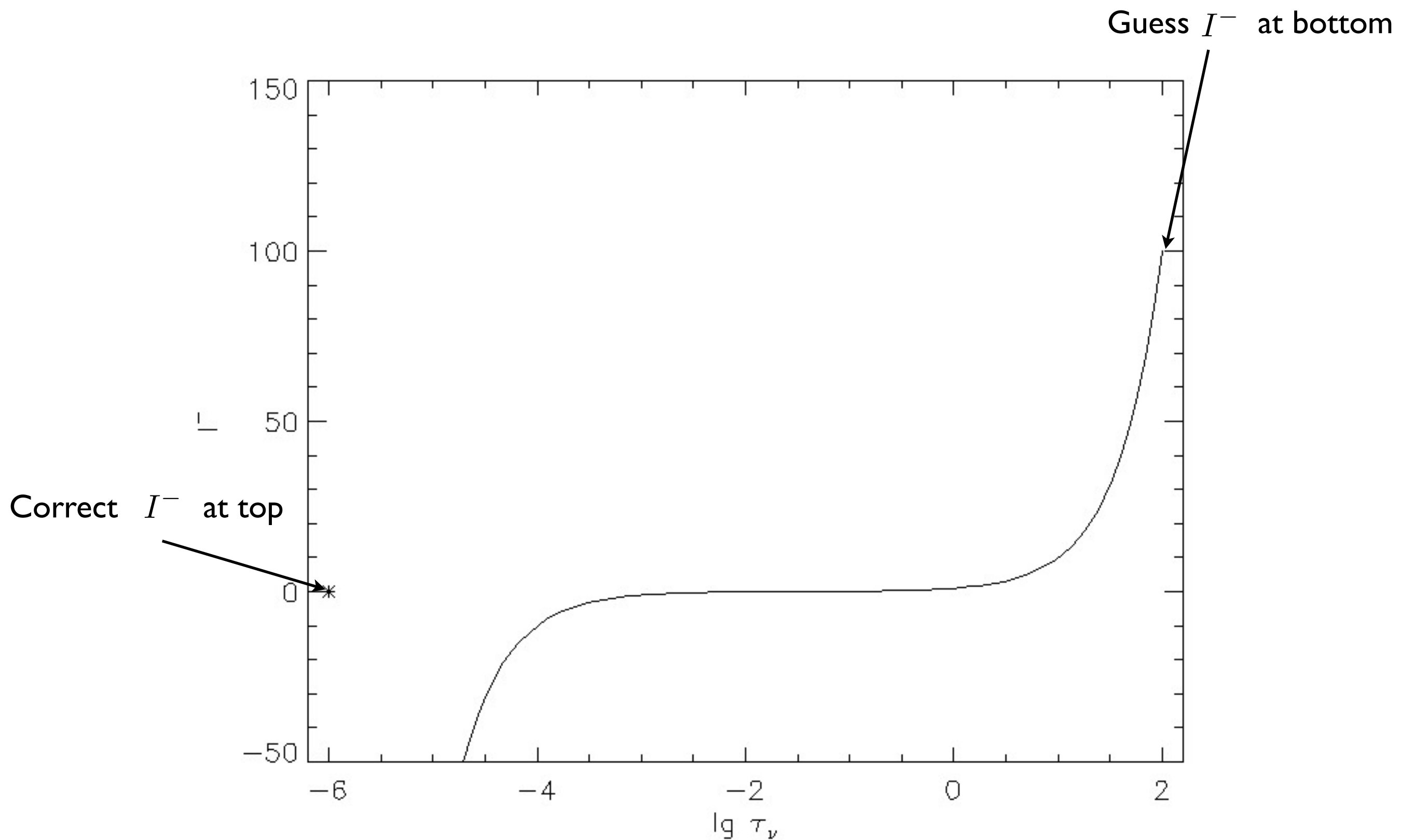
Shooting



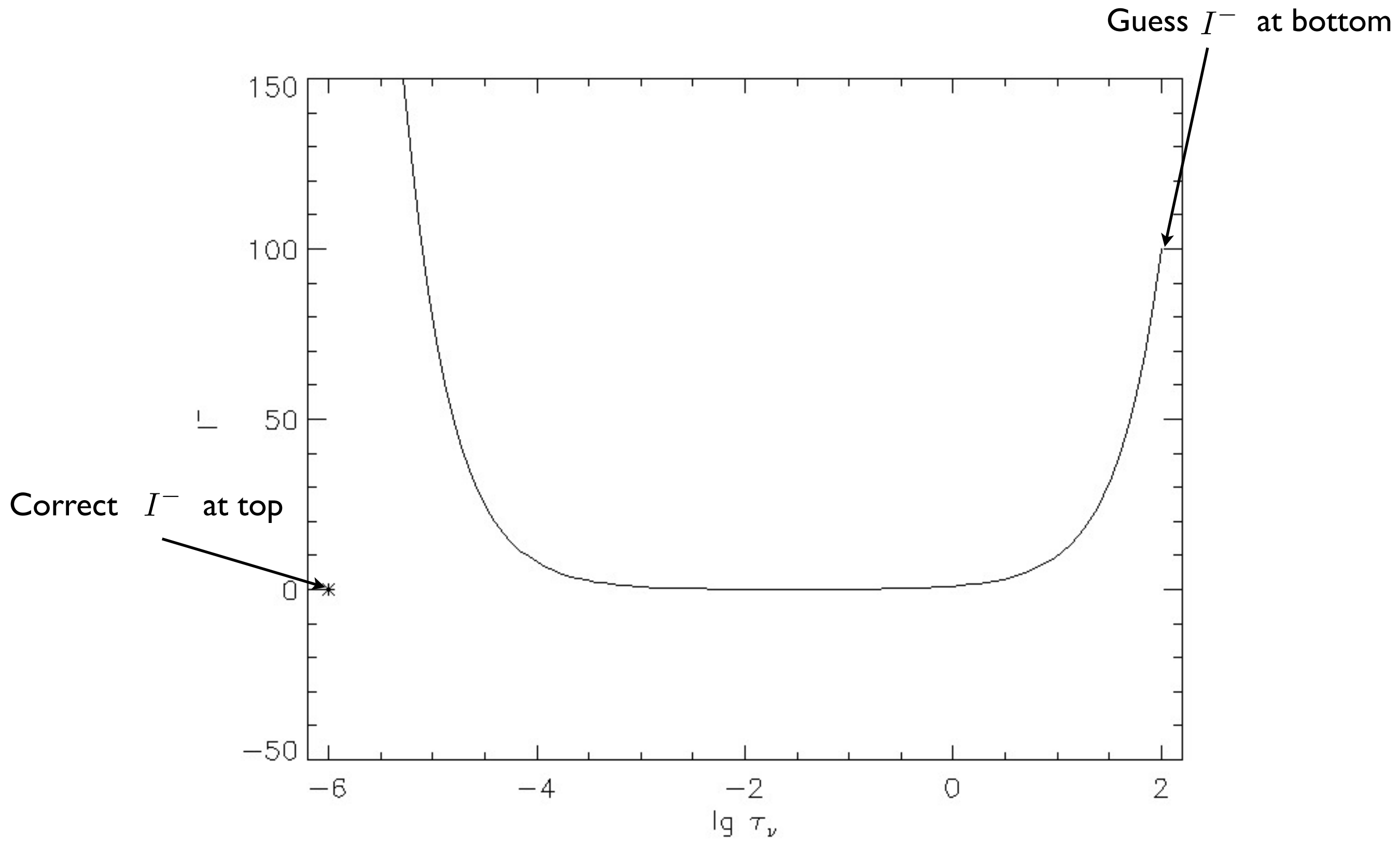
Shooting



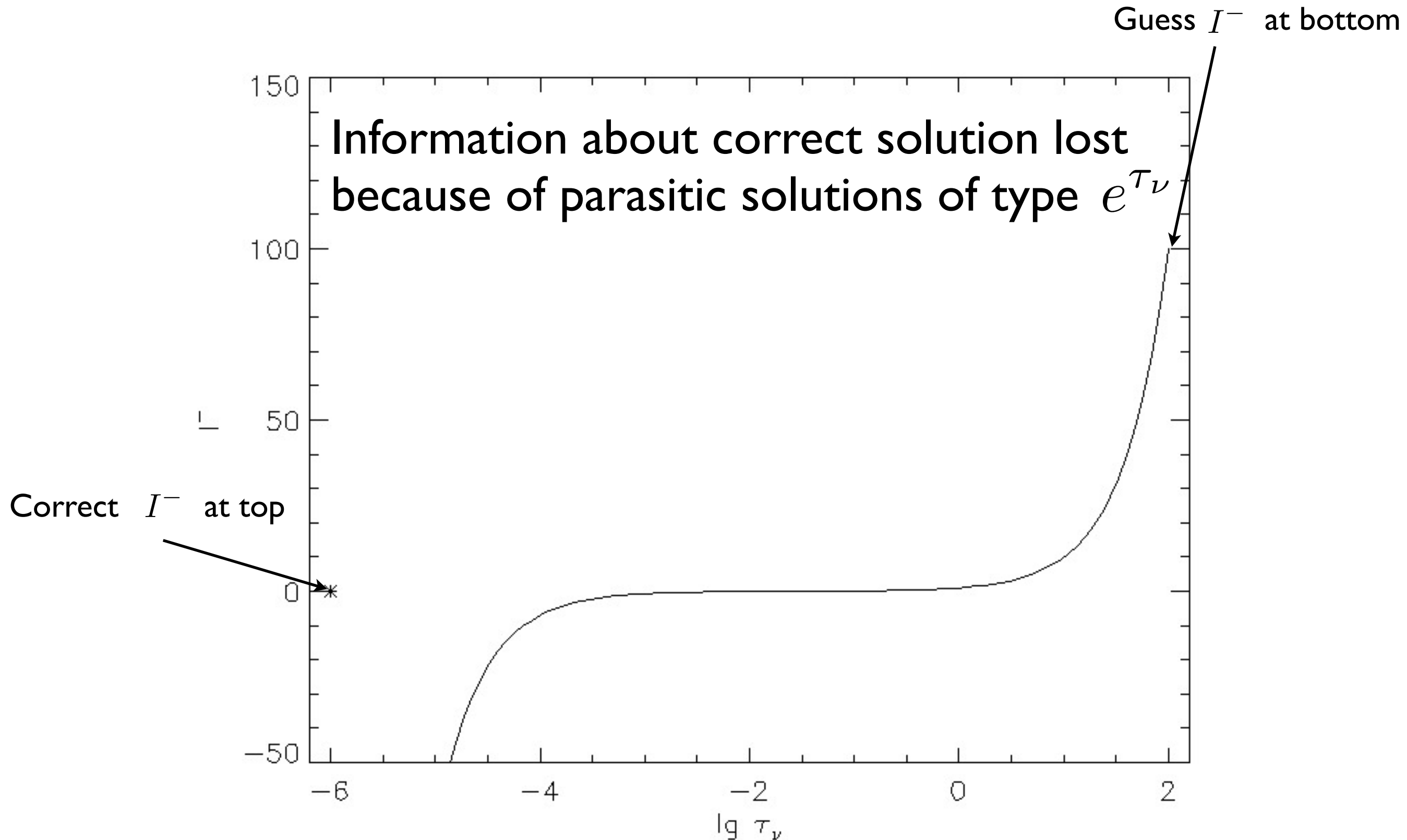
Shooting



Shooting



Shooting



Why is there a problem?

- Boundary condition partially given at one boundary, partially at the other
- Need to solve for whole atmosphere and take into account both boundaries at the same time

Feautrier's method

Feautrier's method

We drop index ν and location τ_ν :

$$\mu \frac{dI_\mu}{d\tau} = I_\mu - S$$

We write separately for outgoing and incoming rays:

$$\mu \frac{dI_\mu^+}{d\tau} = I_\mu^+ - S^+$$

$$-\mu \frac{dI_\mu^-}{d\tau} = I_\mu^- - S^-$$

Multiplying by $\frac{1}{2}$, assuming $S^+ = S^-$
and adding and subtracting we get

$$\mu \frac{d\frac{1}{2}(I_{\mu}^{+} - I_{\mu}^{-})}{d\tau} = \frac{1}{2}(I_{\mu}^{+} + I_{\mu}^{-}) - S^{+}$$

$$\mu \frac{d\frac{1}{2}(I_{\mu}^{+} + I_{\mu}^{-})}{d\tau} = \frac{1}{2}(I_{\mu}^{+} - I_{\mu}^{-})$$

Using the second equation in the first and introducing

$$P \equiv \frac{1}{2}(I_{\mu}^{+} + I_{\mu}^{-}) \quad R \equiv \frac{1}{2}(I_{\mu}^{+} - I_{\mu}^{-})$$

we get

$$\mu^2 \frac{d^2 P}{d\tau^2} = P - S$$

We discretize: $\tau_\nu \longrightarrow \tau_i \quad \mu \longrightarrow \mu_j$

Define differences:

$$[\Delta\tau]_{i+1/2} \approx \tau_{i+1} - \tau_i \equiv \Delta\tau_i \quad (5.20)$$

$$[\Delta\tau]_{i-1/2} \approx \tau_i - \tau_{i-1} \equiv \Delta\tau_{i-1} \quad (5.21)$$

Replace derivatives with differences

$$\begin{aligned} \left[\frac{dP(\tau, \mu_j)}{d\tau} \right]_{i+1/2} &\equiv \lim_{\Delta\tau \rightarrow 0} \frac{[\Delta P(\tau, \mu_j)]_{i+1/2}}{[\Delta\tau]_{i+1/2}} \\ &\approx \frac{P(\tau_{i+1}, \mu_j) - P(\tau_i, \mu_j)}{\tau_{i+1} - \tau_i} = \frac{P_{i+1} - P_i}{\Delta\tau_i}, \end{aligned}$$

2nd derivative replaced by difference between 1st derivatives:

$$\begin{aligned}
\left[\frac{d^2 P(\tau, \mu_j)}{d\tau^2} \right]_i &\approx \frac{[\Delta P(\tau, \mu_j)/\Delta\tau]_{i+1/2} - [\Delta P(\tau, \mu_j)/\Delta\tau]_{i-1/2}}{[\Delta\tau]_i} \\
&\approx \frac{[\Delta P(\tau, \mu_j)/\Delta\tau]_{i+1/2} - [\Delta P(\tau, \mu_j)/\Delta\tau]_{i-1/2}}{\frac{1}{2} \left([\Delta\tau]_{i+1/2} + [\Delta\tau]_{i-1/2} \right)} \\
&\approx \frac{2}{\Delta\tau_{i-1} + \Delta\tau_i} \left[\frac{P_{i+1}}{\Delta\tau_i} - \frac{P_i}{\Delta\tau_i} - \frac{P_i}{\Delta\tau_{i-1}} + \frac{P_{i-1}}{\Delta\tau_{i-1}} \right] \\
&= \frac{2P_{i-1}}{\Delta\tau_{i-1} (\Delta\tau_{i-1} + \Delta\tau_i)} - \frac{2P_i}{\Delta\tau_i \Delta\tau_{i-1}} + \frac{2P_{i+1}}{\Delta\tau_i (\Delta\tau_{i-1} + \Delta\tau_i)}.
\end{aligned}$$

With these (5.17) can be written as:

$$\mu^2 \left[\frac{d^2 P}{d\tau^2} \right]_i - P_i = A_i P_{i-1} - B_i P_i + C_i P_{i+1} = -S_i \quad (5.22)$$

with

$$A_i = \frac{2\mu^2}{\Delta\tau_{i-1} (\Delta\tau_{i-1} + \Delta\tau_i)} \quad (5.23)$$

Numerically unstable for small $\Delta\tau_i$ (use Stein's trick)

$$B_i = 1 + \frac{2\mu^2}{\Delta\tau_i \Delta\tau_{i-1}} \quad (5.24)$$

$$C_i = \frac{2\mu^2}{\Delta\tau_i (\Delta\tau_{i-1} + \Delta\tau_i)}. \quad (5.25)$$

2 level atom with coherent scattering:

$$\mu^2 \frac{d^2 P(\tau, \mu)}{d\tau^2} = P(\tau, \mu) - \varepsilon(\tau) B(\tau) - (1 - \varepsilon(\tau)) J(\tau) \quad (5.27)$$

$$= P(\tau, \mu) - \varepsilon(\tau) B(\tau) - (1 - \varepsilon(\tau)) \sum_{j=1}^m a_j P_j(\tau, \mu_j), \quad (5.28)$$

Source function thus introduces all angles for the equation of a given angle

$$\mathbf{TP} = -\varepsilon \mathbf{B}$$

Structure of matrix:

[illegible]

Solve for all depths at the same time

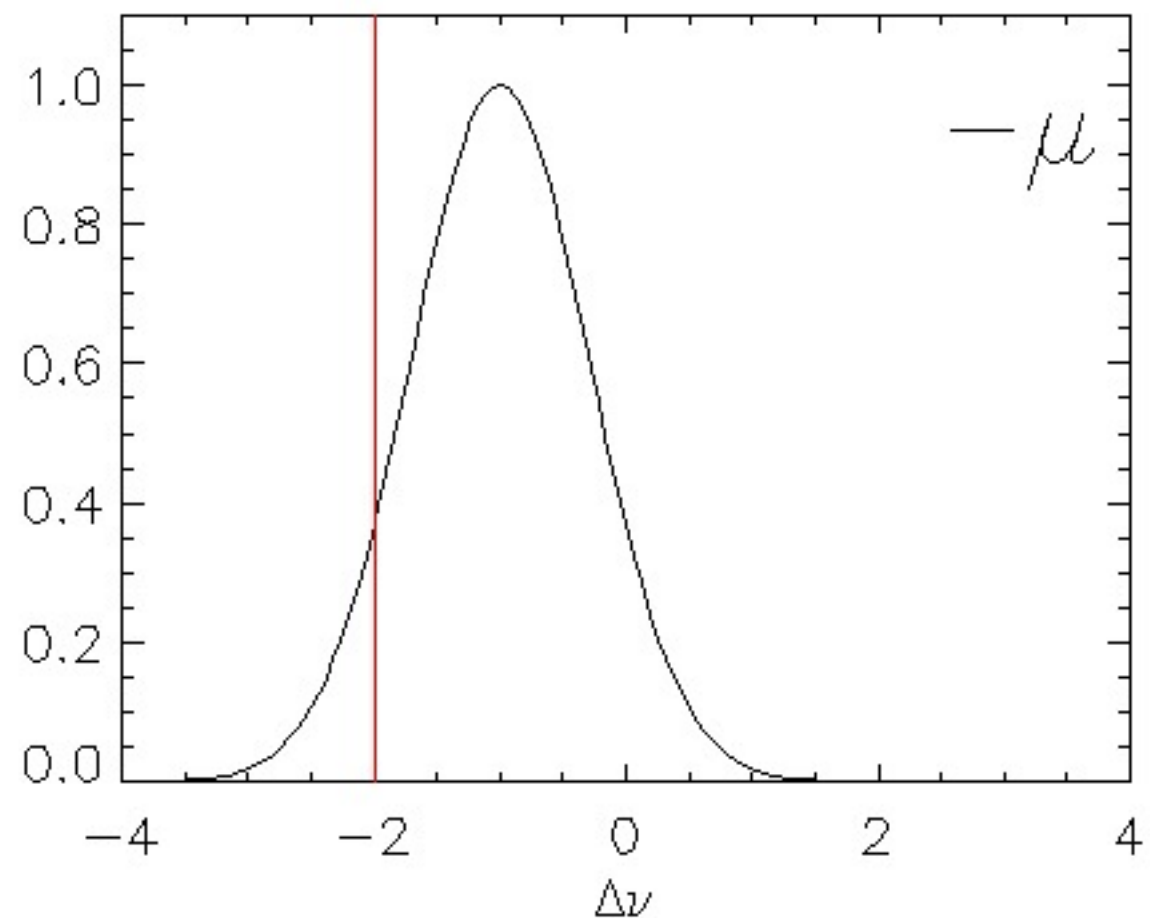
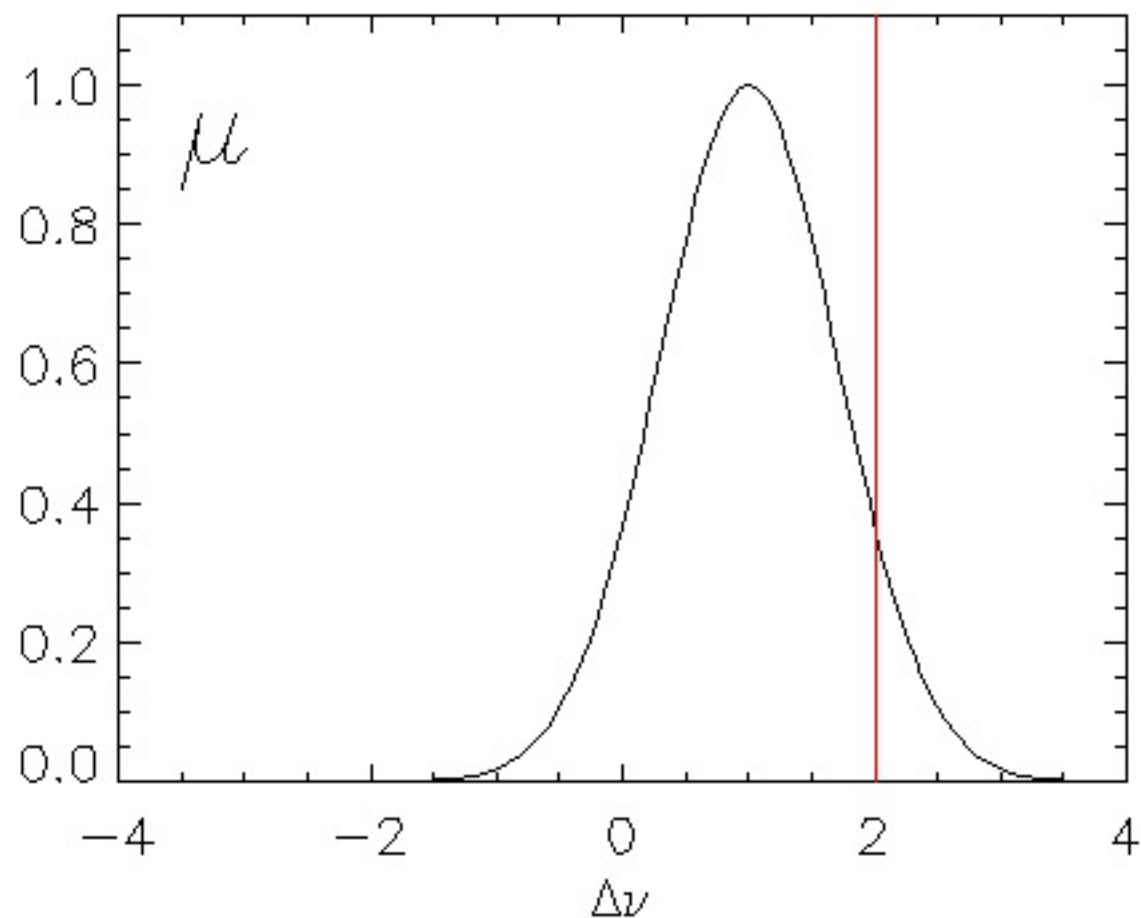
Boundaries at both ends taken into account simultaneously

Note that Feautrier's method assumes
With velocities in the atmosphere this
condition is not fulfilled!!

$$S^+ = S^-$$

If the absorption profile of a line is
symmetric, we can redefine P (and R):

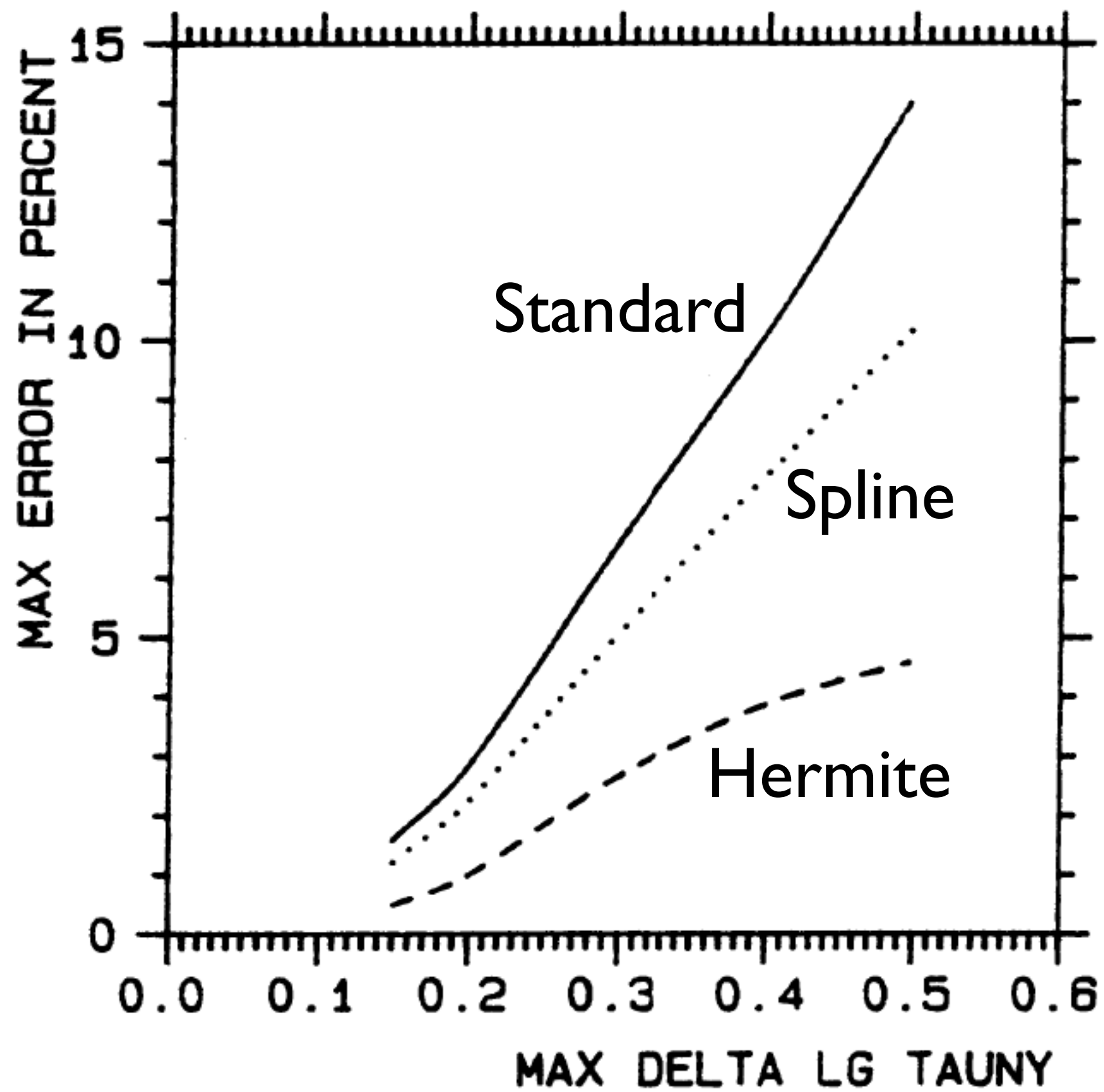
$$P_{\mu}(\tau, \Delta\nu) \equiv \frac{1}{2} (I_{\mu}^{+}(\tau, \Delta\nu) + I_{\mu}^{-}(\tau, -\Delta\nu))$$

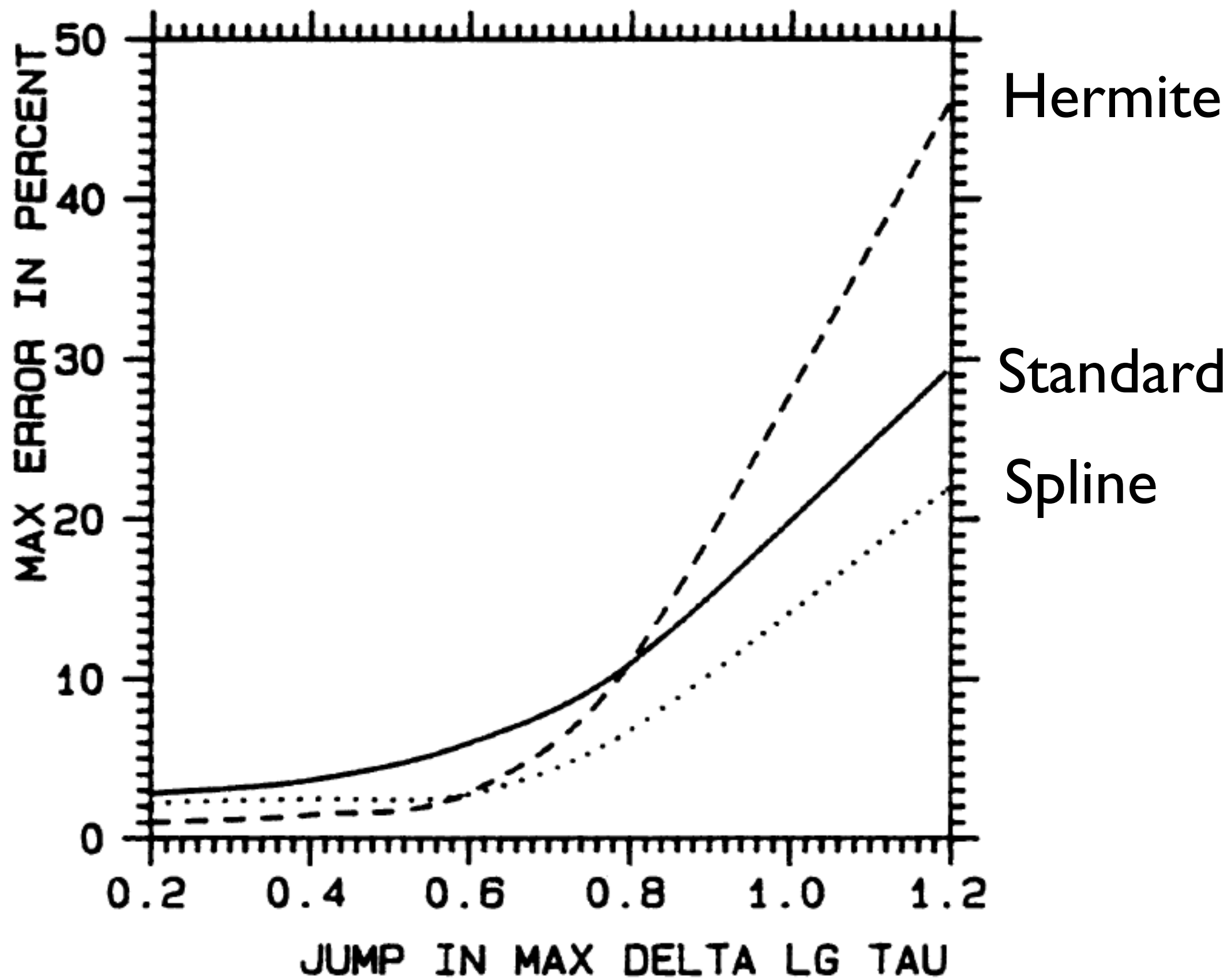


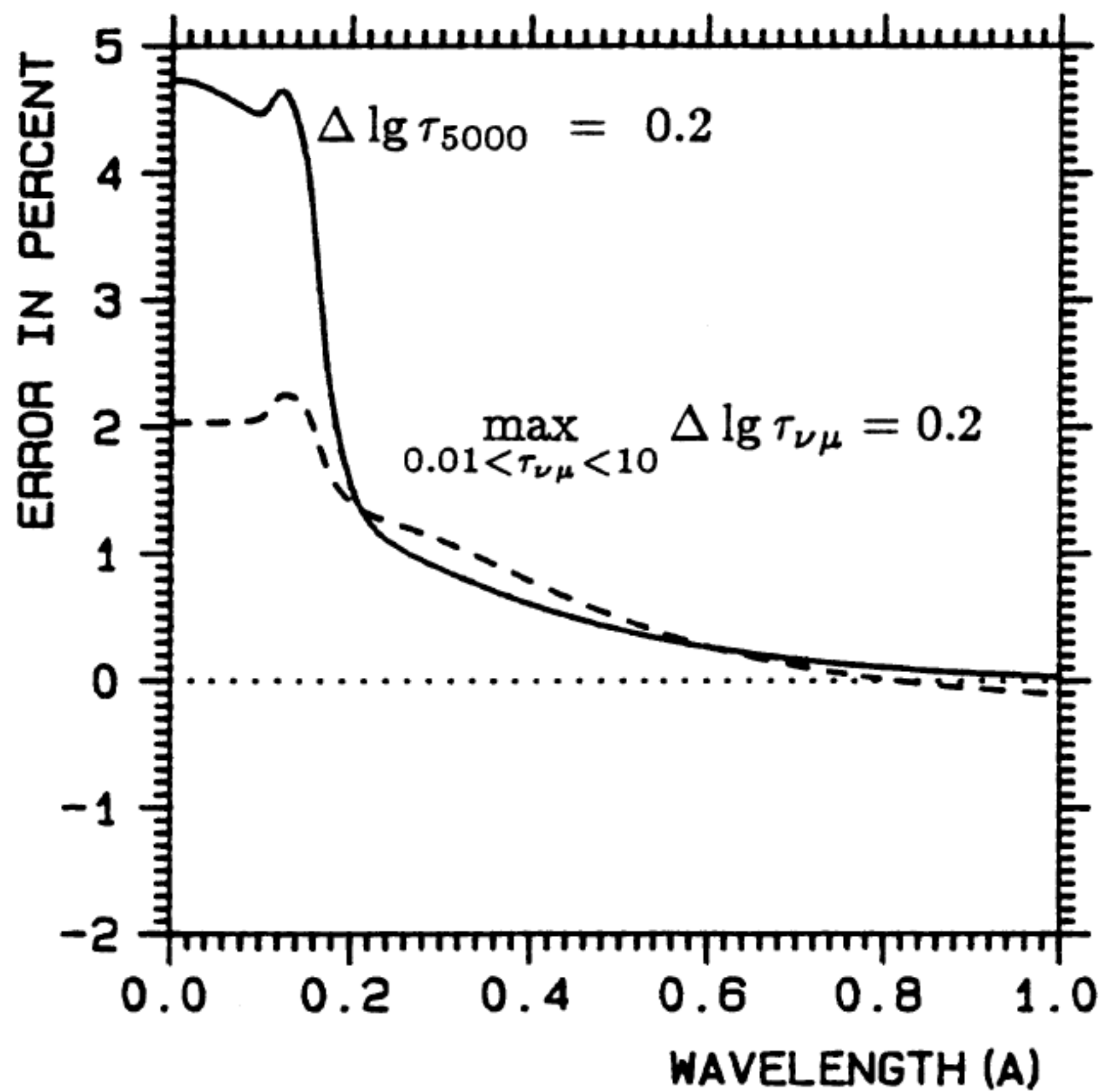
Feautrier's method is fast and accurate (2nd order) and is the method of choice for the formal solution, even when there is no scattering.

There are versions that are 3rd and 4th order accurate (spline and Hermite forms)

Cannot be used if we have both velocity fields and blends!







Velocity fields and blends

Integral methods

- Treat outgoing and incoming rays separately
- Fit source function with a function (e.g. cubic spline)
- Integrate fitting function analytically

ALI

Split the lambda operator into an approximate part and a correction

$$\Lambda_\nu = \Lambda^* + (\Lambda_\nu - \Lambda^*) \quad (5.39)$$

$$J_\nu = \Lambda_\nu^*[S] + (\Lambda_\nu - \Lambda_\nu^*)[S] \quad (5.40)$$

Classical lambda-iteration: $S^{(n+1)} = (1 - \varepsilon) \Lambda[S^{(n)}] + \varepsilon B$, then becomes (5.33)

NB! 

$$S^{(n+1)} = (1 - \varepsilon) \Lambda^*[S^{(n+1)}] + (1 - \varepsilon)(\Lambda_\nu - \Lambda^*)[S^{(n)}] + \varepsilon B \quad (5.41)$$



$$\begin{aligned} S^{(n+1)} - (1 - \varepsilon) \Lambda^*[S^{(n+1)}] &= \boxed{(1 - \varepsilon) \Lambda_\nu[S^{(n)}] + \varepsilon B} - (1 - \varepsilon) \Lambda^*[S^{(n)}] \\ &= \boxed{S^{\text{FS}}} - (1 - \varepsilon) \Lambda^*[S^{(n)}], \end{aligned} \quad (5.42)$$

$$S^{(n+1)} = (1 - (1 - \varepsilon) \Lambda^*)^{-1} [S^{\text{FS}} - (1 - \varepsilon) \Lambda^*[S^{(n)}]]. \quad (5.43)$$

Classical lambda-iteration: $S^{(n+1)} - S^{(n)} = S^{\text{FS}} - S^{(n)}, \quad (5.44)$

Accelerated lambda-iteration:

$$S^{(n+1)} - S^{(n)} = (1 - (1 - \varepsilon) \Lambda^*)^{-1} [S^{\text{FS}} - S^{(n)}]. \quad (5.45)$$

Different choices of approximate lambda operator

Core saturation

Scharmer modified core saturation

Scharmer operator: one point quadrature formula

$$I_\nu(\tau_{\nu\mu}, \mu) \equiv I_{\nu\mu}^\pm = \Lambda_{\nu\mu}^*[S_\nu(\tau_{\nu\mu})] \approx W_{\nu\mu}^\pm(\tau_{\nu\mu}) S_\nu(f_{\nu\mu}^\pm(\tau_{\nu\mu})), \quad (5.52)$$

Use a linear test source function to deduce the W and f

$$\begin{array}{ll} \mu > 0 & \begin{array}{l} W_{\nu\mu}^+ = 1 \\ f_{\nu\mu}^+ = \tau_{\nu\mu} + 1 \end{array} \end{array} \quad \text{=EB} \quad (5.60)$$

$$\begin{array}{ll} \mu < 0 & \begin{array}{l} W_{\nu\mu}^- = 1 - e^{-\tau_{\nu\mu}} \\ f_{\nu\mu}^- = \frac{\tau_{\nu\mu}}{1 - e^{-\tau_{\nu\mu}}} - 1 \end{array} \end{array} \quad (5.62)$$

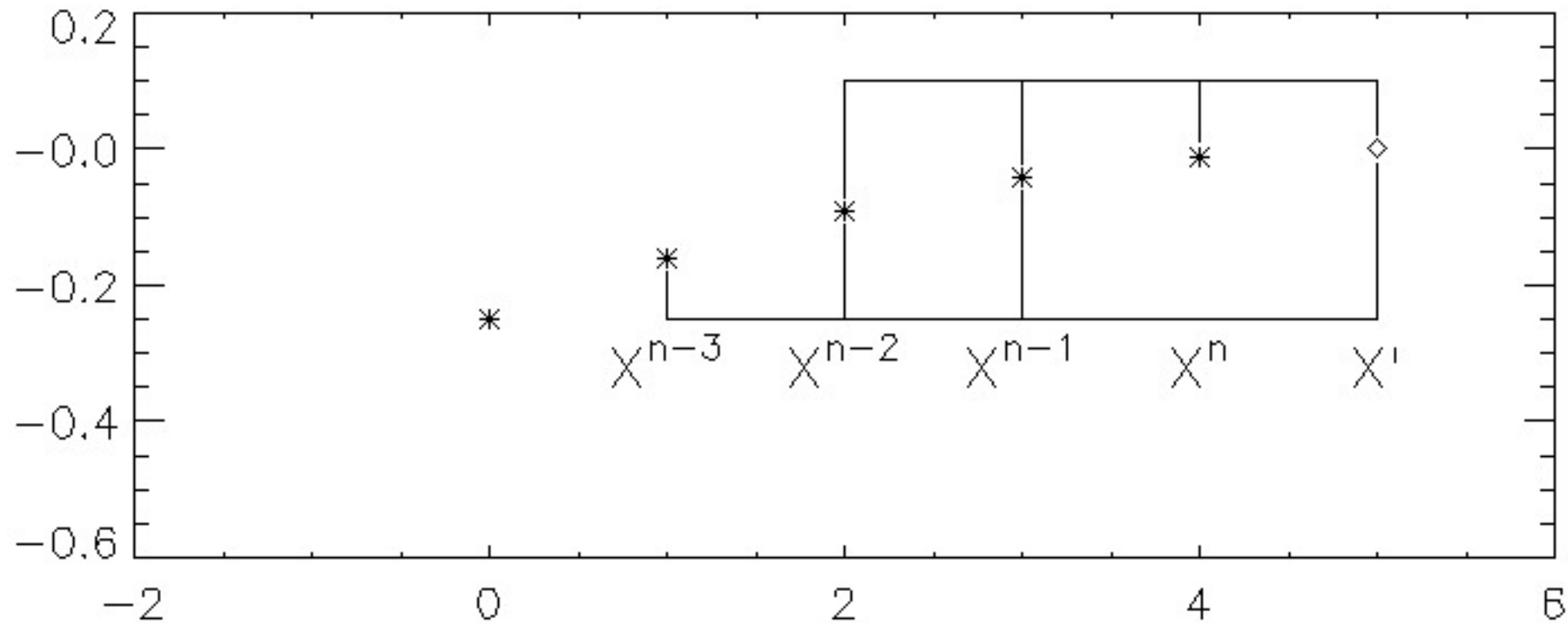
Olson-Auer-Buchler (OAB) operator

The diagonal of the full lambda operator

- Easy to construct (Rybicki-Hummer 1991)
- Easy to “invert” (diagonal matrix)
- Easy to adopt to 3D geometry
- Slow convergence - needs acceleration steps

Convergence acceleration

Ng-acceleration



We use M previous iterations to extrapolate $\mathbf{x}$

$$\mathbf{x} = \left(1 - \sum_{m=1}^M \alpha_m\right) \mathbf{x}^{(n)} + \sum_{m=1}^M \alpha_m \mathbf{x}^{(n-m)}$$

$\downarrow$
 $= \alpha_0$ because $\sum_{m=0}^M \alpha_m = 1$

Same coefficients applied to one iteration back

$$\mathbf{x}' = \left(1 - \sum_{m=1}^M \alpha_m\right) \mathbf{x}^{(n-1)} + \sum_{m=1}^M \alpha_m \mathbf{x}^{(n-m-1)}$$

α_m determined by minimizing distance between vectors $\mathbf{x}$ and $\mathbf{x}'$ with weights w

$$\text{minimize} \quad r^2 = \sum w_d (x_d - x'_d)^2$$

$$\frac{\partial}{\partial \alpha_i} [r^2] = 0, \forall i \quad \text{gives}$$

$$0 = \sum_{d=1}^N w_d (x_d - x'_d) \left(\frac{\partial x_d}{\partial \alpha_i} - \frac{\partial x'_d}{\partial \alpha_i} \right), \forall i$$

$$0 = \sum_{d=1}^N w_d \left[(1 - \sum_{j=1}^M \alpha_j) x_d^{(n)} + \sum_{j=1}^M \alpha_j x_d^{(n-j)} - (1 - \sum_{j=1}^M \alpha_j) x_d^{(n-1)} - \sum_{j=1}^M \alpha_j x_d^{(n-j-1)} \right] \times$$

$$\times \left[-x_d^{(n)} + x_d^{(n-i)} + x_d^{(n-1)} - x_d^{(n-i-1)} \right]$$

introducing

$$\Delta x_d^{(n)} \equiv x_d^{(n)} - x_d^{(n-1)}$$

we get

$$\begin{aligned}
& \sum_{d=1}^N w_d \sum_{j=1}^M \alpha_j (-x_d^{(n)} + x_d^{(n-j)} + x_d^{(n-1)} - x_d^{(n-j-1)}) [\Delta x_d^{(n-i)} - \Delta x_d^{(n)}] = \\
& - \sum_{d=1}^N w_d [x_d^{(n)} - x_d^{(n-1)}] [\Delta x_d^{(n-i)} - \Delta x_d^{(n)}]
\end{aligned}$$

we thus get a matrix equation

$$\mathbf{A}\boldsymbol{\alpha} = \mathbf{b}$$

$$A_{ij} = \sum_{d=1}^N w_d (\Delta x_d^{(n)} - \Delta x_d^{(n-j)}) (\Delta x_d^{(n)} - \Delta x_d^{(n-i)})$$

$$b_i = \sum_{d=1}^N w_d \Delta x_d^{(n)} (\Delta x_d^{(n)} - \Delta x_d^{(n-i)})$$

Linearization

$$x^2 = 2$$

$$(x^{(n)})^2 = 2 + E^{(n)}$$

$$(x^{(n)} + \delta x^{(n)})^2 = 2$$

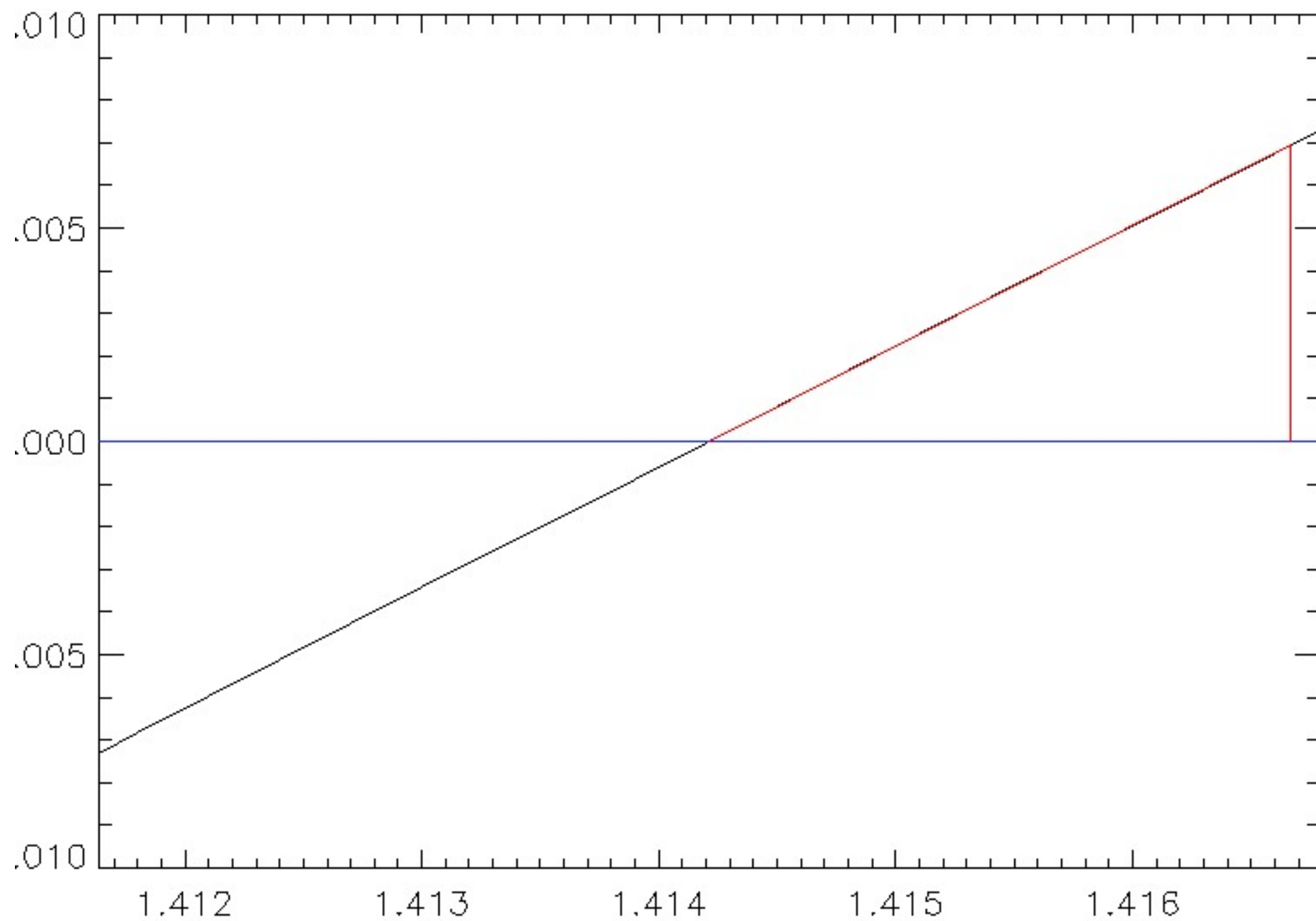
$$(x^{(n)})^2 + 2x^{(n)}\delta x^{(n)} + \cancel{(\delta x^{(n)})^2} = 2$$

$$2x^{(n)}\delta x^{(n)} = -E^{(n)}$$

$$\delta x^{(n)} = \frac{-E^{(n)}}{2x^{(n)}} = \frac{2 - (x^{(n)})^2}{2x^{(n)}}$$

n	$x^{(n)}$	$\lg x - \sqrt{2} $
0	1	-0,4
1	1,5	-1,1
2	1,416	-2,6
3	1,414216	-5,7
4	1,414213562	-11,8

Newton-Raphson



Convergence radius

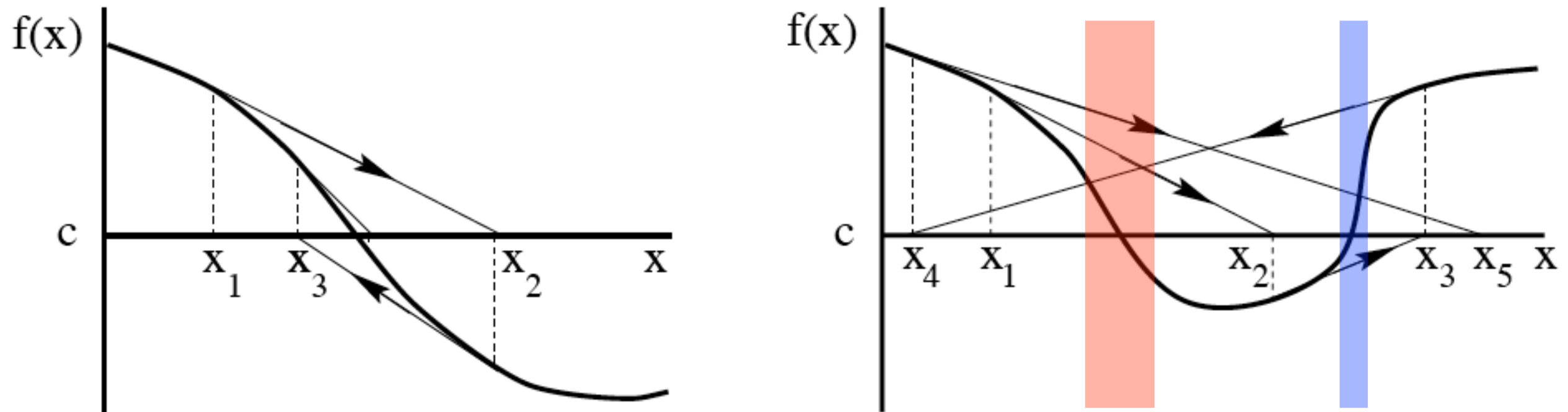
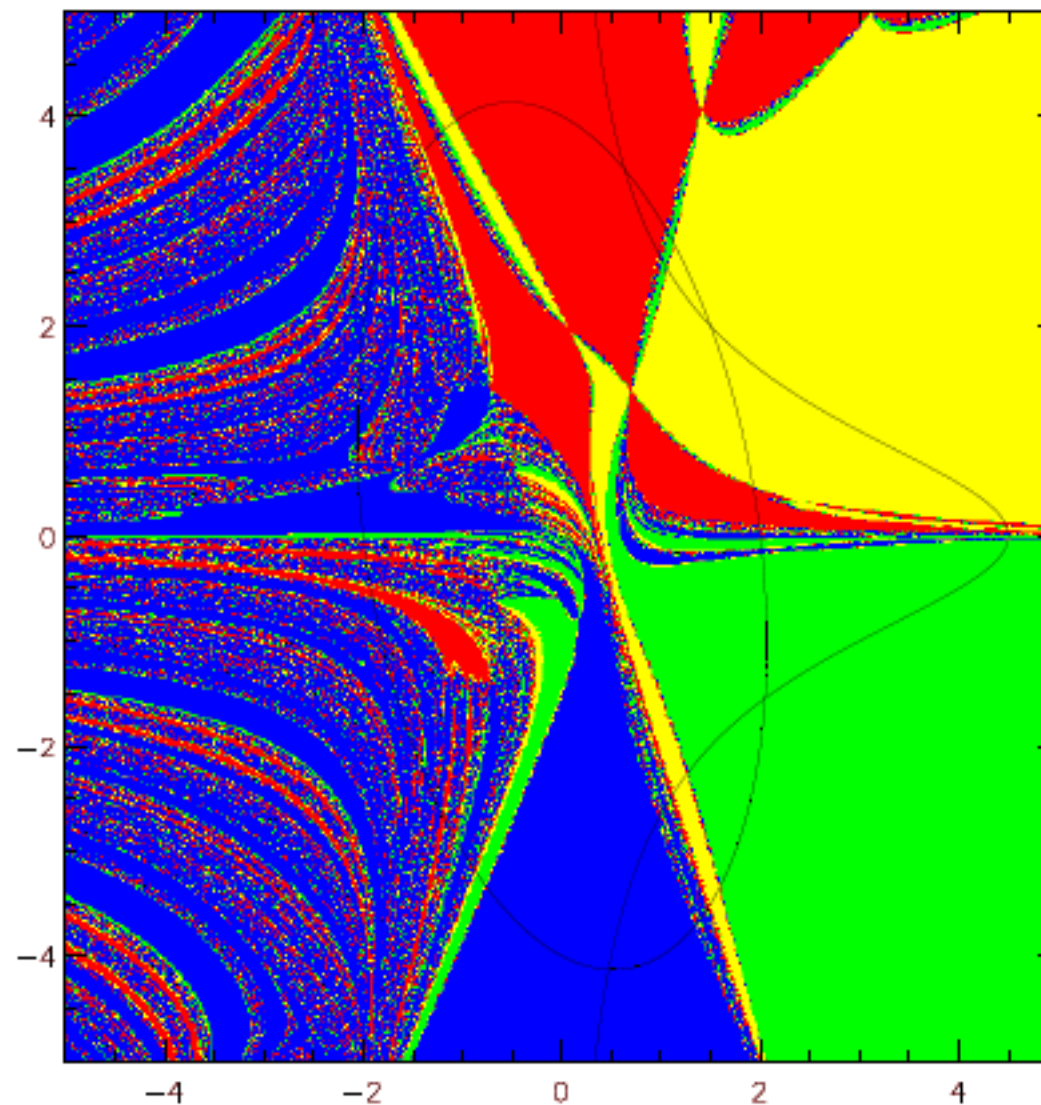


Figure 5.3: Newton-Raphson iteration to find the x for which $f(x) = c$. Find the tangent to $f(x)$ at the first estimate $x = x_1$, find its intersection $x = x_2$ with the constant c , find the tangent to $f(x)$ there, locate its intersection at $x = x_3$, and so on. It works well at left but won't find either solution at right. The convergence region around the solution is small.

Systems of equations

$$\begin{cases} 4x^2 + xy + y^2 - 16 = 0 \\ 2x + xy^2 - 9 = 0 \end{cases}$$

$$\begin{pmatrix} 8x^{(n)} + y^{(n)} & x^{(n)} + 2y^{(n)} \\ 2 + (y^{(n)})^2 & 2x^{(n)}y^{(n)} \end{pmatrix} \begin{pmatrix} \delta x^{(n)} \\ \delta y^{(n)} \end{pmatrix} = \begin{pmatrix} -4(x^{(n)})^2 - x^{(n)}y^{(n)} - (y^{(n)})^2 + 16 \\ -2x^{(n)} - x^{(n)}(y^{(n)})^2 + 9 \end{pmatrix}$$



non-LTE

Transfer equation

The intensity depends on the opacity and the source function. The opacity depends on population densities.

Local Thermodynamic Equilibrium (LTE):

- Source function: Planck function
- Population densities: $f(T, N_e)$ (Saha, Boltzmann)

non-LTE:

Source function and population densities depend on the non-local radiation field

non-LTE

$$\frac{dI}{d\tau} = S - I \quad f(\nu, \mu)$$

$$S_l = \frac{n_j A_{ji} \Psi}{n_i B_{ij} \Phi - n_j B_{ji} \Psi_{se}} \quad f(\nu, \mu)$$

$$\frac{Dn_i}{Dt} = \sum_{j \neq i}^N n_j P_{ji} - n_i \sum_{j \neq i}^N P_{ij}$$

P_{ij} is the probability for a transition from level i to level j

non-LTE (CRD)

$$P_{ij} = R_{ij} + C_{ij}$$

$$R_{ji} = A_{ji} + B_{ji}\bar{J}_{ij}$$

$$R_{ij} = B_{ij}\bar{J}_{ij}$$

with A_{ji} , B_{ij} and B_{ji} the Einstein coefficients for spontaneous emission, absorption and stimulated emission, respectively. All these are given by atomic physics. $\bar{J}_{ij}$ is the absorption profile $(\phi_{\nu\mu})$ weighted integrated mean intensity:

$$\bar{J}_{ij} = \frac{1}{2} \int_{-1}^1 \int_0^{\infty} \phi_{\nu\mu} I_{\nu\mu} d\nu d\mu$$

non-LTE

$$\frac{Dn_i}{Dt} = \sum_{j \neq i}^N n_j P_{ji} - n_i \sum_{j \neq i}^N P_{ij}$$

P_{ij} contains the intensities and thus an integral of the source function over the whole atmosphere. The source function depends on the population densities. We thus have a non-local, non-linear problem to solve.

Statistical equilibrium, particle conservation
and radiative transfer equations are to be
solved together through linearization

(Equation numbers from Uppsala Report 33)

$$n_i \sum_{j \neq i}^{n_l} P_{ij} - \sum_{j \neq i}^{n_l} n_j P_{ji} = 0 \quad (2.1)$$

$$\sum_{j=1}^{n_l} n_j = n_{tot} \quad (2.2)$$

$$\mu \frac{dI_{\nu\mu}}{dz} = -\kappa_{\nu\mu} I_{\nu\mu} + j_{\nu\mu} \quad (2.3)$$

Rates are the sum of radiative and collisional rates

$$P_{ij} = R_{ij} + C_{ij} \quad (2.4)$$

Radiative (bb) and (bf) rates can be written in general form

$$R_{ij} = \begin{cases} \frac{1}{2} \int_{-1}^1 \int_0^\infty \frac{4\pi}{h\nu} \alpha_{ji} G_{ji} (I_{\nu\mu} + \frac{2h\nu^3}{c^2}) d\nu d\mu & \text{if } i > j \\ \frac{1}{2} \int_{-1}^1 \int_0^\infty \frac{4\pi}{h\nu} \alpha_{ij} I_{\nu\mu} d\nu d\mu & \text{if } i < j \end{cases} \quad (2.5)$$

$$\alpha_{ij} = \begin{cases} B_{ij} \frac{h\nu_{ij}}{4\pi} \phi_{\nu\mu} & \text{(b-b);} \\ \alpha_c(\nu) & \text{(b-f).} \end{cases} \quad (2.6)$$

$$G_{ij} = \begin{cases} g_i/g_j & \text{(b-b);} \\ \frac{n_i^*}{n_j^*} e^{\frac{-h\nu}{kT}} & \text{(b-f).} \end{cases} \quad (2.7)$$

For bb transitions this simplifies to the familiar form:

$$R_{ij} = \begin{cases} A_{ij} + B_{ij} \bar{J}_{ij}, & \text{if } i > j; \\ B_{ij} \bar{J}_{ij}, & \text{if } i < j. \end{cases} \quad (2.8)$$

$$\bar{J}_{ij} = \frac{1}{2} \int_{-1}^1 \int_0^{\infty} \phi_{\nu\mu} I_{\nu\mu} d\nu d\mu \quad (2.9)$$

$$\frac{1}{2} \int_{-1}^1 \int_0^{\infty} \phi_{\nu\mu} d\nu d\mu = 1$$

Opacity and emissivity in general form:

Background (continuum) contribution

$$\kappa_{\nu\mu} = \kappa_{\nu c} + \alpha_{ij}(\nu, \mu)(n_i - G_{ij}n_j) \quad (2.10)$$

$$j_{\nu\mu} = j_{\nu c} + \frac{2h\nu^3}{c^2} G_{ij} \alpha_{ij}(\nu, \mu) n_j \quad (2.11)$$

$$S_{\nu\mu} = j_{\nu\mu} / \kappa_{\nu\mu} \quad (2.12)$$

(Equation numbers from Scharmer & Carlsson 1981)

$$n_i^{(n)} \sum_{j \neq i}^{n_l} P_{ij}^{(n)} - \sum_{j \neq i}^{n_l} n_j^{(n)} P_{ji}^{(n)} = E_i^{(n)} \quad (3.1)$$

$$n_i^{(n+1)} = n_i^{(n)} + \delta n_i^{(n)} \quad (3.2)$$

$$P_{ij}^{(n+1)} = P_{ij}^{(n)} + \delta P_{ij}^{(n)} \quad (3.3)$$

$$n_i^{(n+1)} \sum_{j \neq i}^{n_l} P_{ij}^{(n+1)} - \sum_{j \neq i}^{n_l} n_j^{(n+1)} P_{ji}^{(n+1)} = 0 \quad (3.4)$$

We insert 3.2 and 3.3 in 3.4, subtract 3.1 and neglect non-linear terms

$$\begin{aligned} \delta n_i^{(n)} \sum_{j \neq i}^{n_l} P_{ij}^{(n)} + n_i^{(n)} \sum_{j \neq i}^{n_l} \delta P_{ij}^{(n)} - \sum_{j \neq i}^{n_l} \delta n_j^{(n)} P_{ji}^{(n)} \quad (3.5) \\ - \sum_{j \neq i}^{n_l} n_j^{(n)} \delta P_{ji}^{(n)} = -E_i^{(n)} \end{aligned}$$

$$\delta P_{ij}^{(n)} = B_{ij} \delta \bar{J}_{ij}^{(n)} = B_{ij} \frac{1}{2} \int_{-1}^1 \int_0^\infty \phi_{\nu\mu} \delta I_{\nu\mu}^{(n)} d\nu d\mu \quad (3.6)$$

We need to express $\delta I_{\nu\mu}^{(n)}$ in terms of $\delta n_i^{(n)}$ and $\delta n_j^{(n)}$

We use the transfer equation:

$$\mu \frac{dI_{\nu\mu}^{(n)}}{dz} = -\kappa_{\nu\mu}^{(n)} I_{\nu\mu}^{(n)} + j_{\nu\mu}^{(n)} \quad (3.7)$$

$$\mu \frac{d}{dz} \delta I_{\nu\mu}^{(n)} = -\kappa_{\nu\mu}^{(n)} \delta I_{\nu\mu}^{(n)} - I_{\nu\mu}^{(n)} \delta \kappa_{\nu\mu}^{(n)} + \delta j_{\nu\mu}^{(n)} \quad (3.8)$$

Usual definition of optical depth along a ray

$$d\tau_{\nu\mu}^{(n)} = -\kappa_{\nu\mu}^{(n)} dz / \mu \quad (3.9)$$

We *define* an equivalent source function perturbation:

$$\delta S_{\nu\mu}^{(n)} = \delta j_{\nu\mu}^{(n)} / \kappa_{\nu\mu}^{(n)} - I_{\nu\mu}^{(n)} \delta \kappa_{\nu\mu}^{(n)} / \kappa_{\nu\mu}^{(n)} \quad (3.10)$$

This gives the usual transfer equation, now for the perturbations

$$\frac{d}{d\tau_{\nu\mu}^{(n)}} \delta I_{\nu\mu}^{(n)} = \delta I_{\nu\mu}^{(n)} - \delta S_{\nu\mu}^{(n)} \quad (3.11)$$

$$\kappa_{\nu\mu} = \kappa_{\nu c} + \alpha_{ij}(\nu, \mu)(n_i - G_{ij}n_j) \quad (2.10)$$

$$j_{\nu\mu} = j_{\nu c} + \frac{2h\nu^3}{c^2} G_{ij} \alpha_{ij}(\nu, \mu) n_j \quad (2.11)$$

$$\delta S_{\nu\mu}^{(n)} = \delta j_{\nu\mu}^{(n)} / \kappa_{\nu\mu}^{(n)} - I_{\nu\mu}^{(n)} \delta \kappa_{\nu\mu}^{(n)} / \kappa_{\nu\mu}^{(n)} \quad (3.10)$$

Gives

$$\delta S_{\nu\mu}^{(n)} = c_l^{(n)} \delta n_i^{(n)} + c_u^{(n)} \delta n_j^{(n)} \quad (3.13)$$

$$c_l^{(n)} = -\alpha_{ij}(\nu, \mu) I_{\nu\mu}^{(n)} / \kappa_{\nu\mu}^{(n)} \quad (3.14)$$

$$c_u^{(n)} = G_{ij} \alpha_{ij}(\nu, \mu) \left(\frac{2h\nu^3}{c^2} + I_{\nu\mu}^{(n)} \right) / \kappa_{\nu\mu}^{(n)} \quad (3.15)$$

We have thus expressed $\delta S_{\nu\mu}^{(n)}$ in $\delta n_i^{(n)}$ and $\delta n_j^{(n)}$

$$\delta I_{\nu\mu}^{(n)} = \Lambda_{\nu\mu}^{(n)} [\delta S_{\nu\mu}^{(n)}] \quad (3.12)$$

completes the task of expressing

$\delta I_{\nu\mu}^{(n)}$ in terms of $\delta n_i^{(n)}$ and $\delta n_j^{(n)}$

We now have a non-local but linear system of equations for the unknowns $\delta \mathbf{n}$

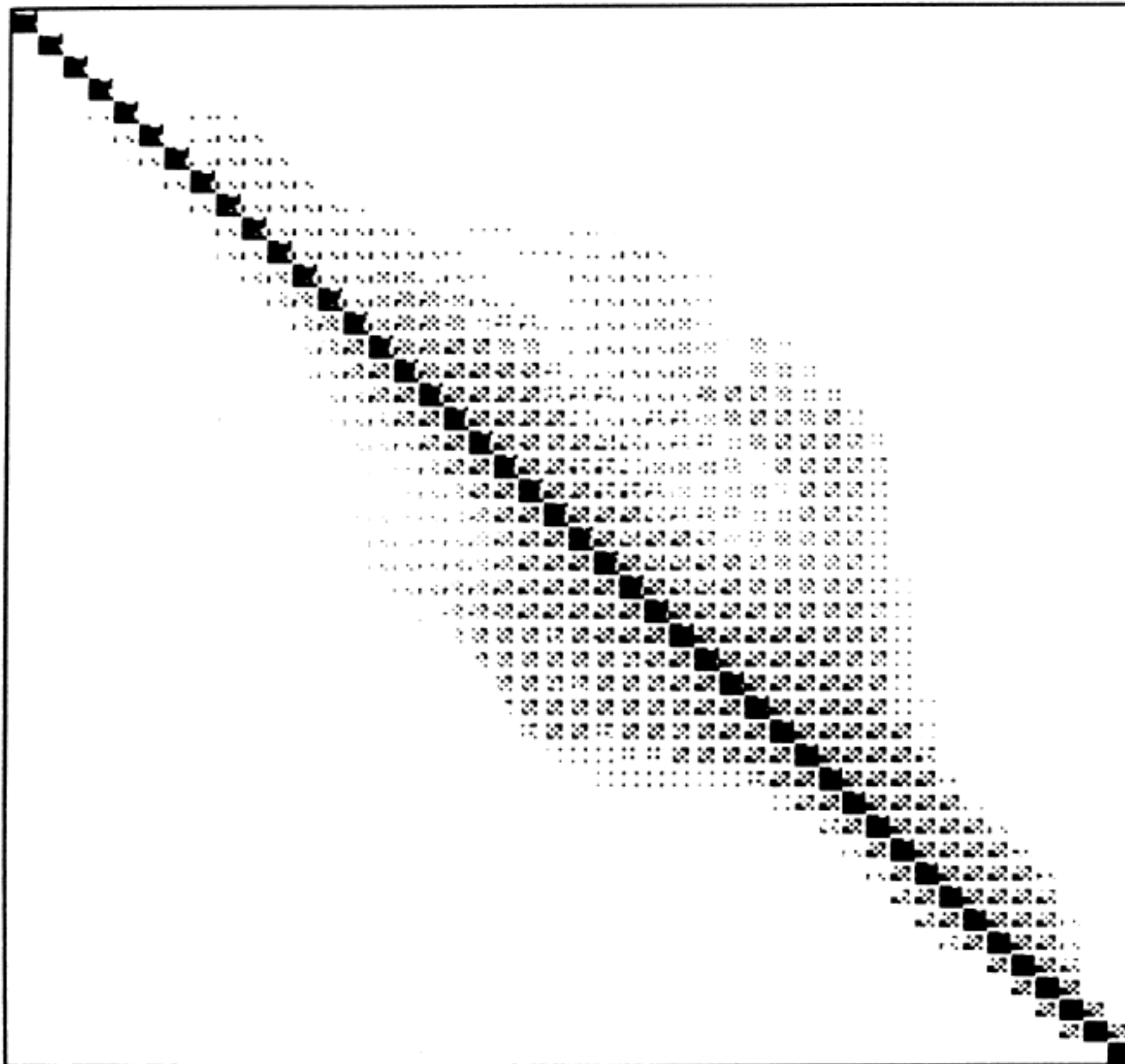
For $\Lambda_{\nu\mu}^{(n)}$ we may choose

Exact operator: slow to construct, slow to invert

Scharmer's operator: faster and global

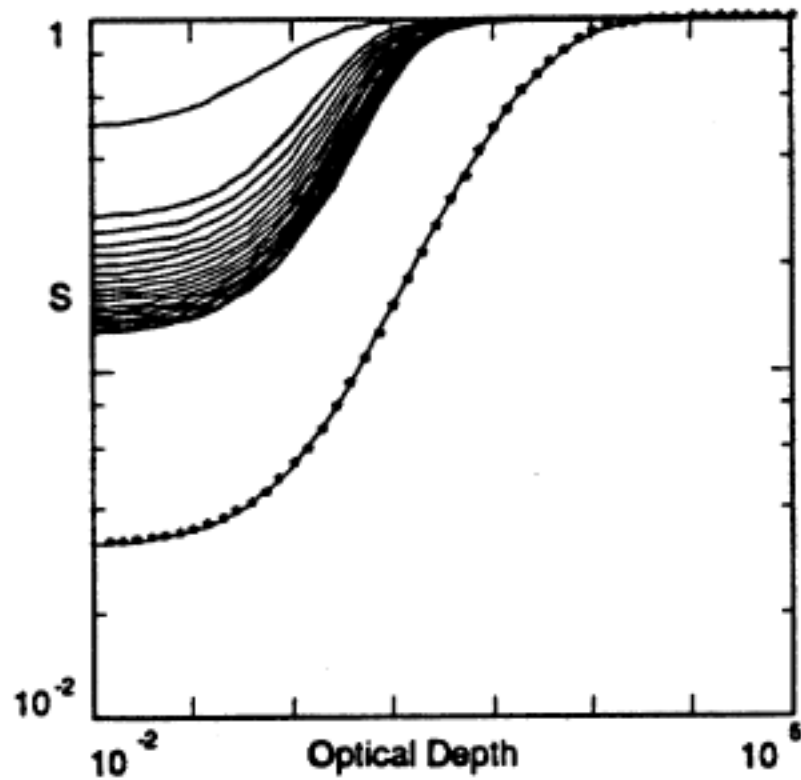
Local operator (OAB): fast to construct, invert, but slow convergence.

Coefficient matrix for Scharmer operator

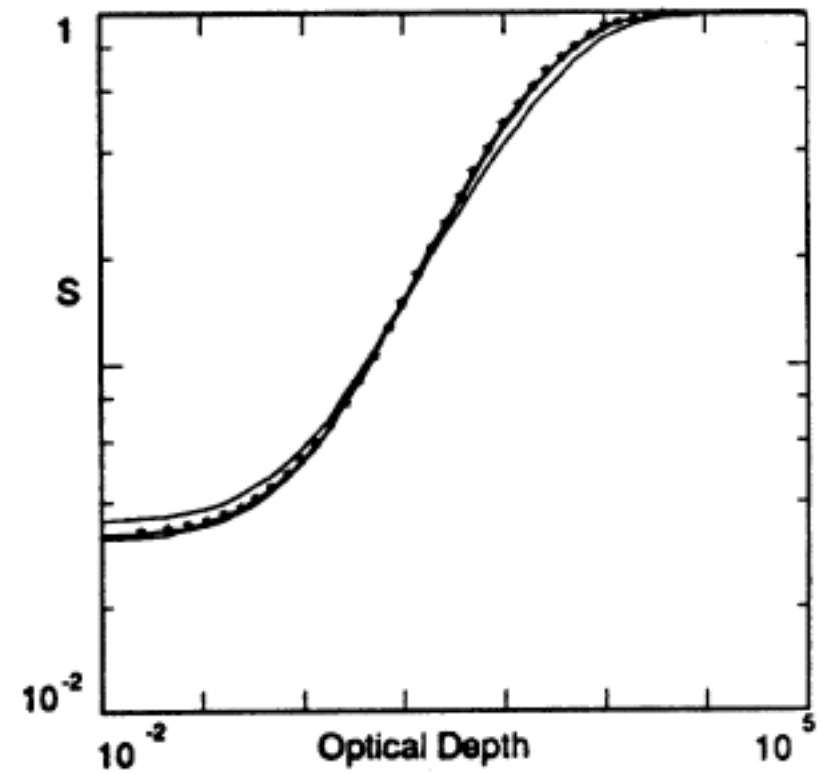


Convergence properties

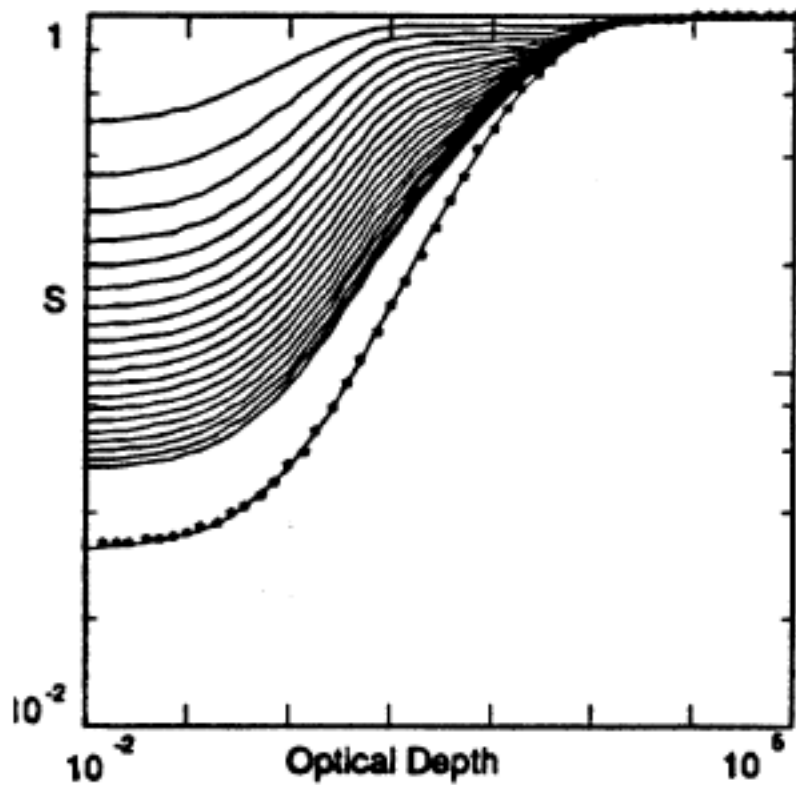
Lambda iteration



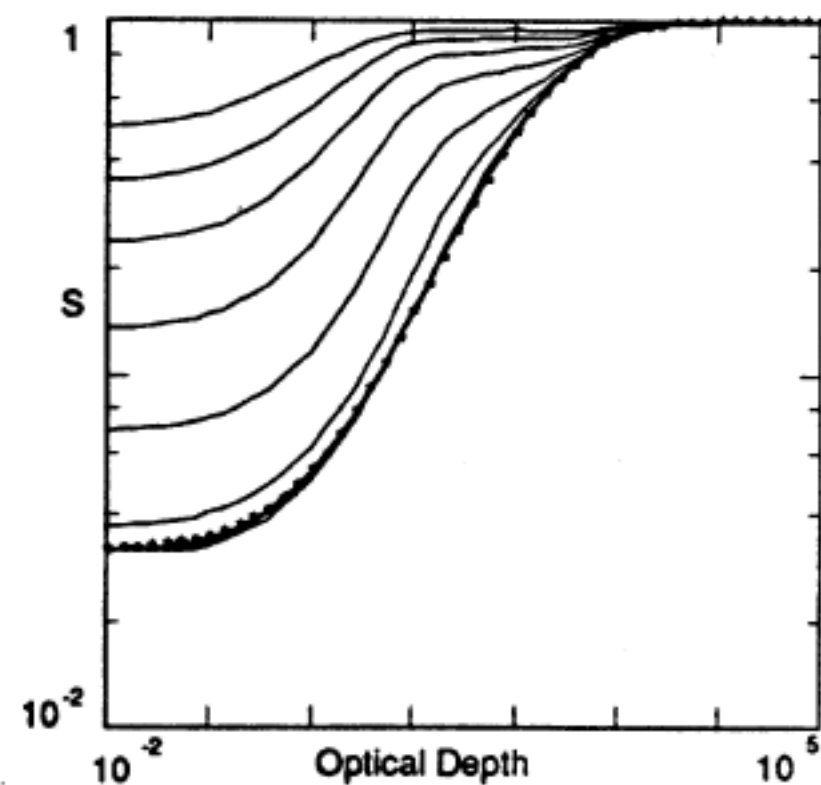
Scharmer operator



Local operator



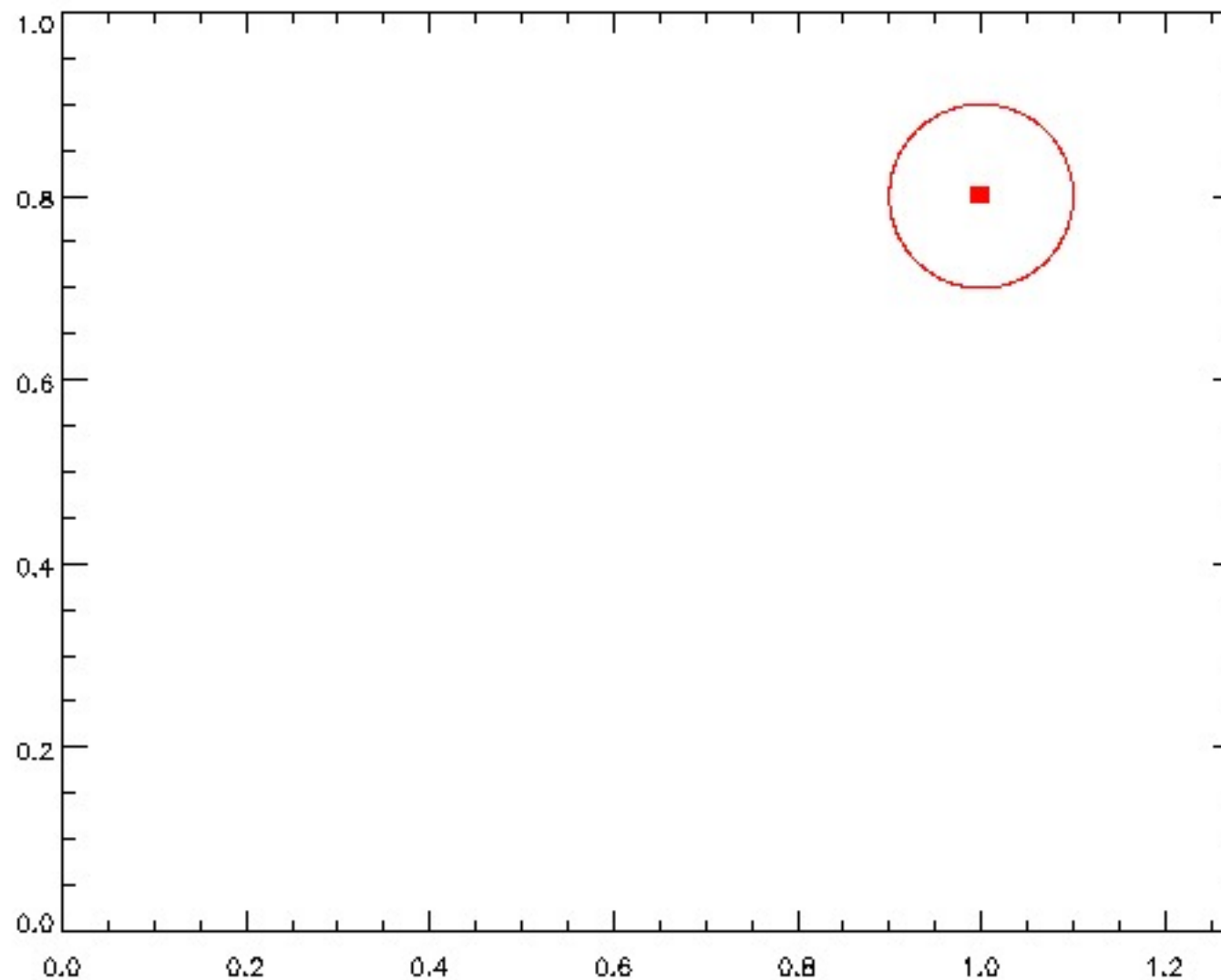
Local + acceleration



CRSW

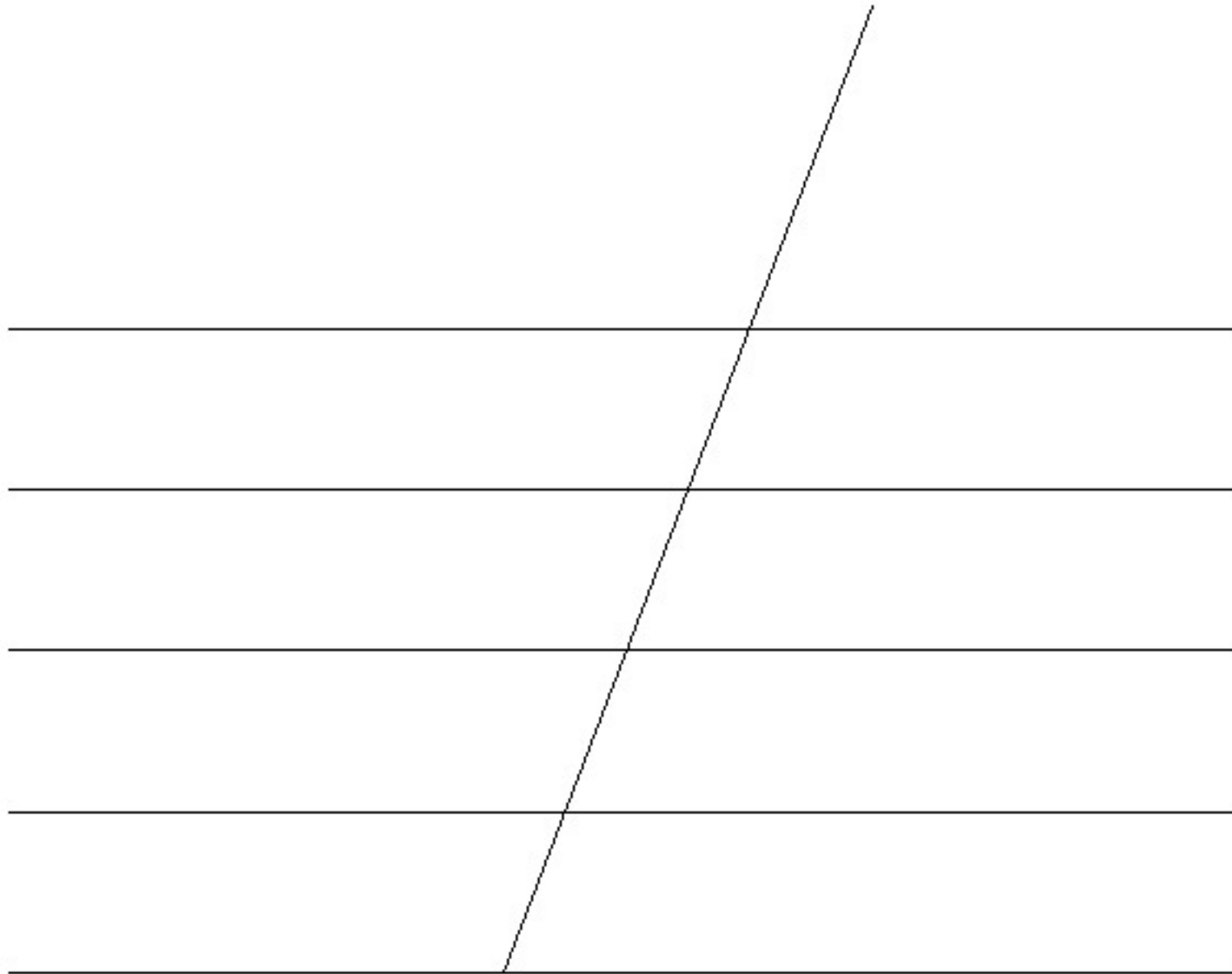
Collisional-Radiative Switching

Multiply collisional rates with a factor that is changed from iteration to iteration

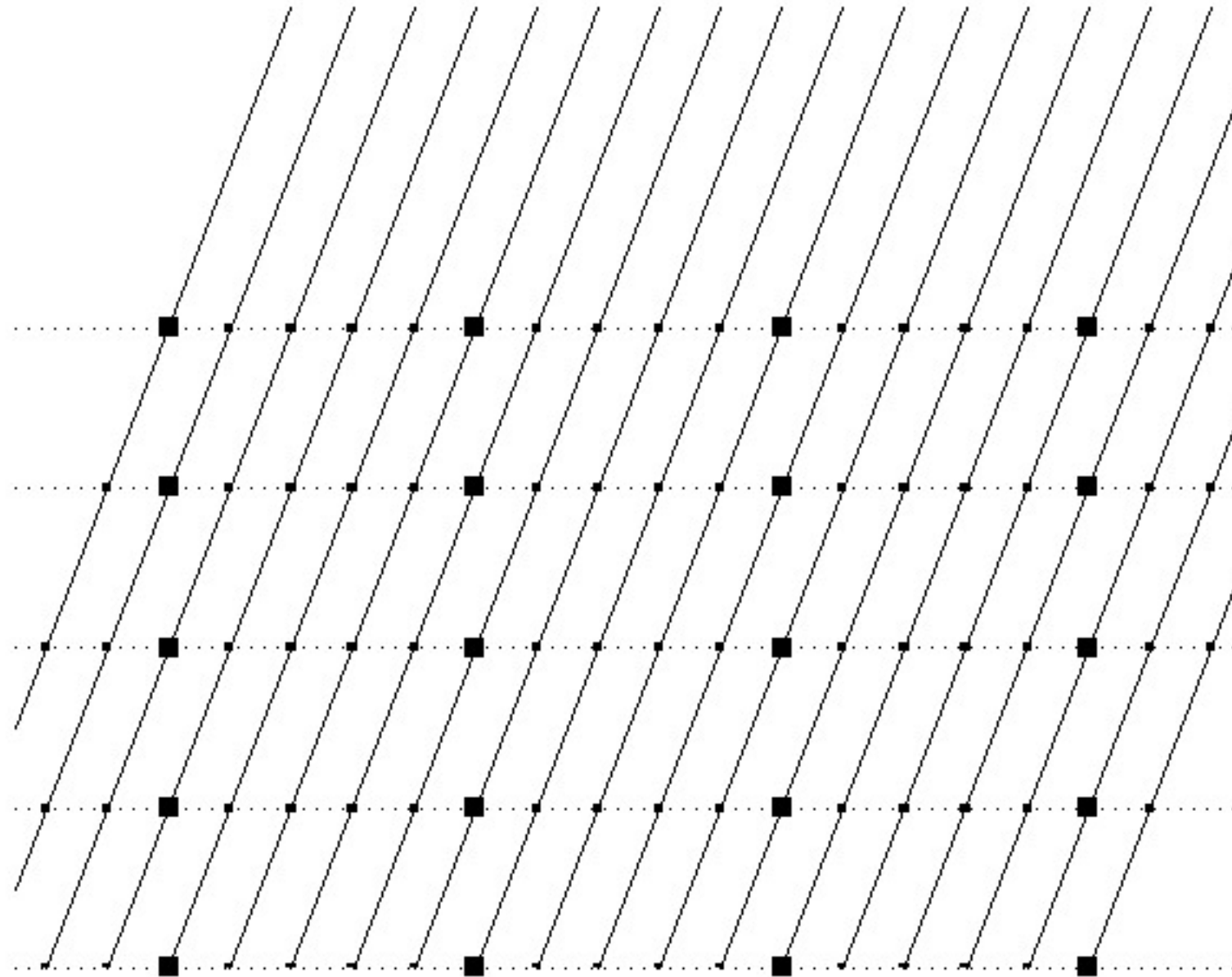


2D-3D

In 1D all rays pass through all grid “points” (planes).

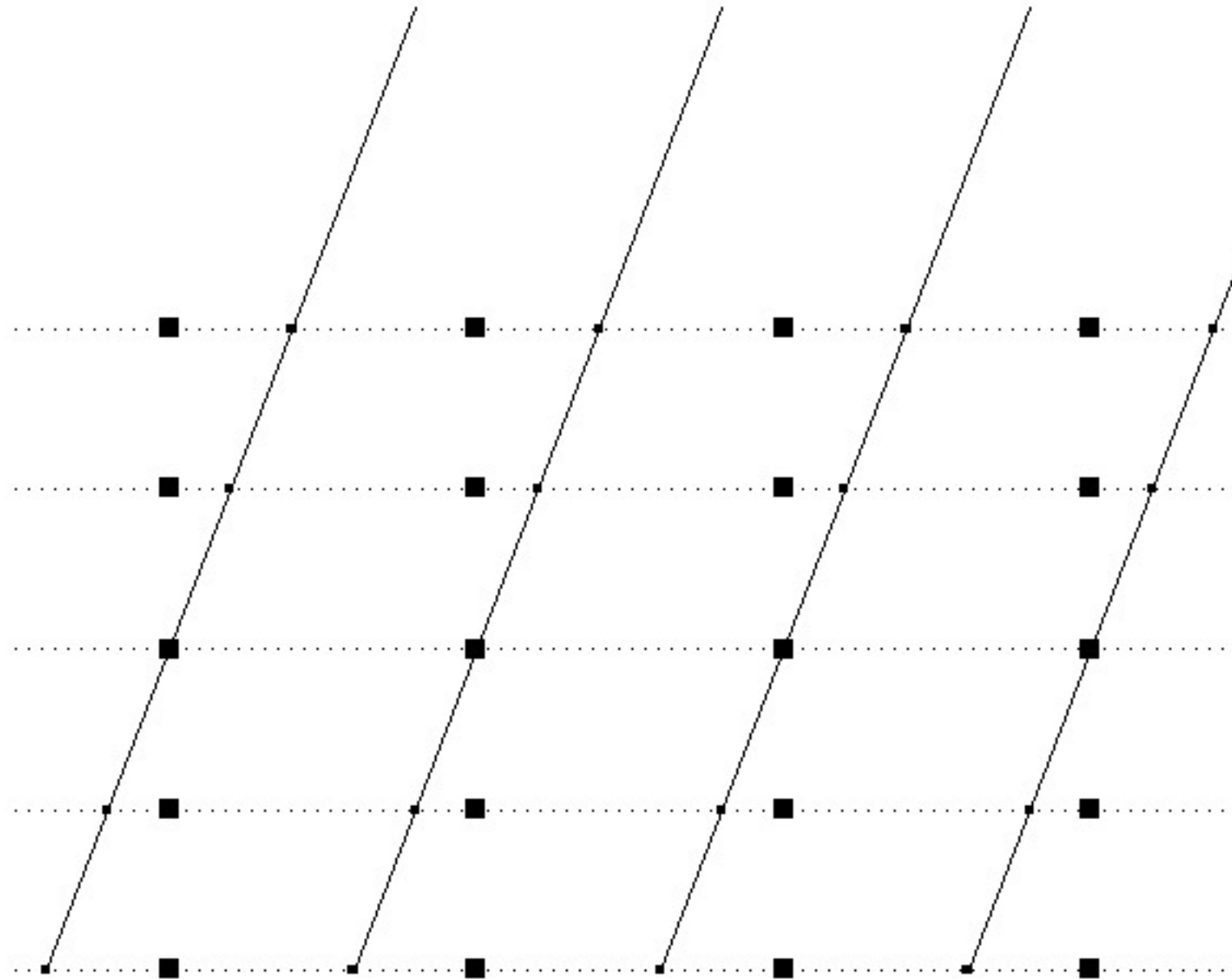


Long characteristics through all grid-points



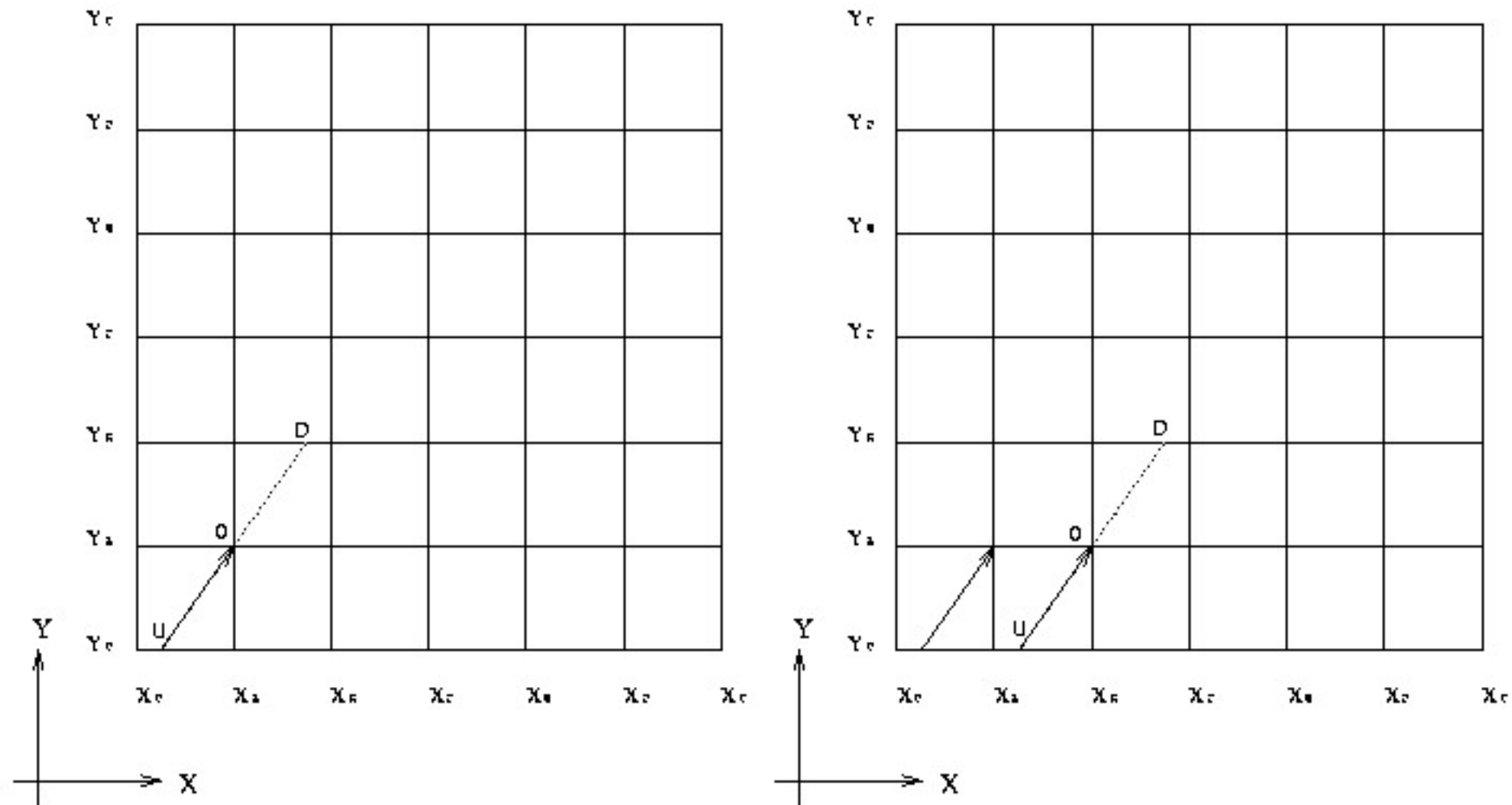
Many rays: slow

Long characteristics through one plane



Fast but may miss localized sources

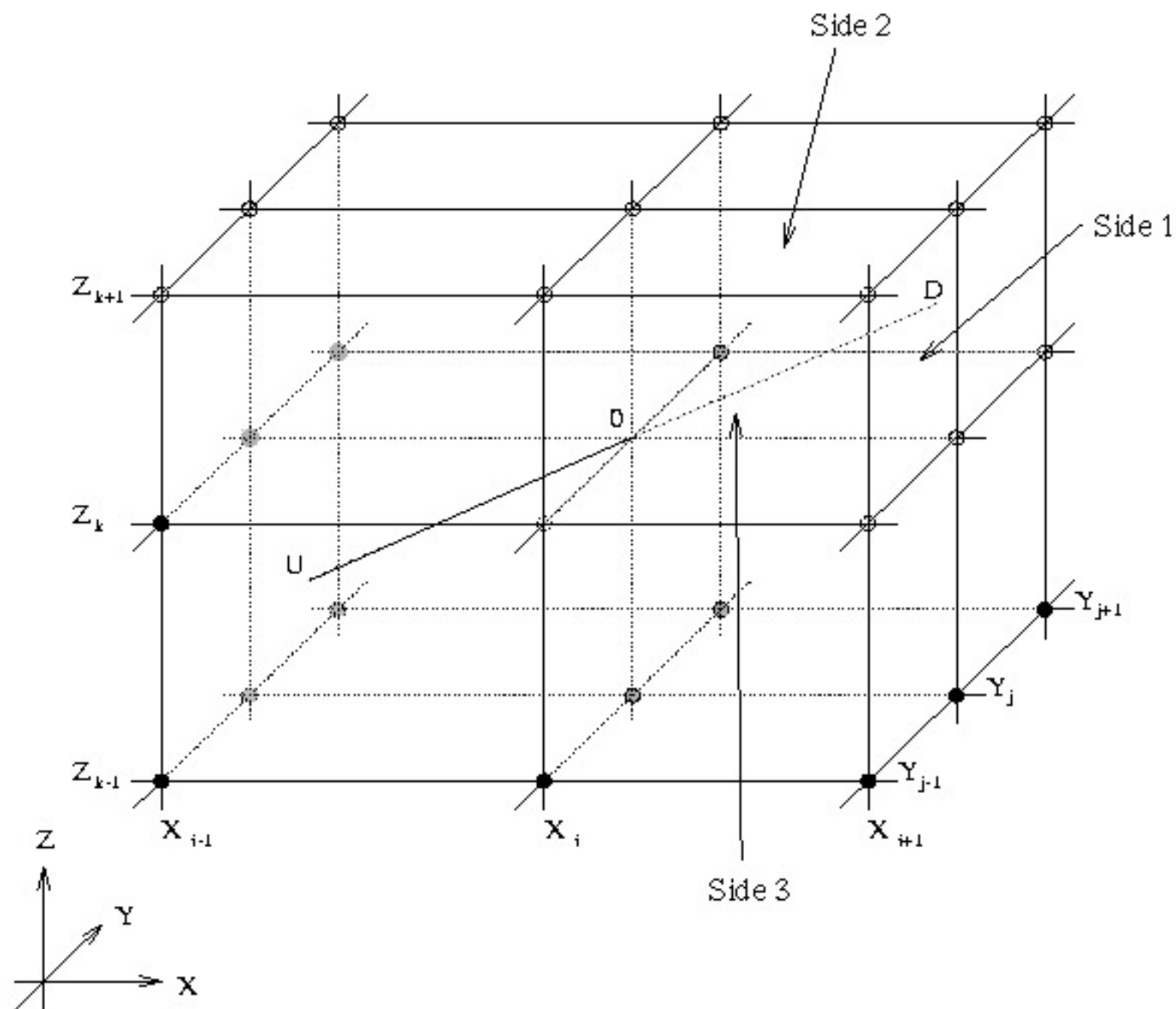
Short characteristics



Approximate S through 3 points (U, O, D),
integrate analytically

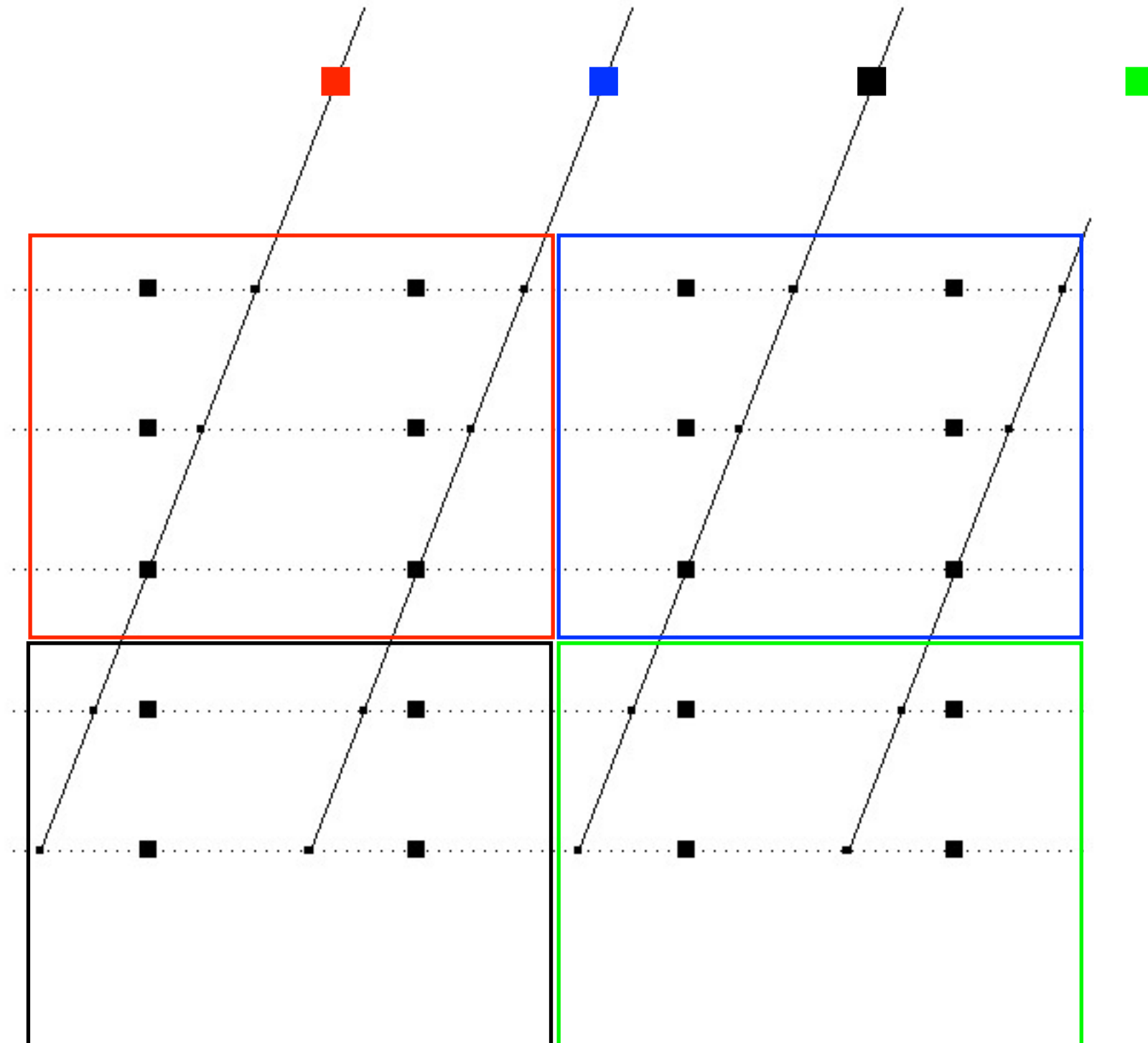
Diffusive

Short characteristics in 3D



Parallelization strategies

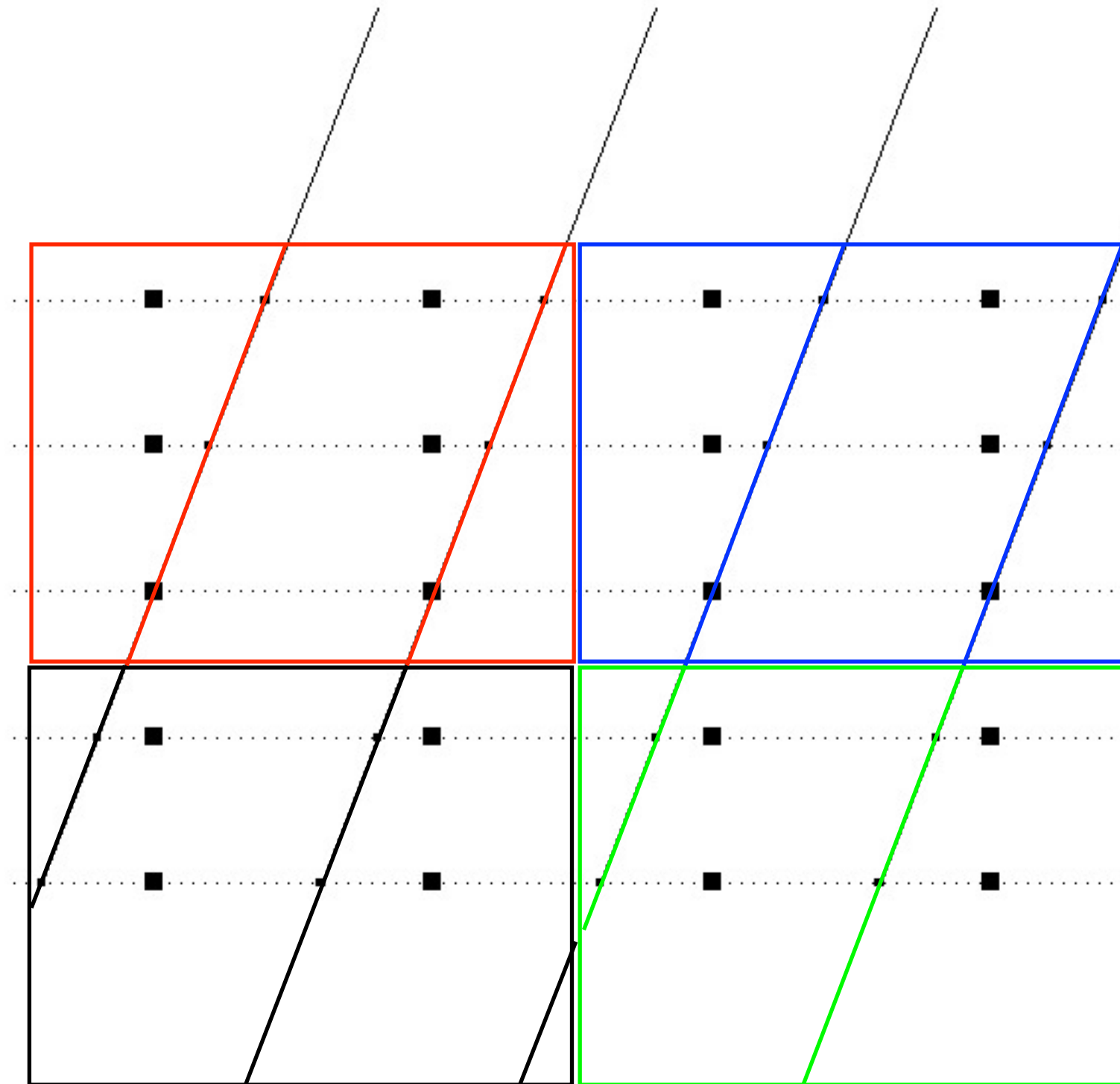
over rays: SMP OK



MPI: massive communication

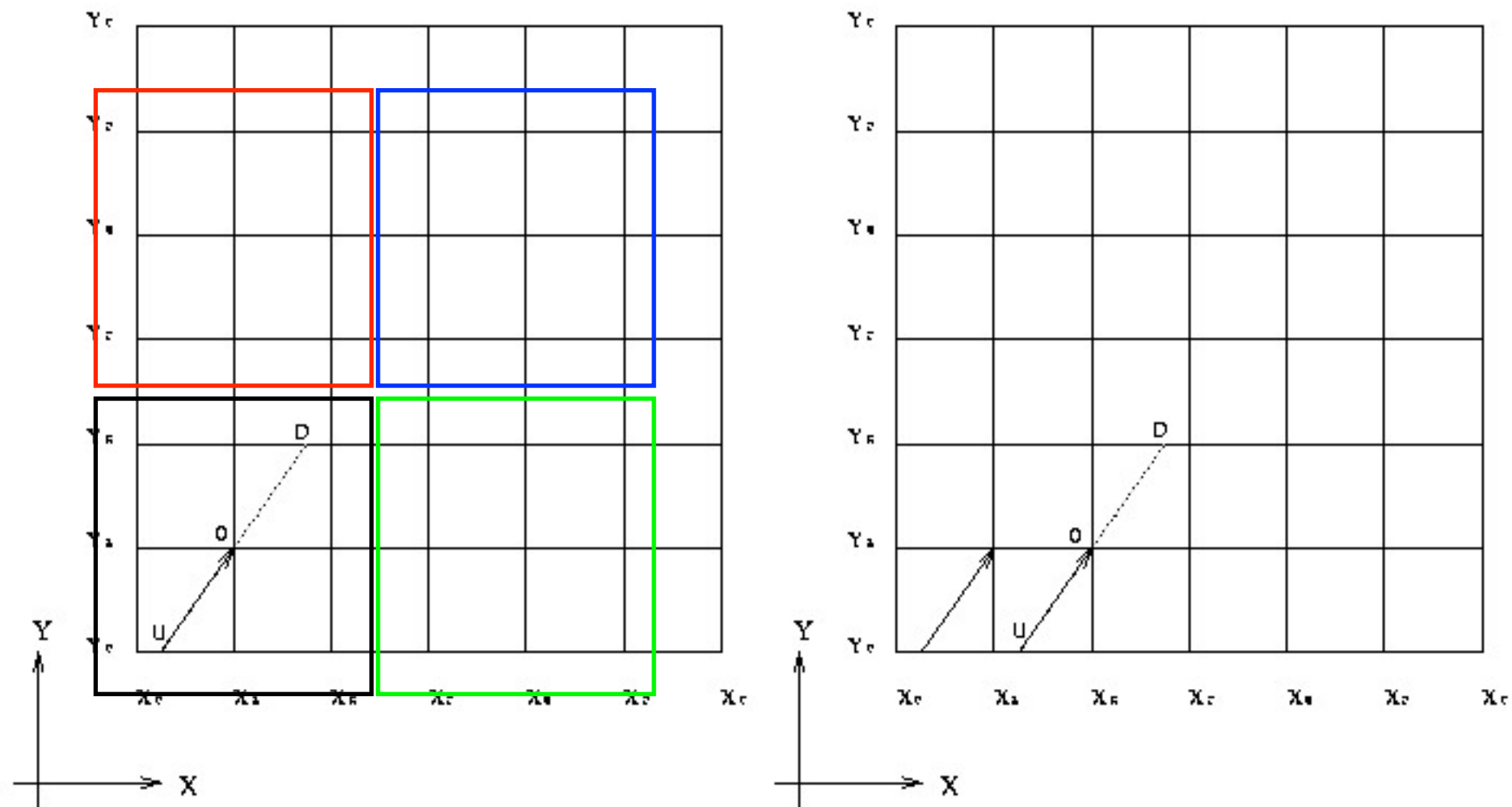
Parallelization strategies

Local rays



MPI: simple communication, complicated admin

Short characteristics



Order: passive processors
multiple sweeps

Energy equation

Radiative equilibrium

$$F_{\text{rad}} = \sigma T_{\text{eff}}^4$$

$$\nabla F = 0$$

$$\mu \frac{dI_\nu}{dz} = \chi_\nu (S_\nu - I_\nu)$$

integrate over angle

$$\frac{dF_\nu}{dz} = 2\pi \int_{-1}^1 \chi_\nu (S_\nu - I_\nu) d\mu$$

integrate over frequency

$$\frac{dF}{dz} = 2\pi \int_{-1}^1 \int_0^\infty \chi_\nu (S_\nu - I_\nu) d\nu d\mu = 0$$

isotropic χ_ν , S_ν gives

$$\int_0^\infty \chi_\nu (S_\nu - J_\nu) d\nu = 0$$

NB! flux not specified, only its constancy

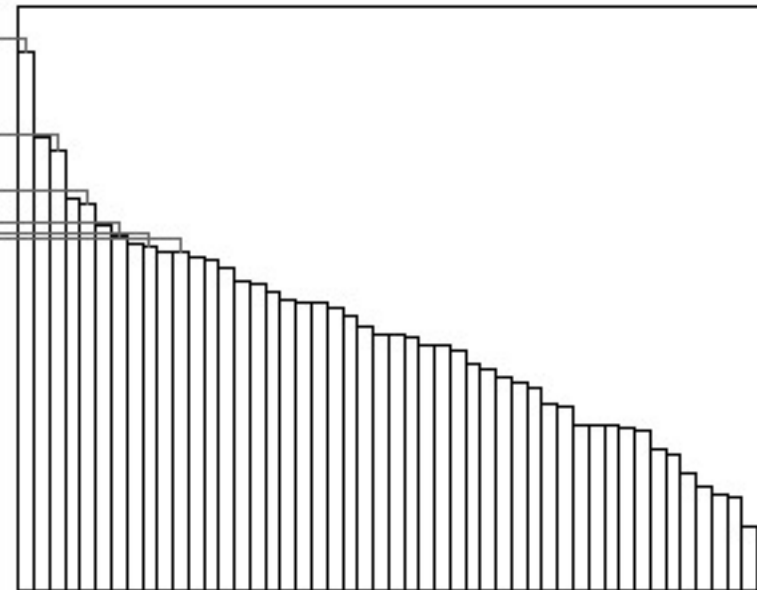
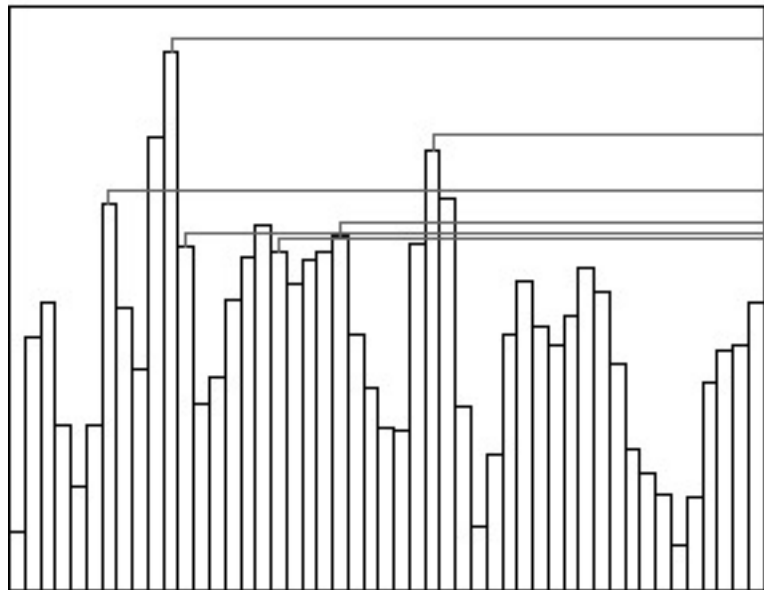
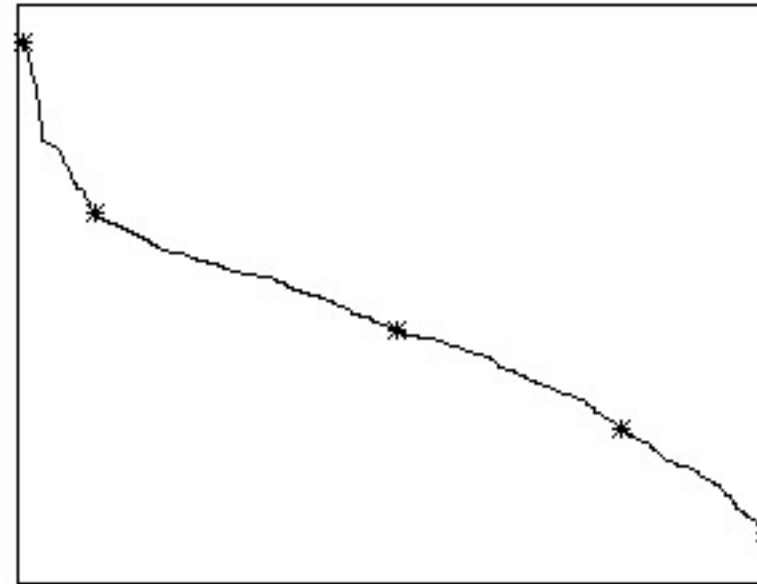
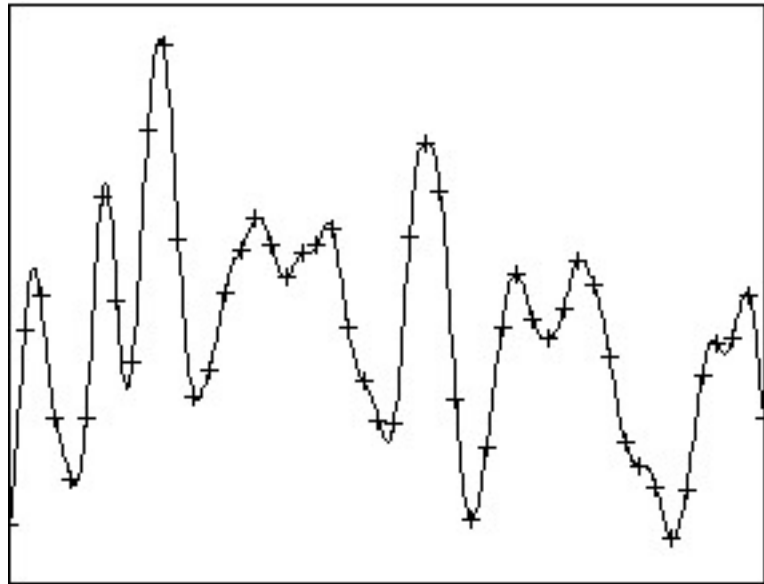
We thus need to solve the transfer equation at many frequencies throughout the spectrum

OS: Opacity sampling. Sample throughout the spectrum, enough points to get a statistically good representation of the integral ~ 10000 points.

ODF: Opacity distribution function. Reorder frequency points to get smoother function. Fewer points needed ~ 1000 points. Assumes that high opacity line up.

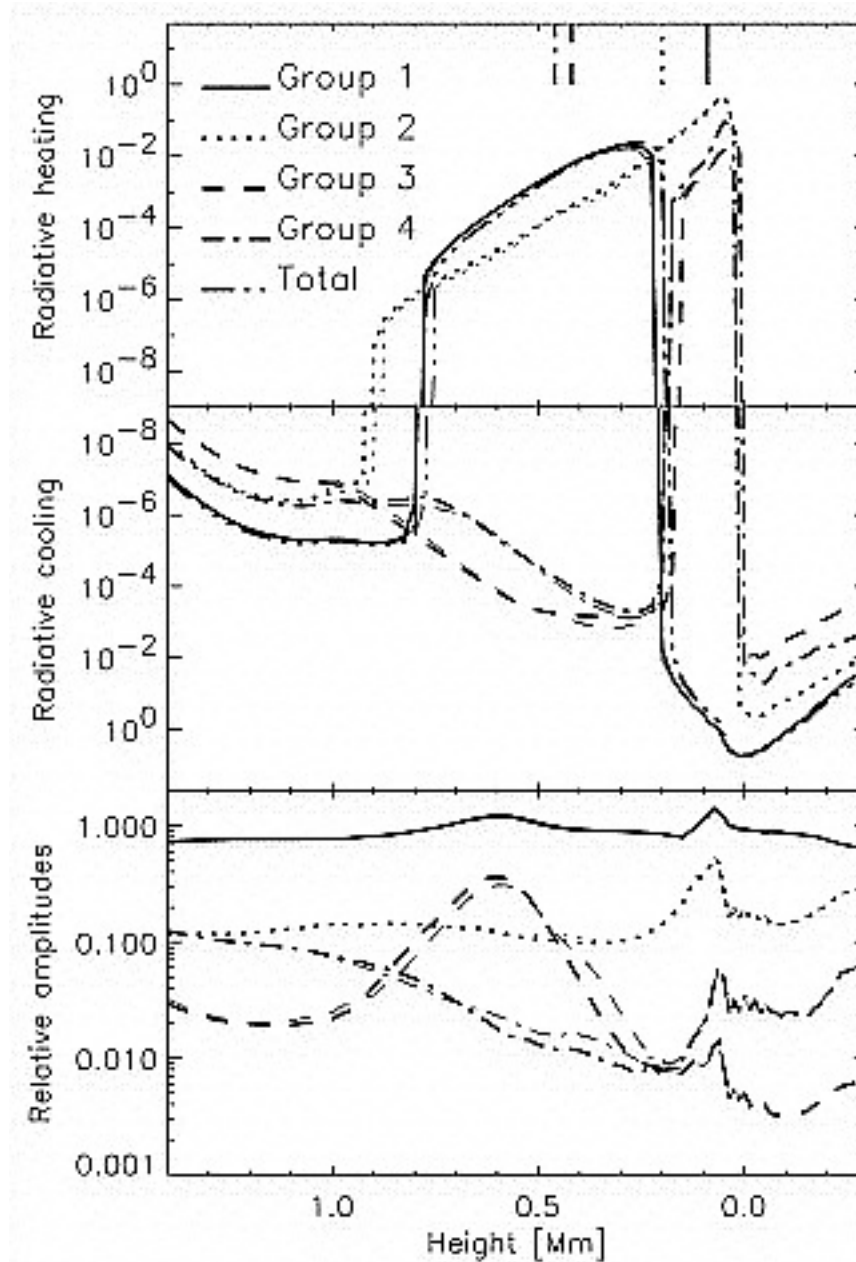
Multi group opacities. As ODF but average also the source function. ~ 4 points.

ODF



Multi-group opacities

$$\int Y_{\lambda} d\lambda = \sum_{\lambda} Y_{\lambda ij} w_{ij} = \sum_i \sum_j Y_{\lambda ij} w_{ij}$$



Linearization

We used to have:

$$\delta j_{\nu\mu} = \frac{\partial j_{\nu\mu}}{\partial n_i} \delta n_i + \frac{\partial j_{\nu\mu}}{\partial n_j} \delta n_j$$

If the atmosphere is not given we get extra variables to solve for:

$$\delta\rho, \delta T, \delta n_e$$

and extra derivatives with respect to these variables

$$\delta j_{\nu\mu} = \frac{\partial j_{\nu\mu}}{\partial \rho} \delta\rho + \frac{\partial j_{\nu\mu}}{\partial T} \delta T + \frac{\partial j_{\nu\mu}}{\partial n_e} \delta n_e + \sum_{i=1}^{N_L} \frac{\partial j_{\nu\mu}}{\partial n_i} \delta n_i$$

$$\frac{\partial j_{\nu c}}{\partial x}, \frac{\partial \kappa_{\nu c}}{\partial x}, \frac{\partial \alpha_{ij}}{\partial x}, \frac{\partial G_{ij}}{\partial x}, \frac{\partial C_{ij}}{\partial x}$$

are no longer zero

Extra equations: Hydrostatic equilibrium

Energy equation, charge conservation

Examples, non-LTE

- non-local, non-linear
- 1D: Accelerated Lambda Iteration (ALI)
 - 500-1000 atomic levels possible
 - codes available (MULTI, RH (Uitenbroek),...)
- 3D: ALI + long or short characteristics
 - 20-30 levels possible
 - not as easy to use as black-box (convergence problems, discretization issues etc) (RH (Uitenbroek), MULTI3D)

Examples

- Contribution & response functions
- non-Statistical equilibrium
- 3D simulations from convection zone to corona
- 3D radiative transfer
- IRIS
- Mg II diagnostics

Contribution functions

$$I_{\nu\mu}(0) = \int C_I(x) dx$$

$$C_I(\tau_\nu) = \frac{1}{\mu} S_\nu(\tau_\nu) e^{-\tau_\nu/\mu}$$

$$C_I(z) = \frac{1}{\mu} S_\nu(\tau_\nu) e^{-\tau_\nu/\mu} \chi_\nu$$

Contribution functions give the contributions from different layers of the atmosphere to a given quantity.

Rewrite of contribution function

$$C_I(z) = \frac{1}{\mu} S_\nu(\tau_\nu) e^{-\tau_\nu/\mu} \chi_\nu$$

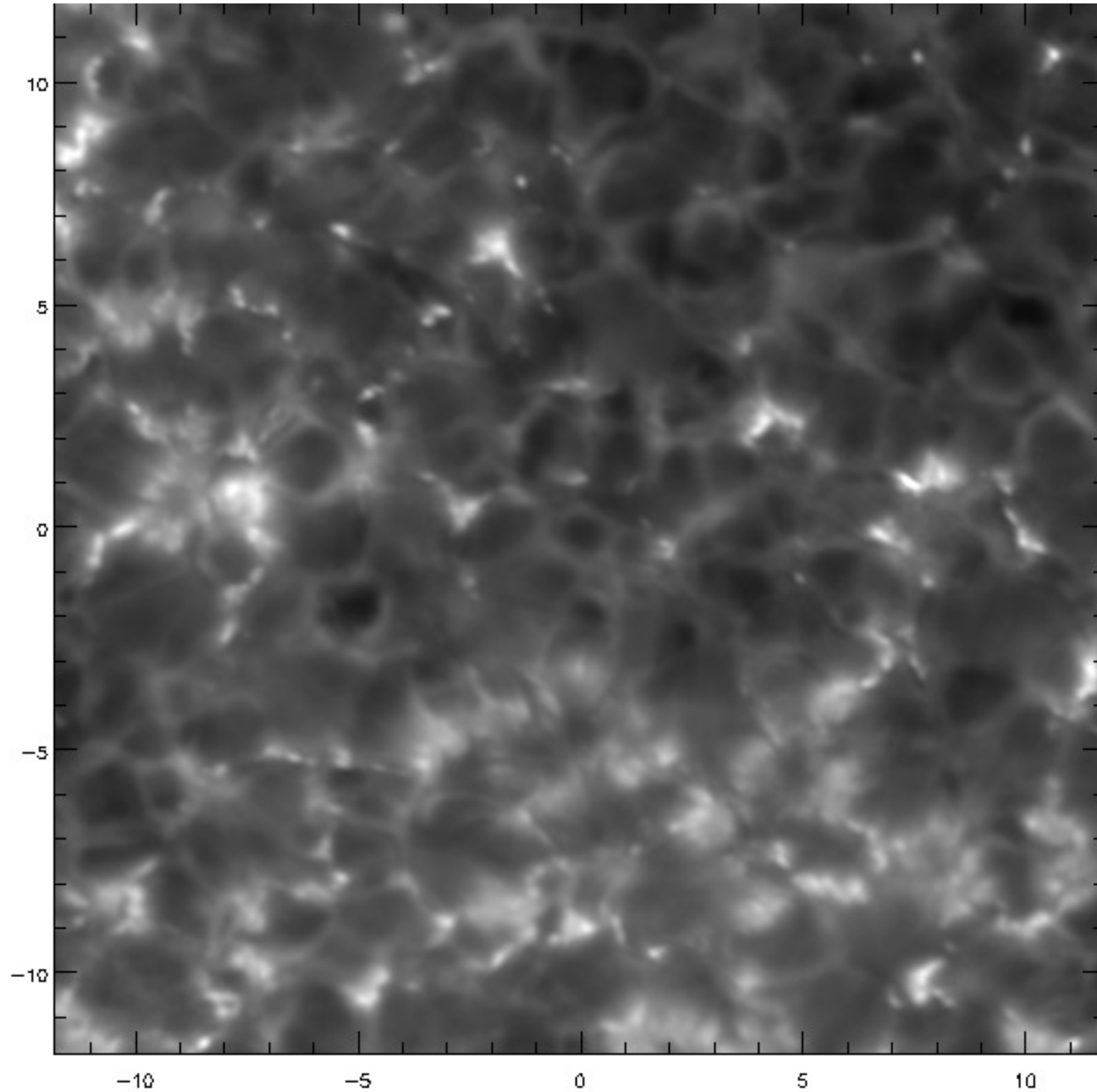
$$C_I(z) = S_\nu(\tau_\nu) \frac{1}{\mu} \tau_\nu e^{-\tau_\nu/\mu} \frac{\chi_\nu}{\tau_\nu}$$

Source term

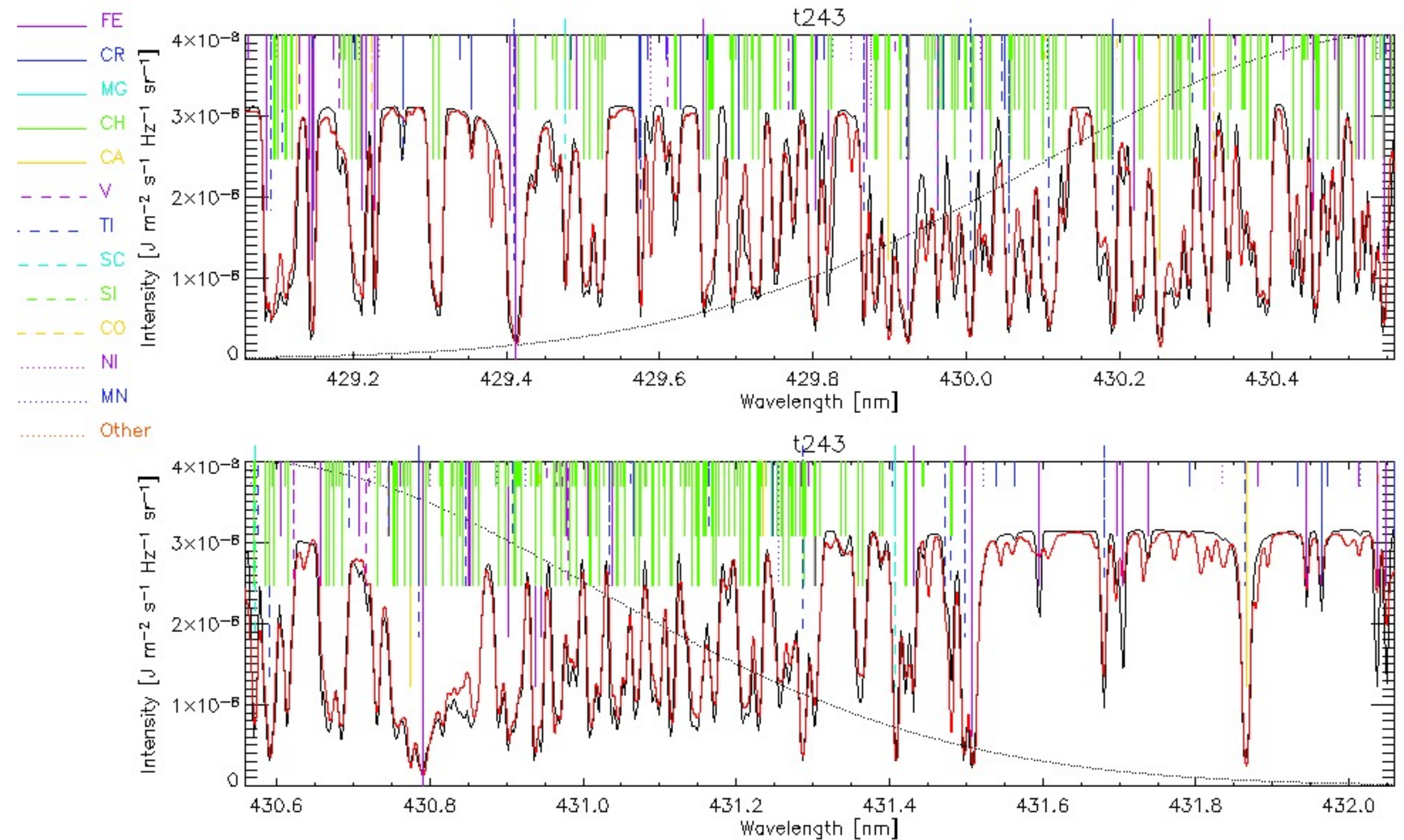
Maximum for $\tau_\nu = \mu$

Dynamic term

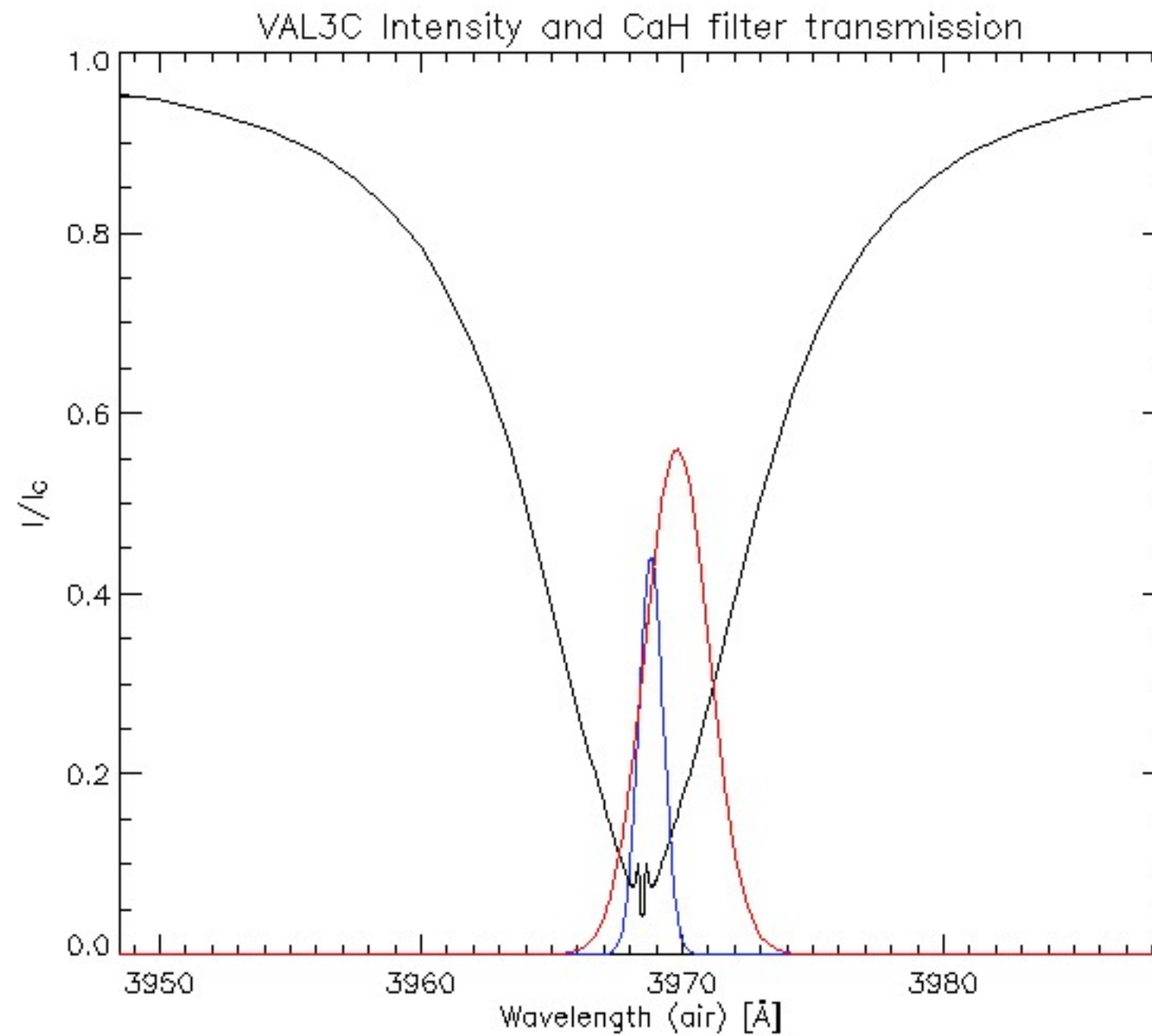
G-band vs Ca H filtergram



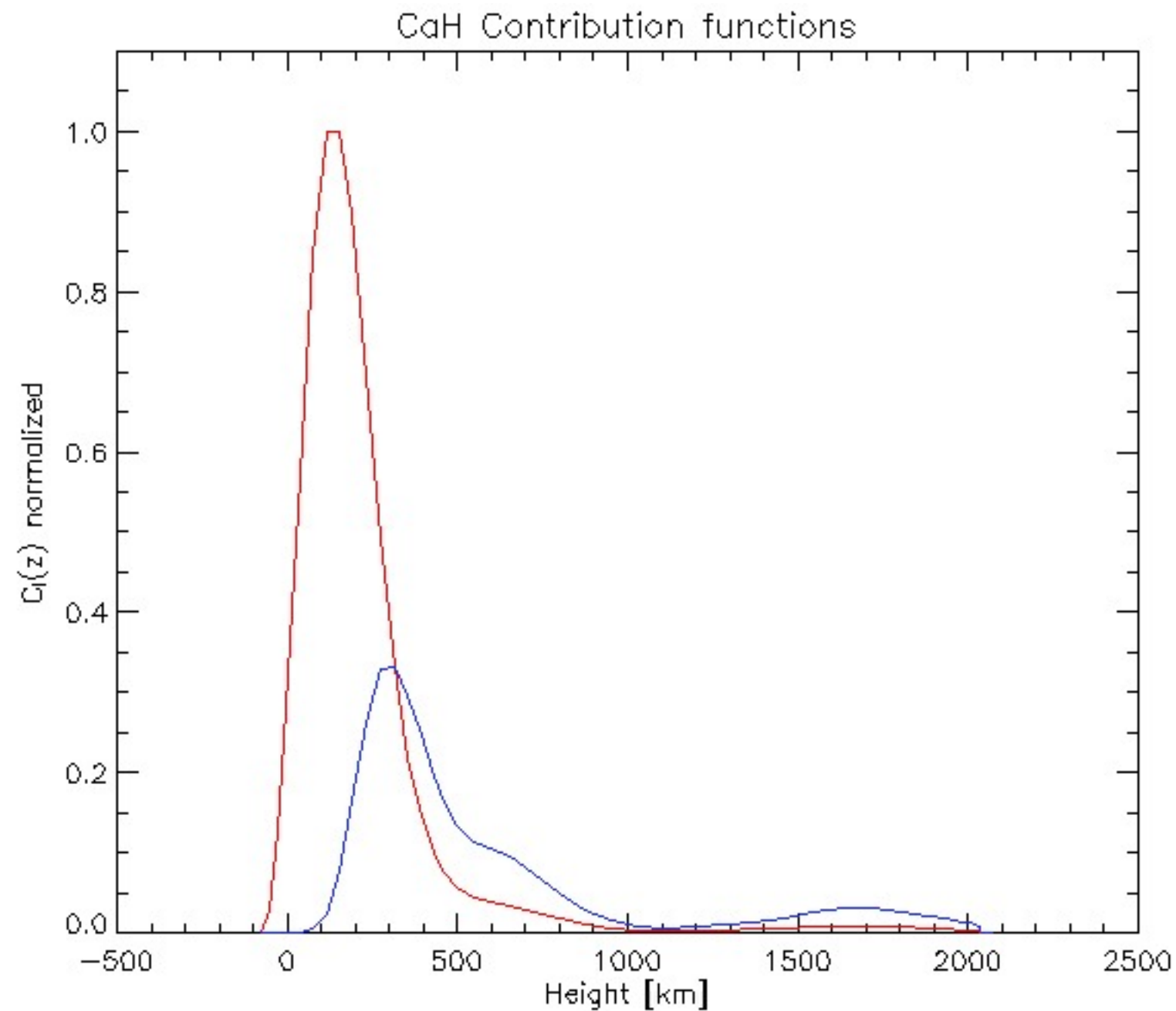
Synthetic spectrum



LaPalma Ca H filters



Contribution to Ca-H filter intensity



Response functions

$$\frac{\Delta I}{I} = \int_{-\infty}^{\infty} R(z) \frac{\Delta T}{T}(z) dz$$

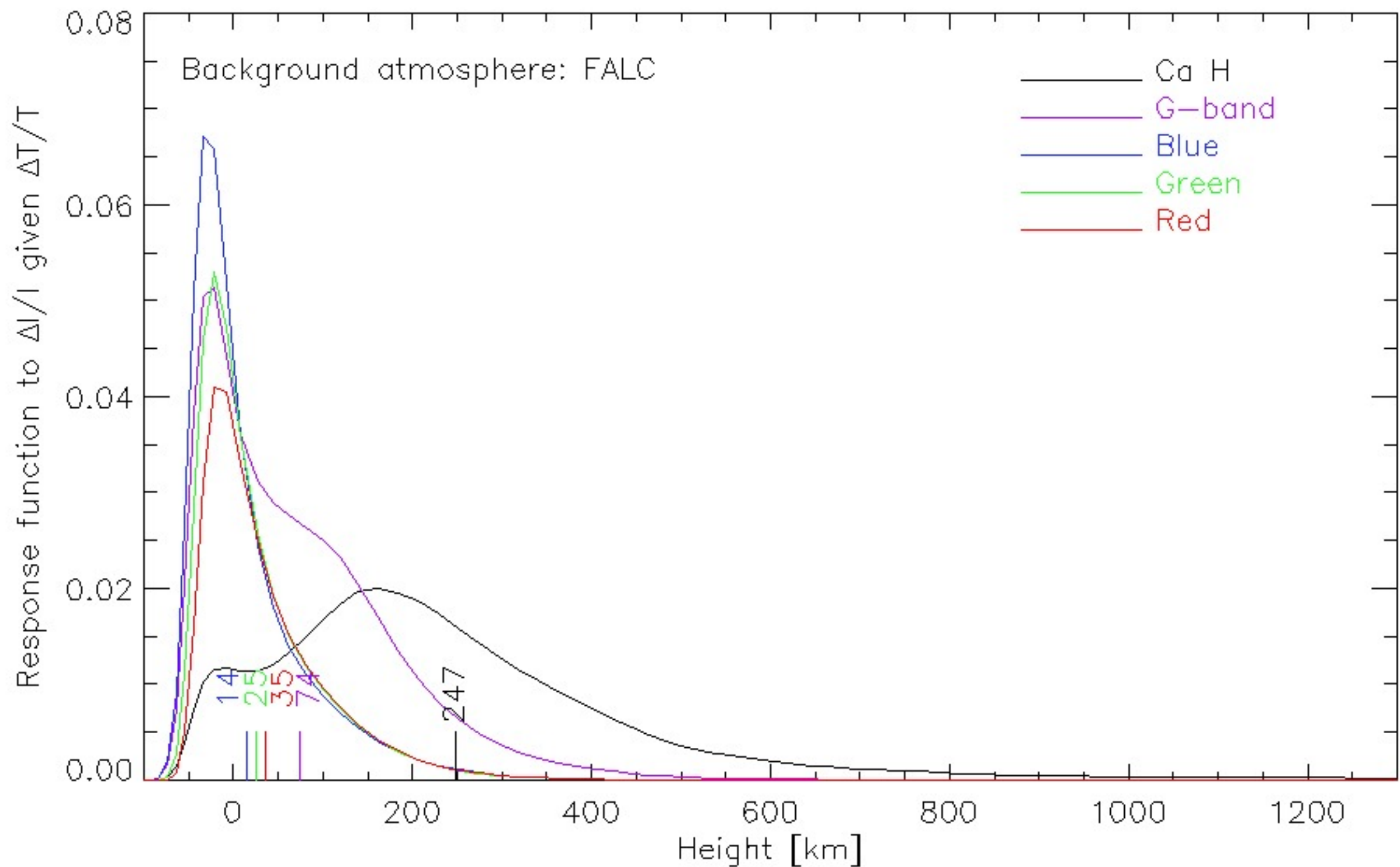
Numerical calculation of a response function

$$\begin{aligned} \frac{\Delta T}{T}(z) &= C, z \leq z' \\ &= 0 \quad z > z' \end{aligned}$$

$$\frac{\Delta I}{I}(z') = C \int_{-\infty}^{z'} R(z) dz$$

$$R(z') = \frac{1}{C} \frac{d}{dz'} \frac{\Delta I}{I}(z')$$

Response functions of Hinode wide band filters



non-Statistical equilibrium

- 2-level case
- linear rate matrix
- hydrogen ionization

non-Statistical equilibrium

$$\frac{Dn_i}{Dt} = \sum_{j \neq i}^N n_j P_{ji} - n_i \sum_{j \neq i}^N P_{ij}$$

2-level case:

$$n_1(t) = n_1(\infty) + (n_1(0) - n_1(\infty))e^{-(P_{12}+P_{21})t}$$

Timescale depends on both upward and downward rate

There is only one timescale involved

non-Statistical equilibrium

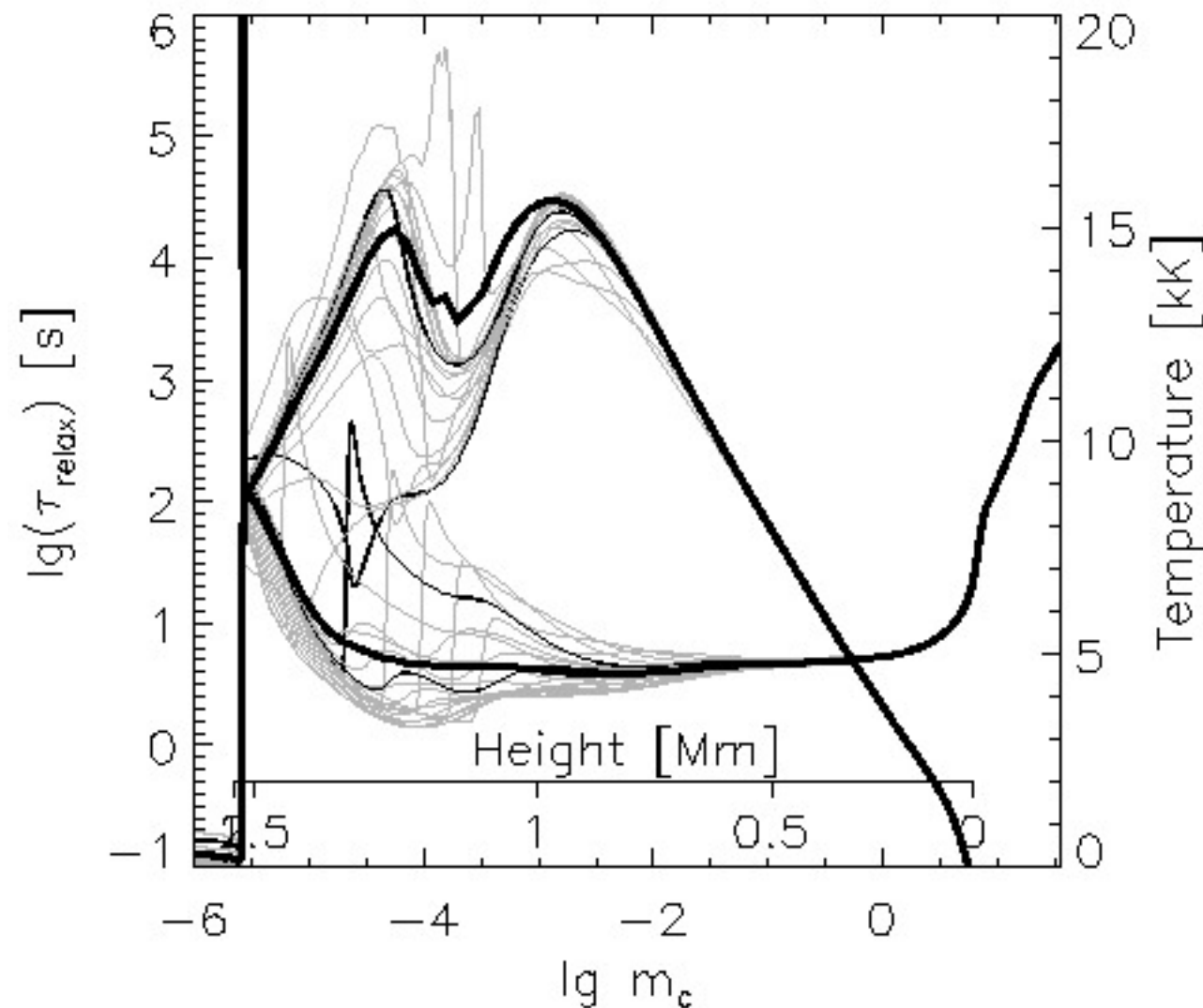
$$\frac{Dn_i}{Dt} = \sum_{j \neq i}^N n_j P_{ji} - n_i \sum_{j \neq i}^N P_{ij}$$

$$\frac{D\mathbf{n}}{Dt} = \mathbf{W}\mathbf{n}$$

linear rate matrix:

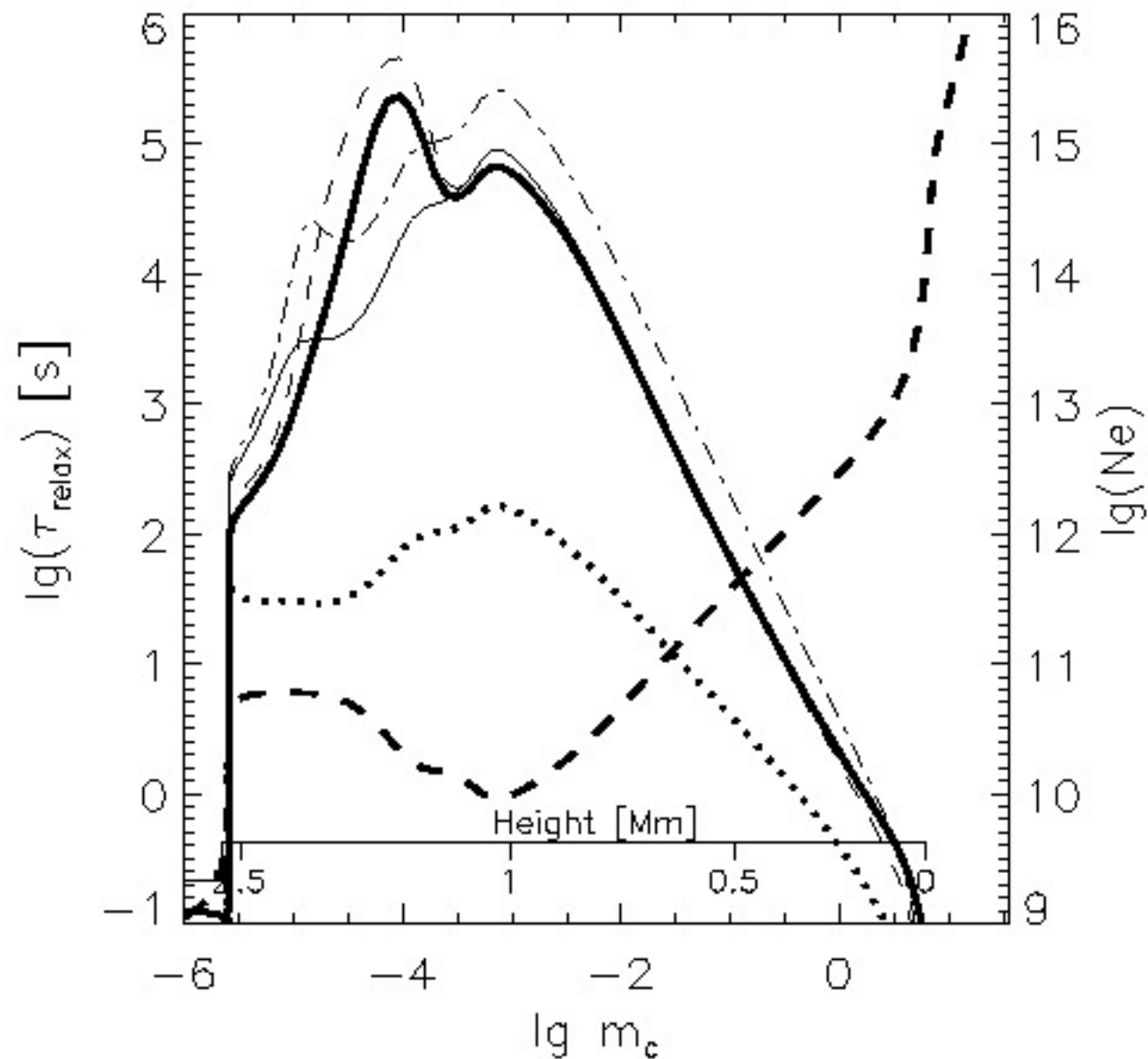
Populations can be written as linear combination of eigenvectors of $\mathbf{W}$ with time-evolution given by eigenvalues of $\mathbf{W}$ (Judge 2005, JQSRT, 92, 479)

Hydrogen ionization



Time scale for hydrogen ionization/recombination is highly time-varying. Fast rates when temperature is high (ionizing phase), slow rates when temperature is low (recombining phase).

Hydrogen ionization

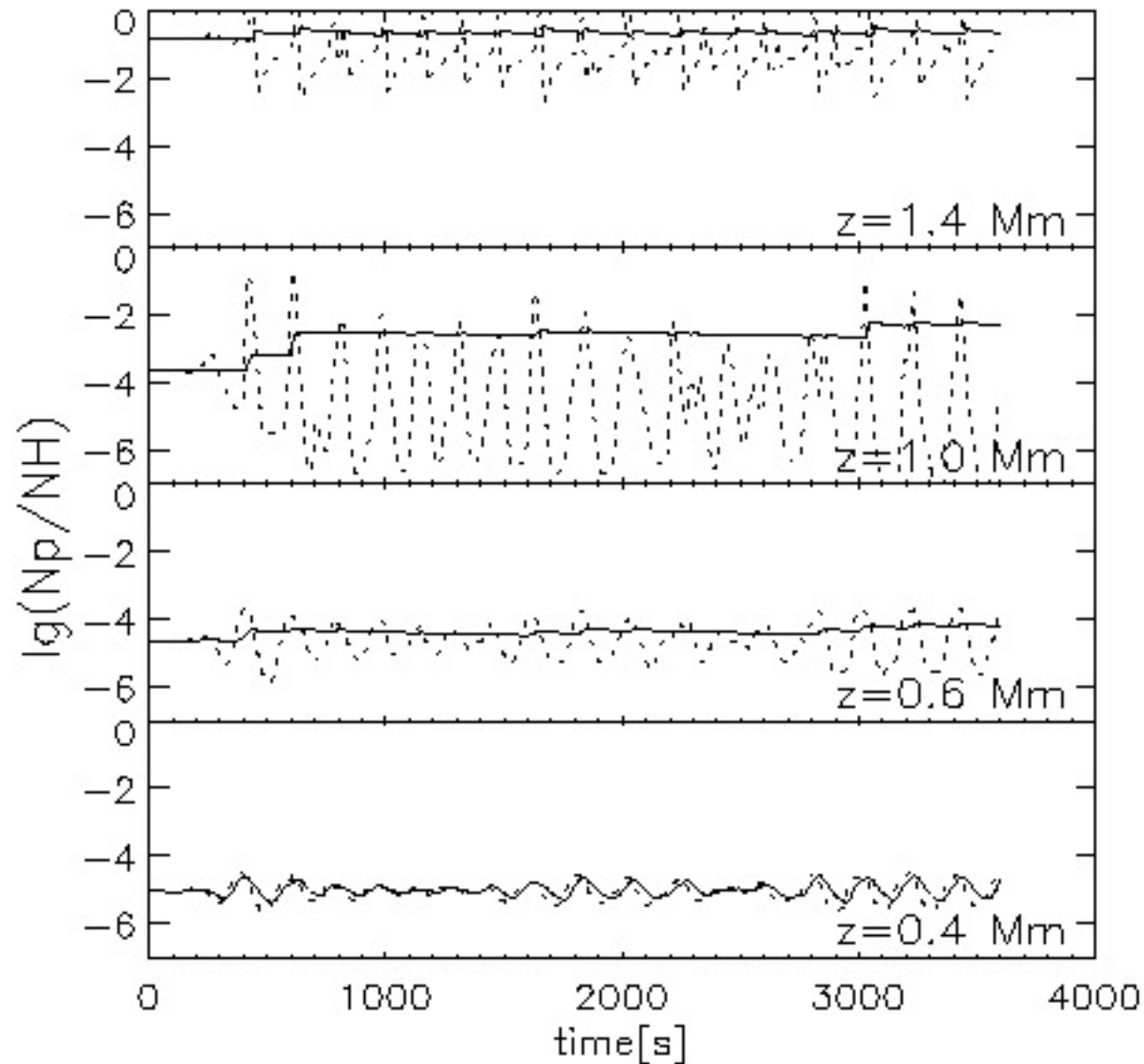


Electron density (thick dashed)
Eigenvalue timescales (thick dotted)
only collisions (dot-dashed)
Lyman lines in detailed balance (thin solid)
Lyman-alpha in escape probability (dashed)
Numerical result (thick solid)

Eigenvalues of rate-matrix give erroneous timescales for non-linear rate-matrix. Exclusion of large, canceling rates (Lyman transitions) give much better results.

(Carlsson & Stein, 2002, ApJ 572,626)

Hydrogen ionization



Time dependent ionization (solid)
Equilibrium ionization (dashed)

Slow rates when recombining results in ionization higher than equilibrium values.

3D RMHD models

BIFROST

Hansteen 2004, Hansteen, Carlsson, Gudiksen 2007, Sykora, Hansteen, Carlsson 2008,
Gudiksen et al 2011

- 6th order scheme, with “artificial viscosity/diffusion”
- Open vertical boundaries, horizontally periodic
- Possible to introduce field through bottom boundary

- “Realistic” EOS
- Detailed radiative transfer along 48 rays
 - Multi group opacities (4 bins) with scattering
- NLTE losses in the chromosphere, optically thin in corona

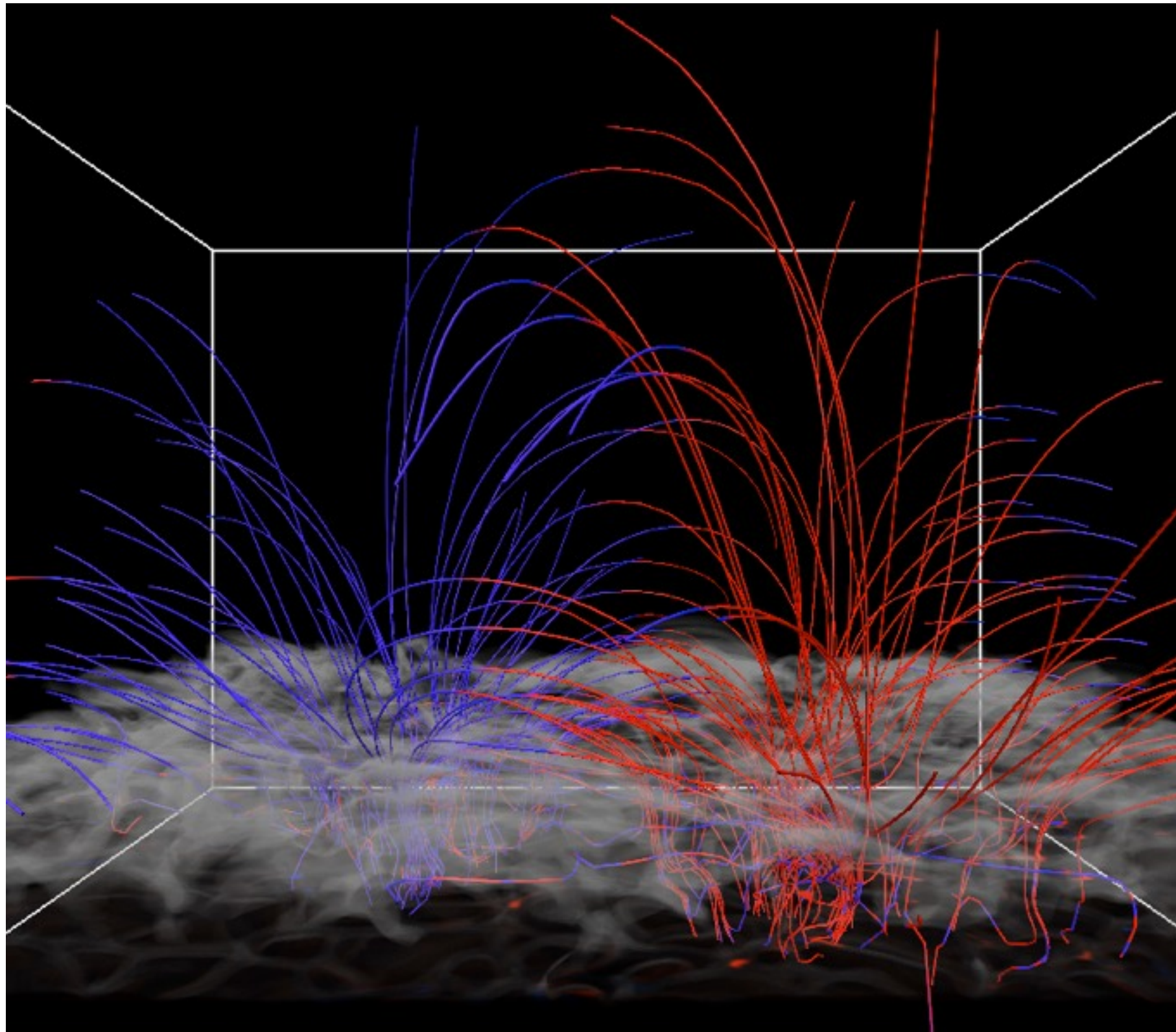
- Conduction along field lines
 - Operator split and solved by using multi grid method

- Time dependent Hydrogen ionization
- Generalized Ohm’s Law

“enhanced network” simulation

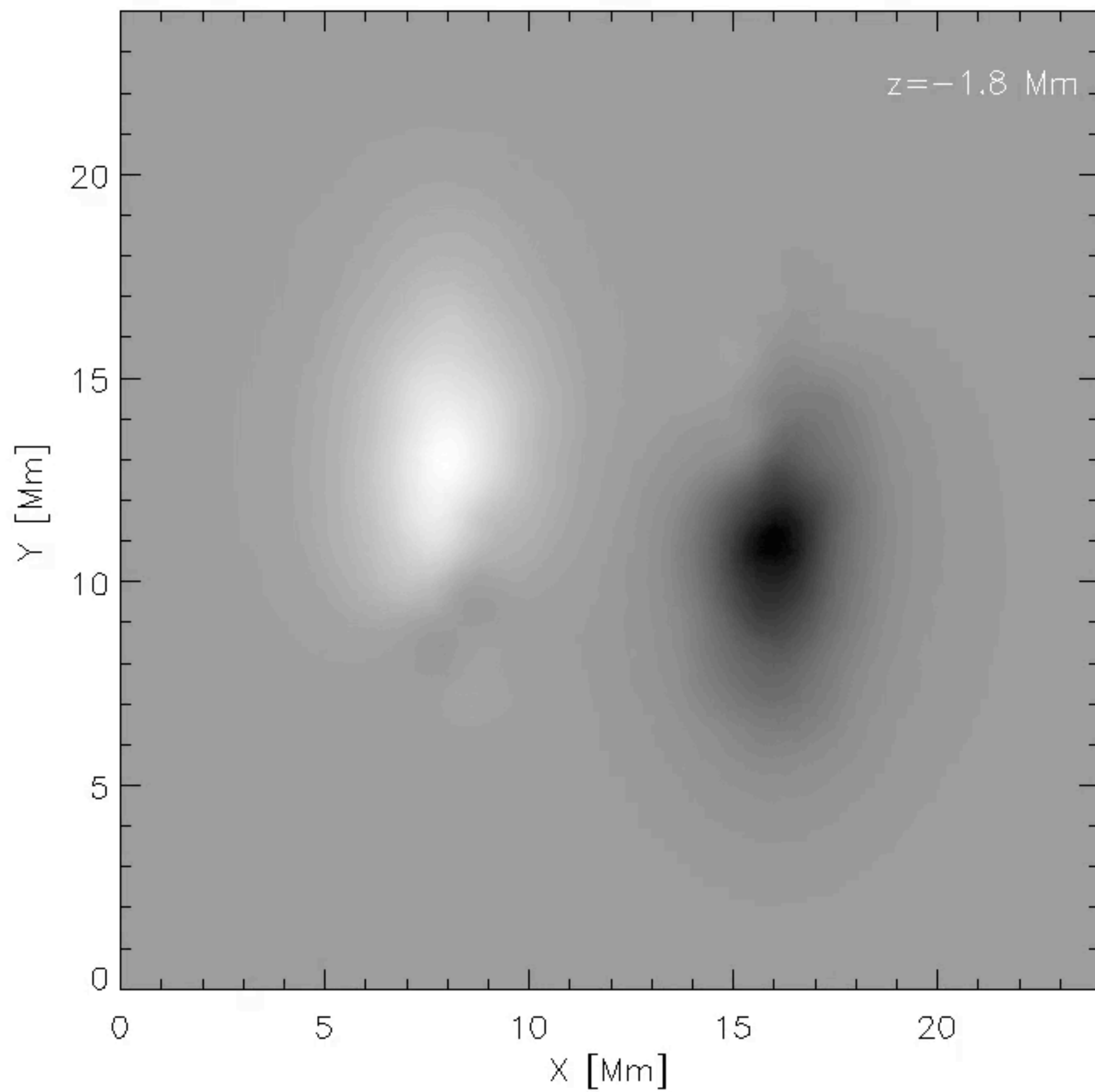
<http://sdc.uio.no/search/simulations>

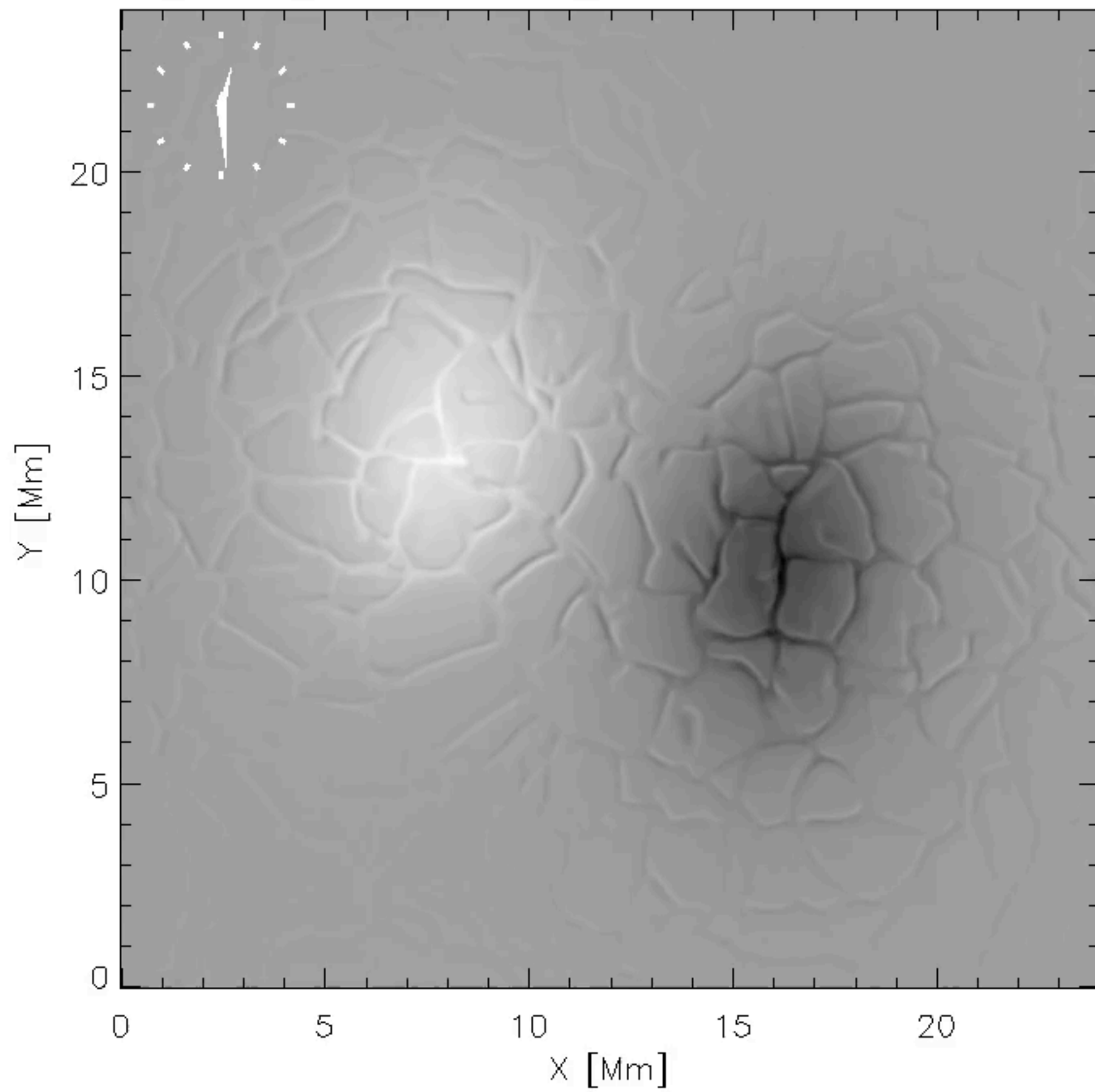
IRIS Technical Note 33; Carlsson et al 2014



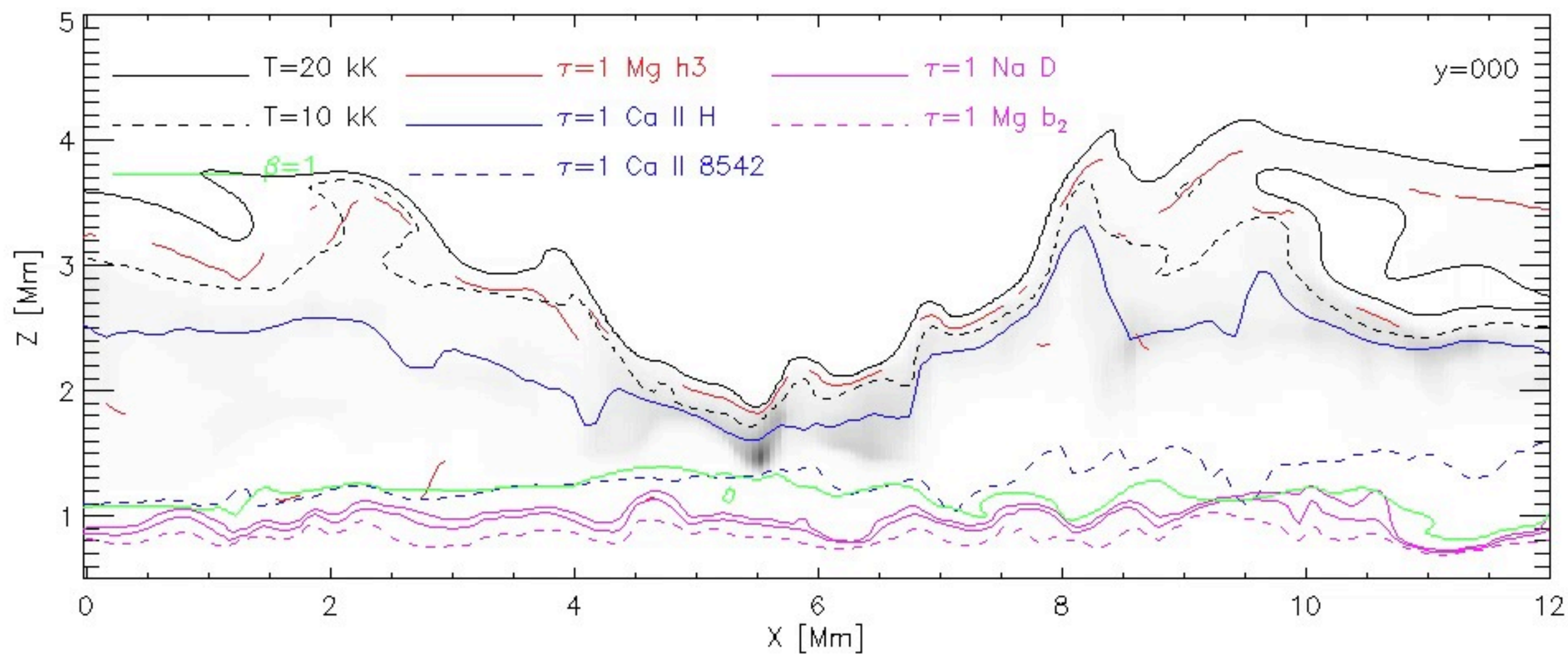
Corona

Transition region
Chromosphere
Photosphere
Convection zone



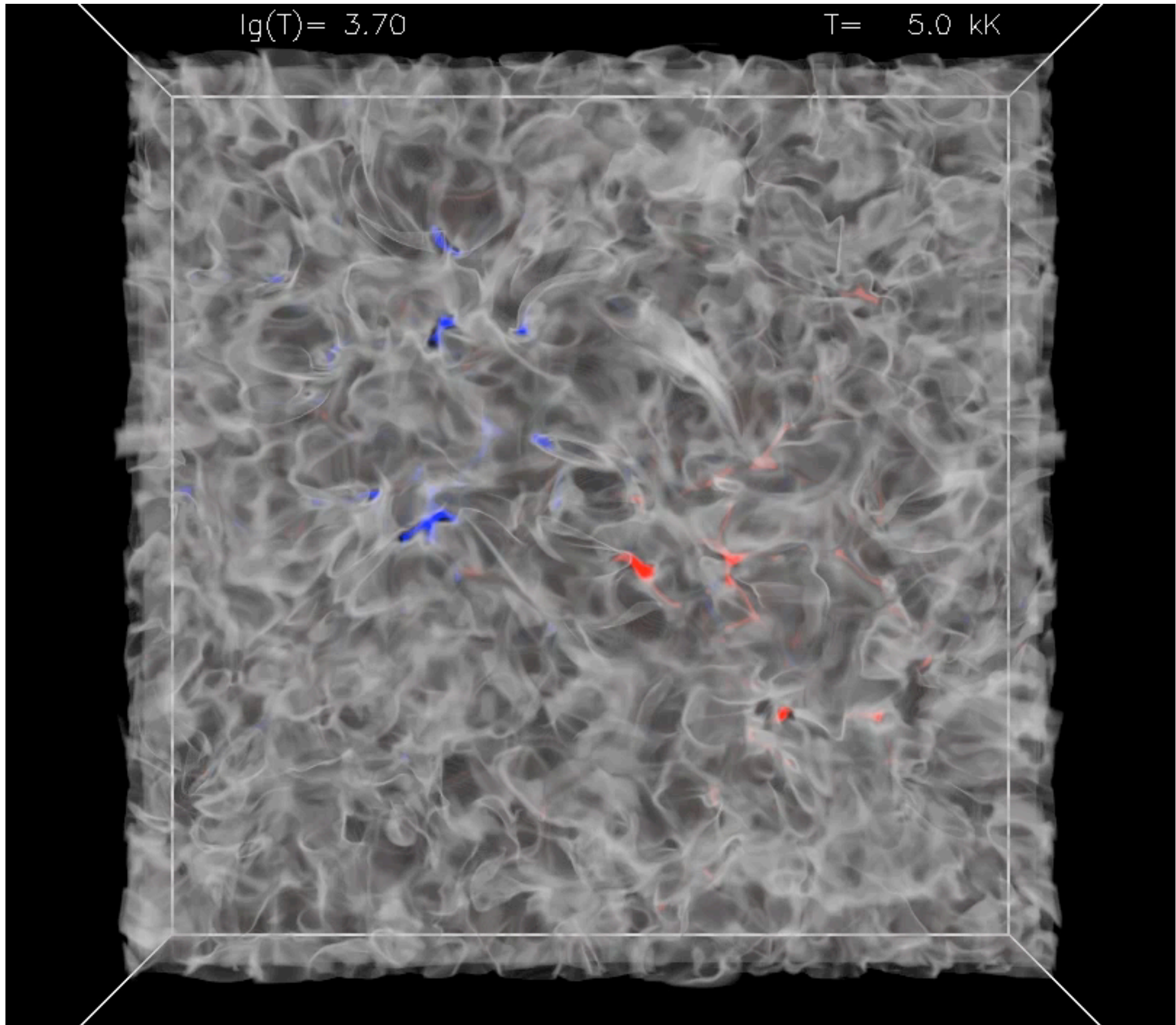


Transition region corrugated



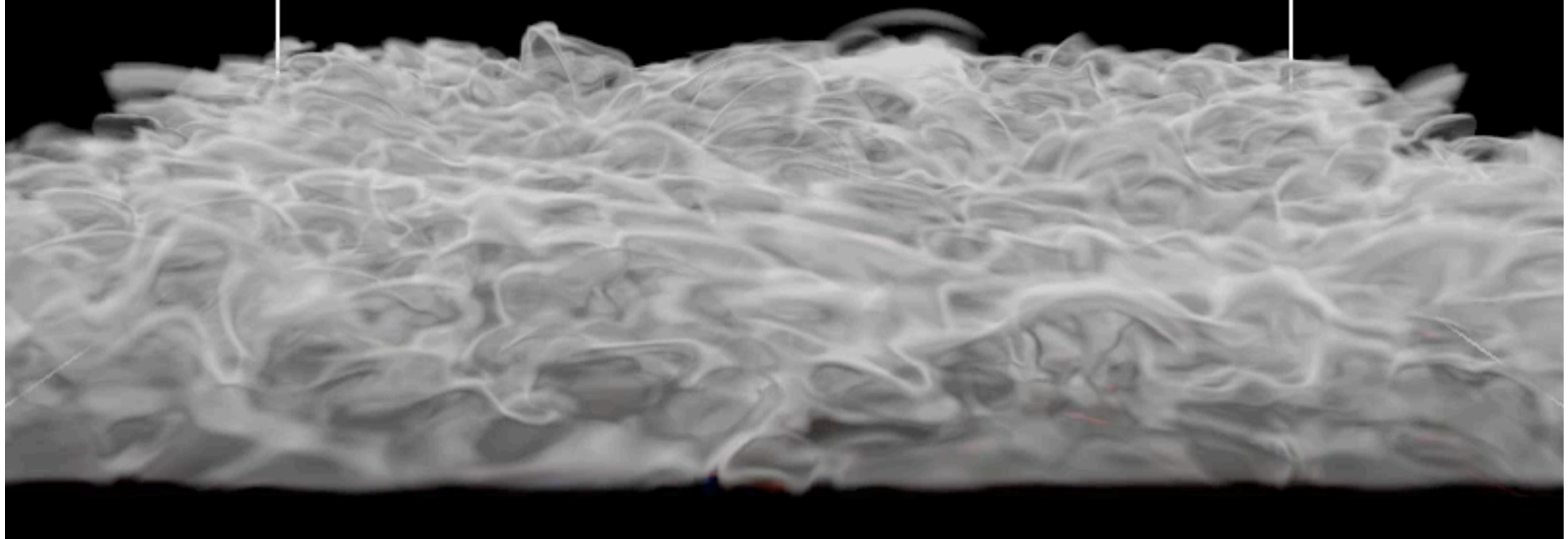
$\lg(T) = 3.70$

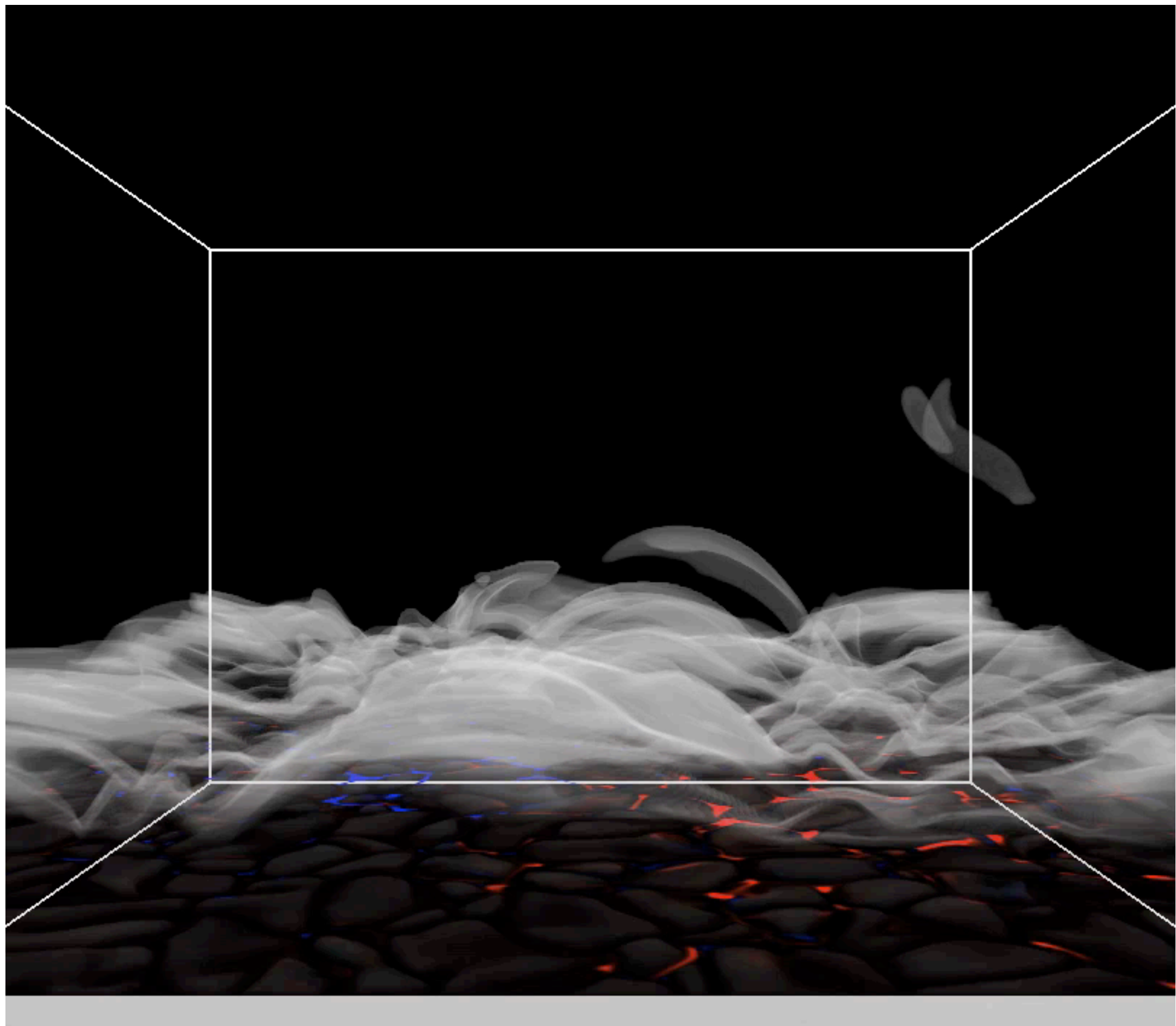
$T = 5.0 \text{ kK}$



$\lg(T) = 3.70$

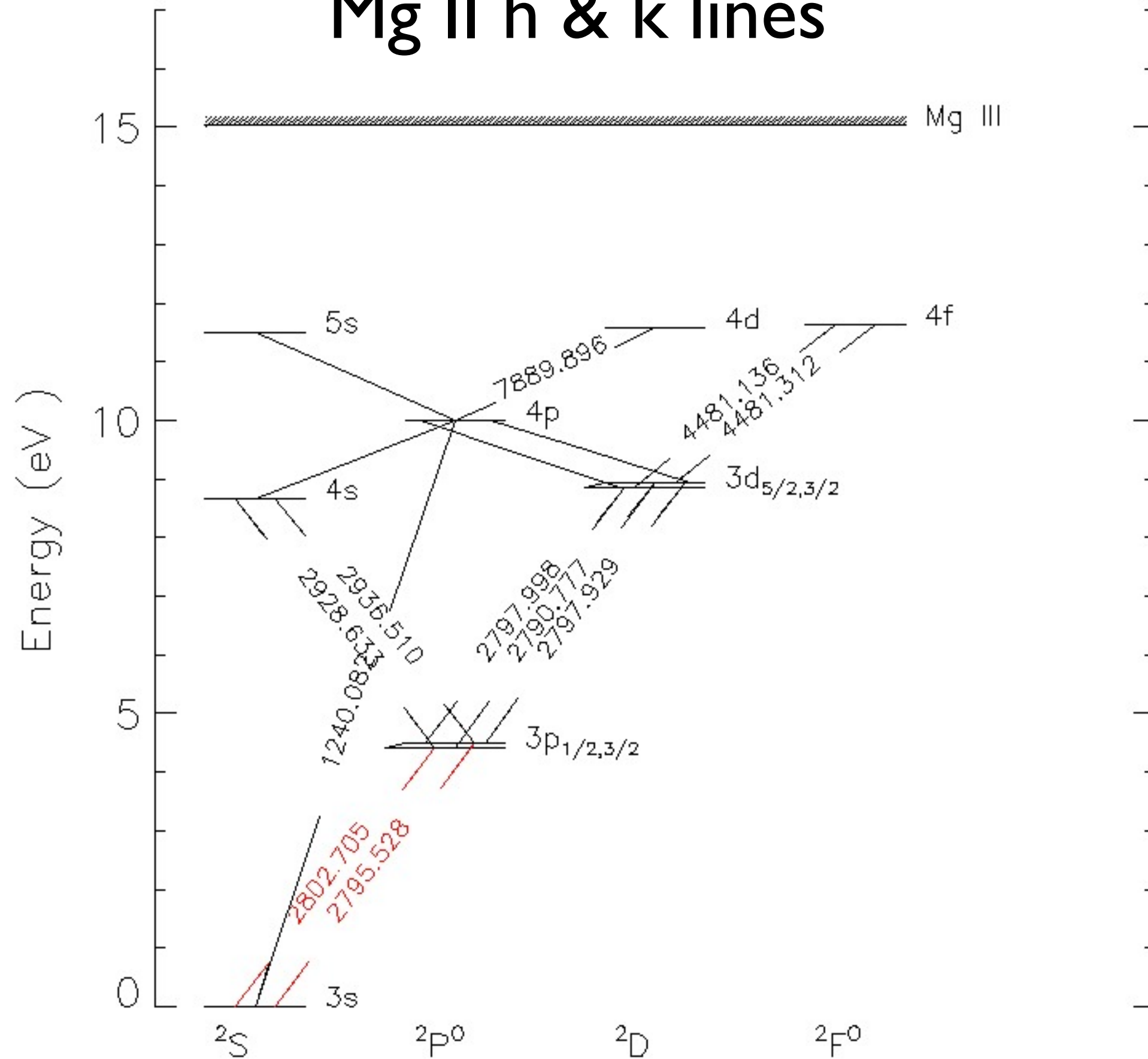
$T = 5.0 \text{ kK}$



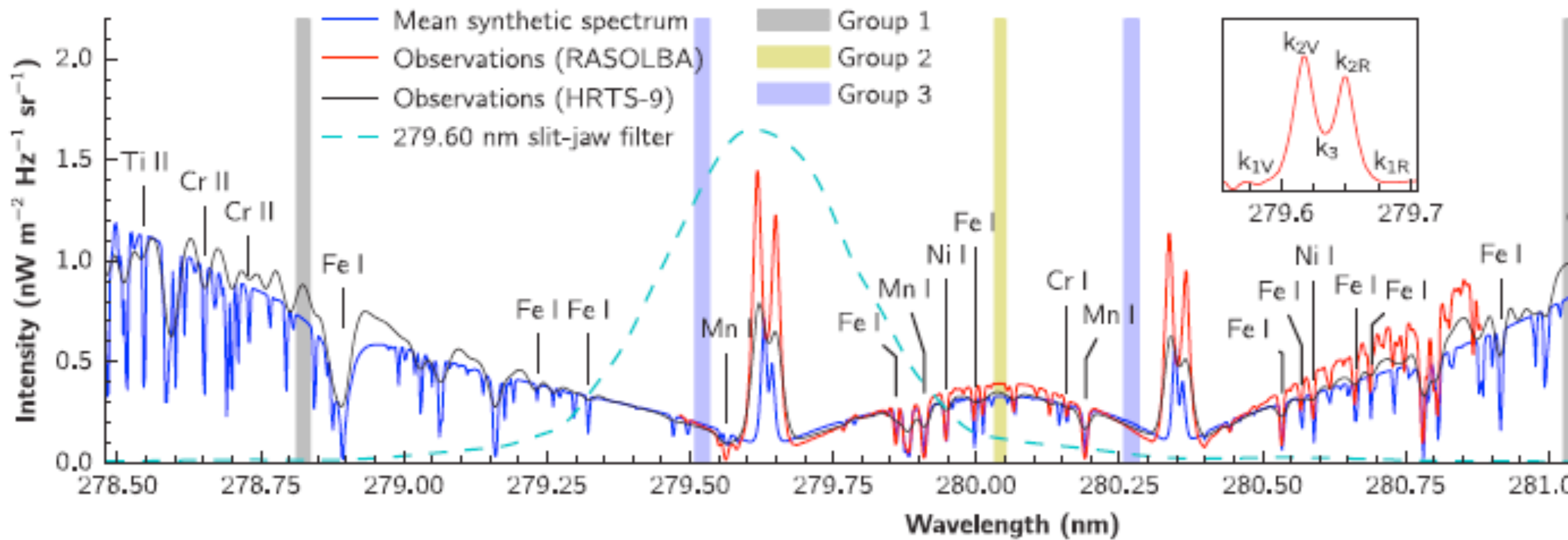


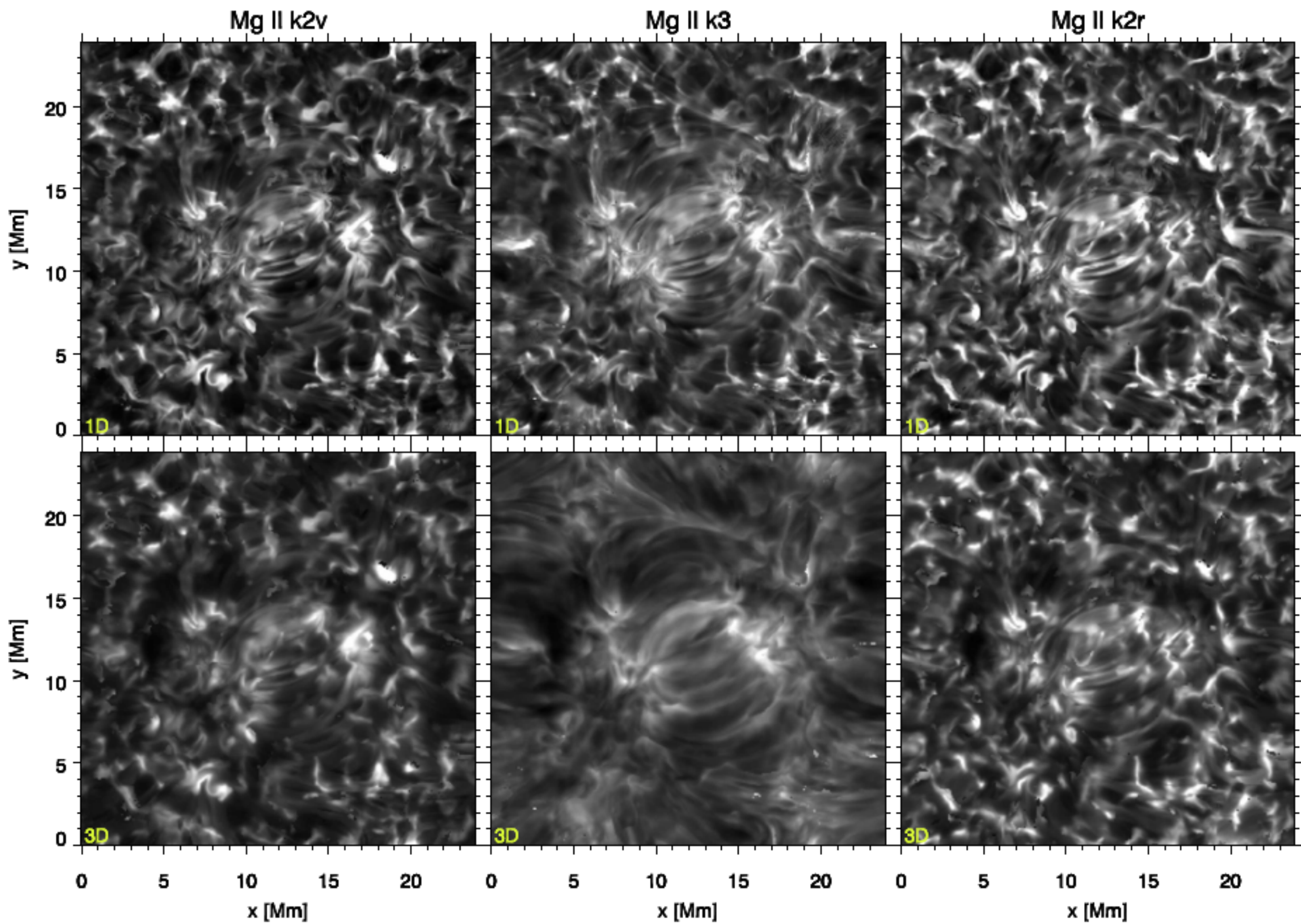
3D radiative transfer

Mg II h & k lines



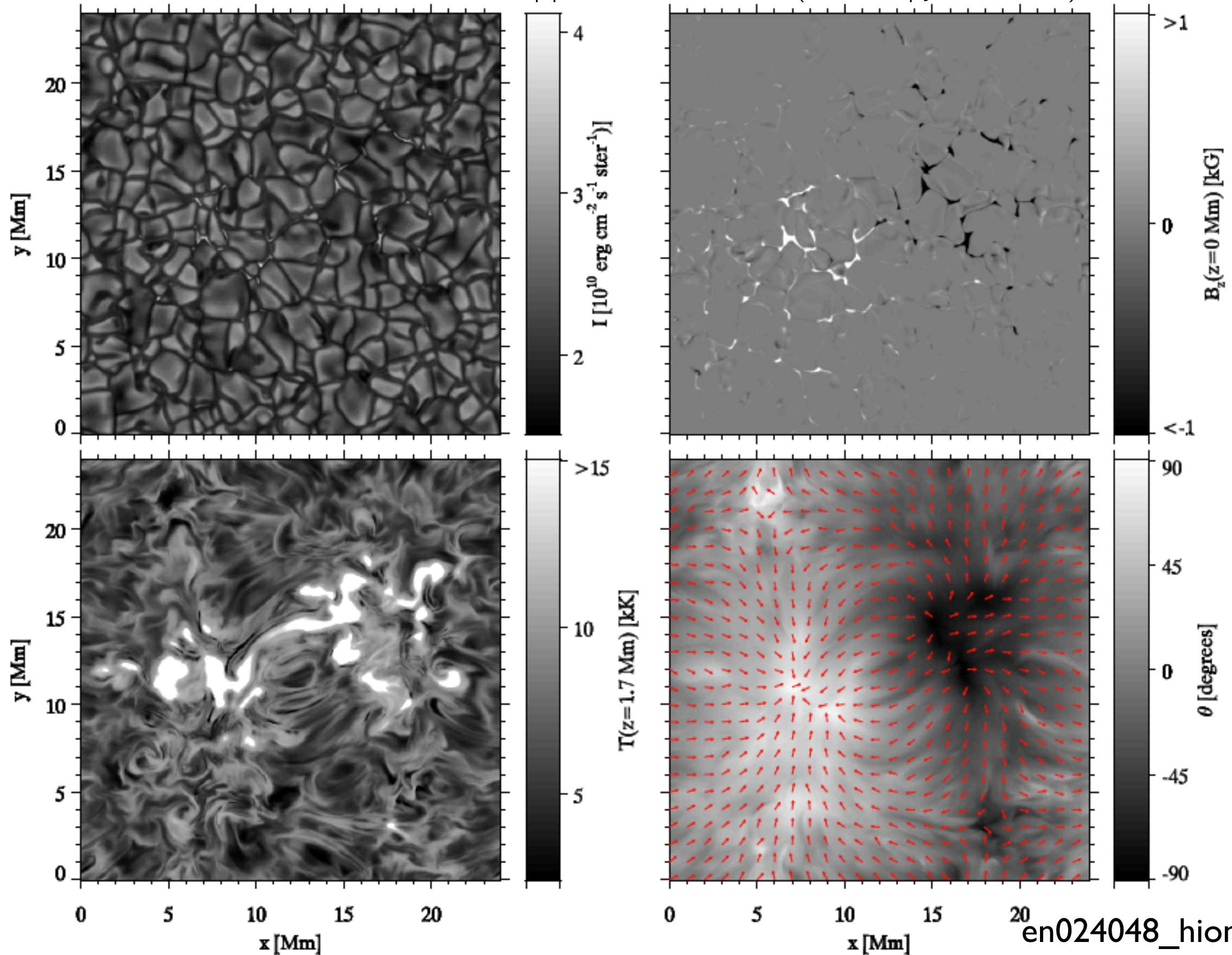
Mg II h & k lines





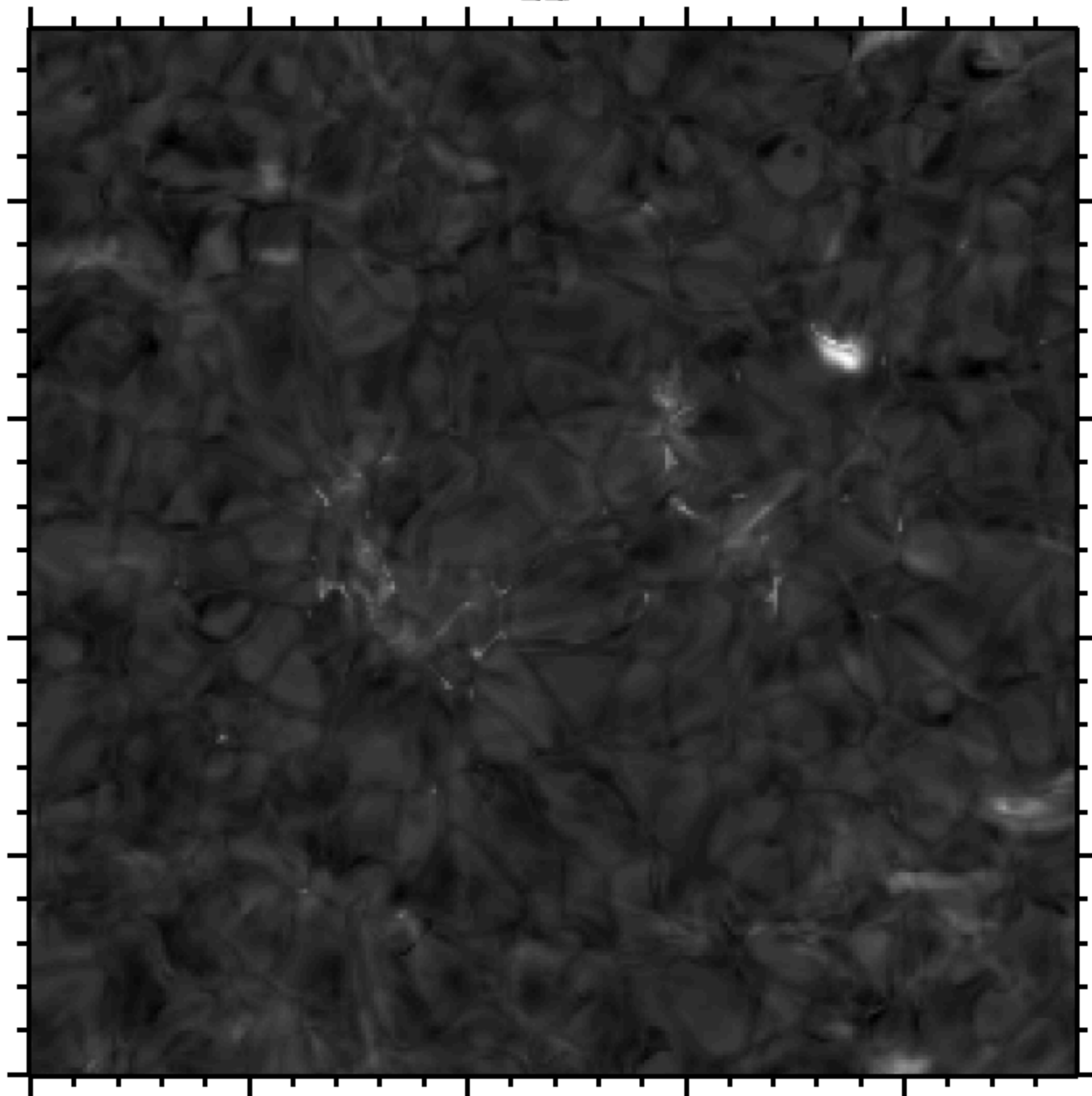
H- α

Leenaarts, Carlsson, Rouppe van der Voort (2012, ApJ 749,L136)

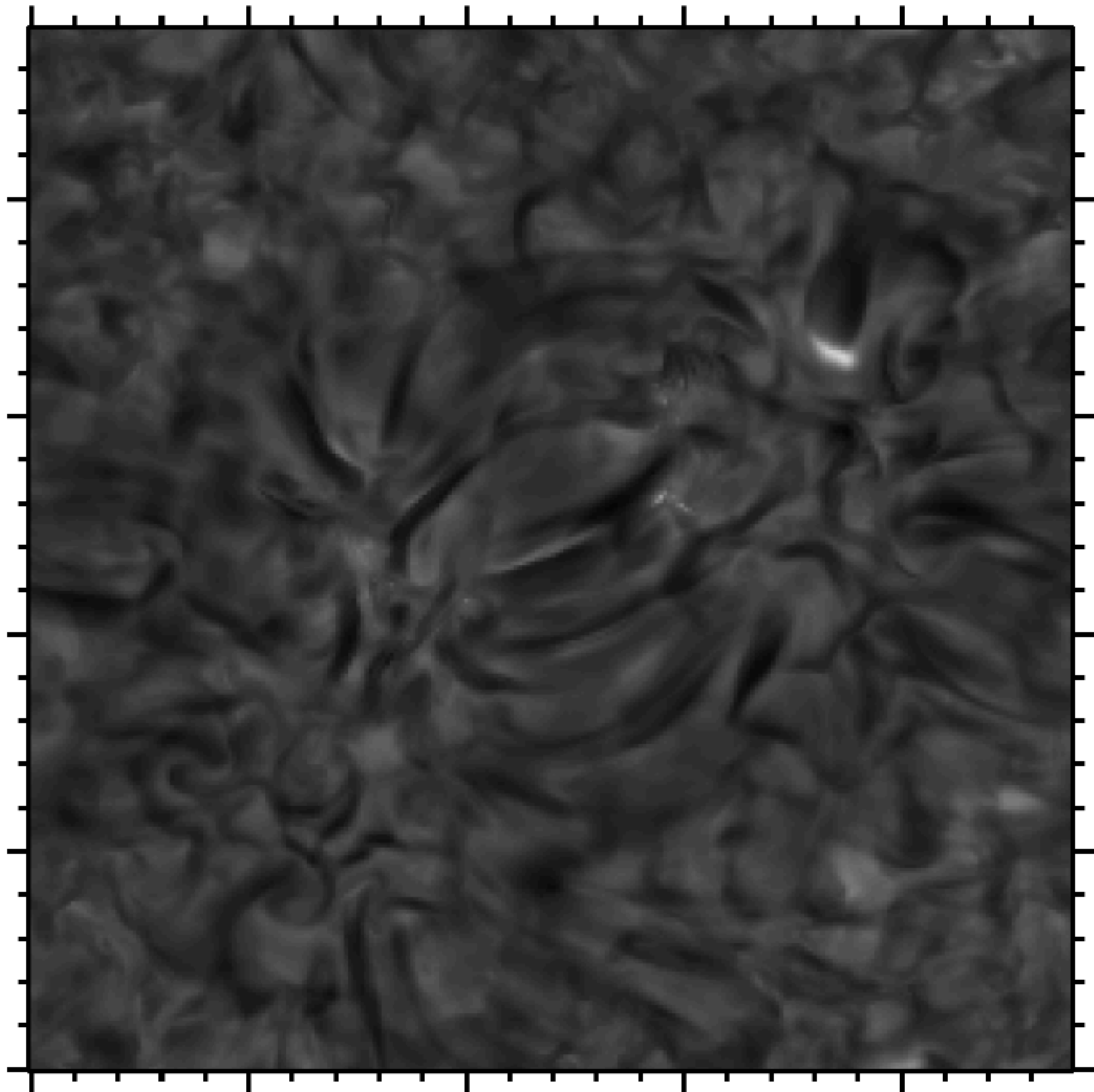


en024048_hion, $t=38.50$

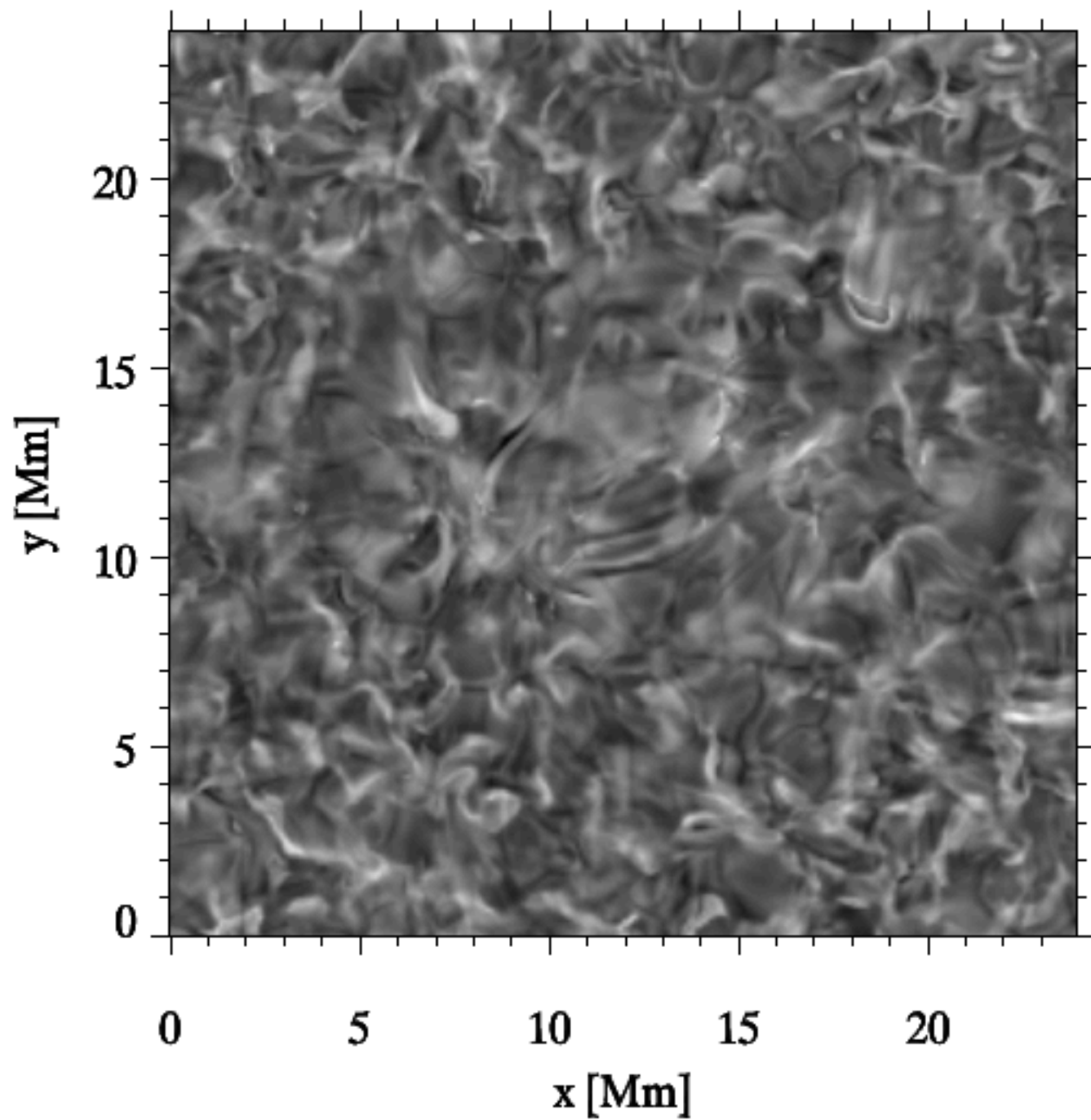
1D



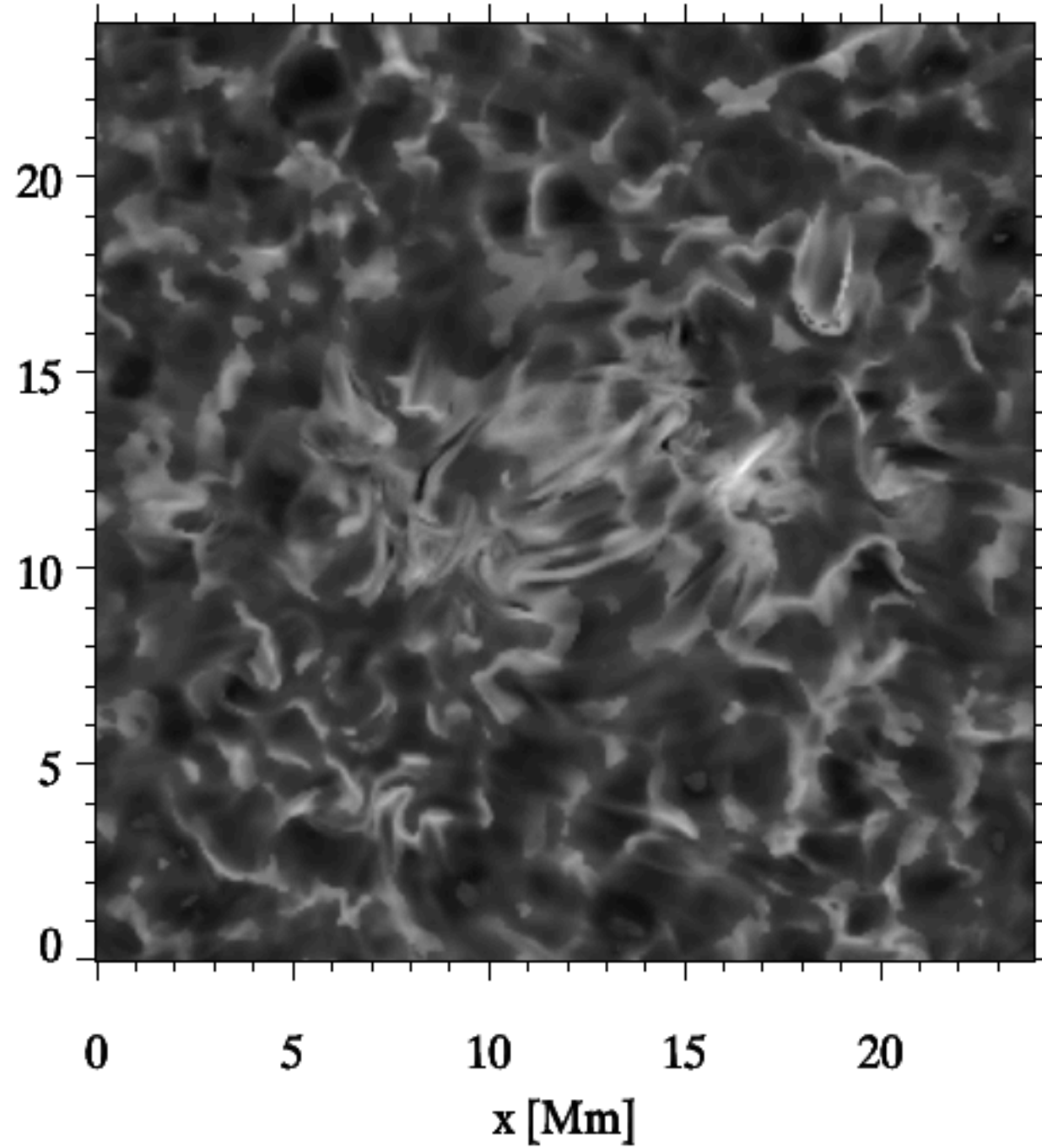
3D



Line width



T ($\tau=0.5-5$)

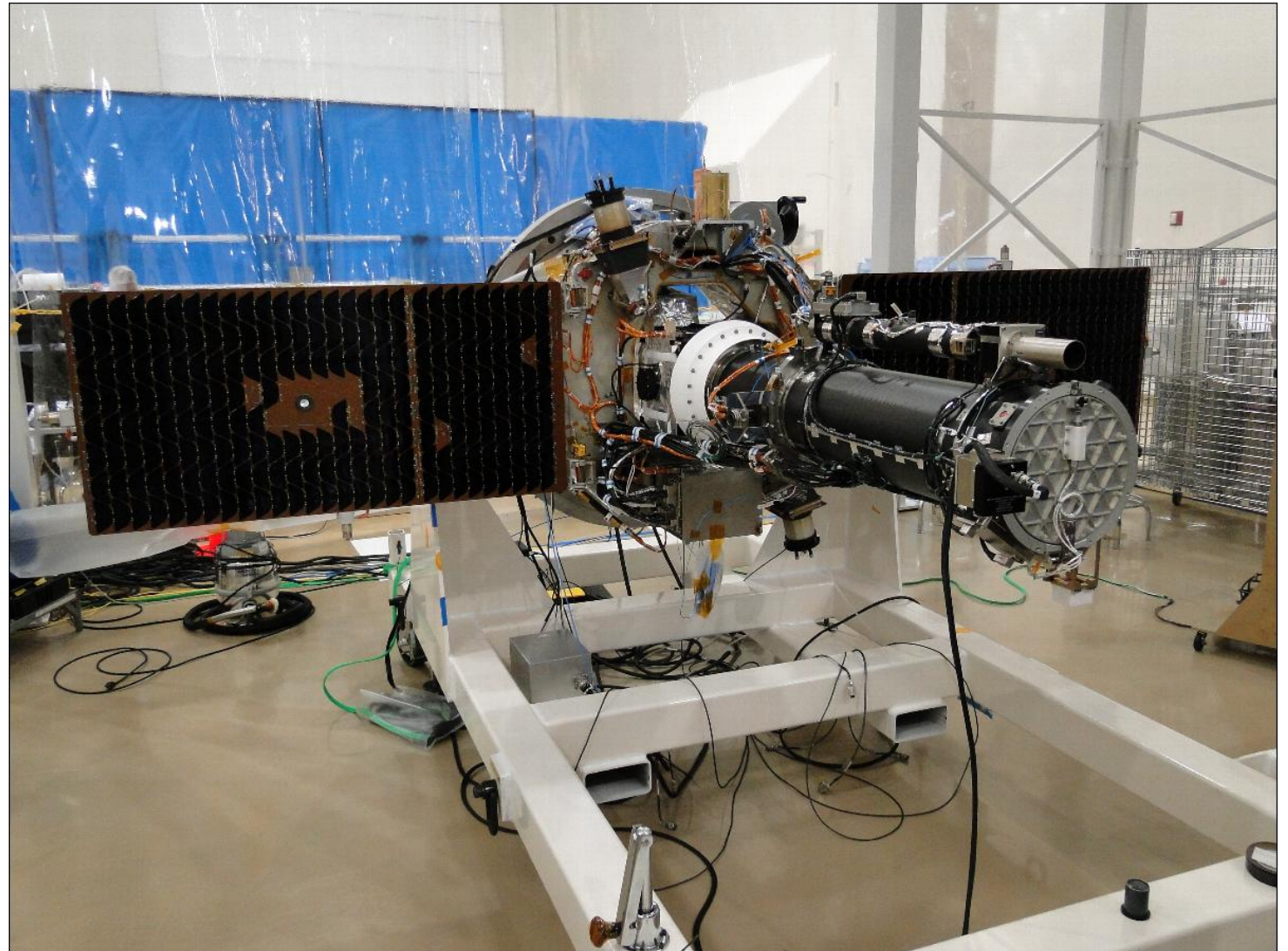




IRIS milestones and schedule

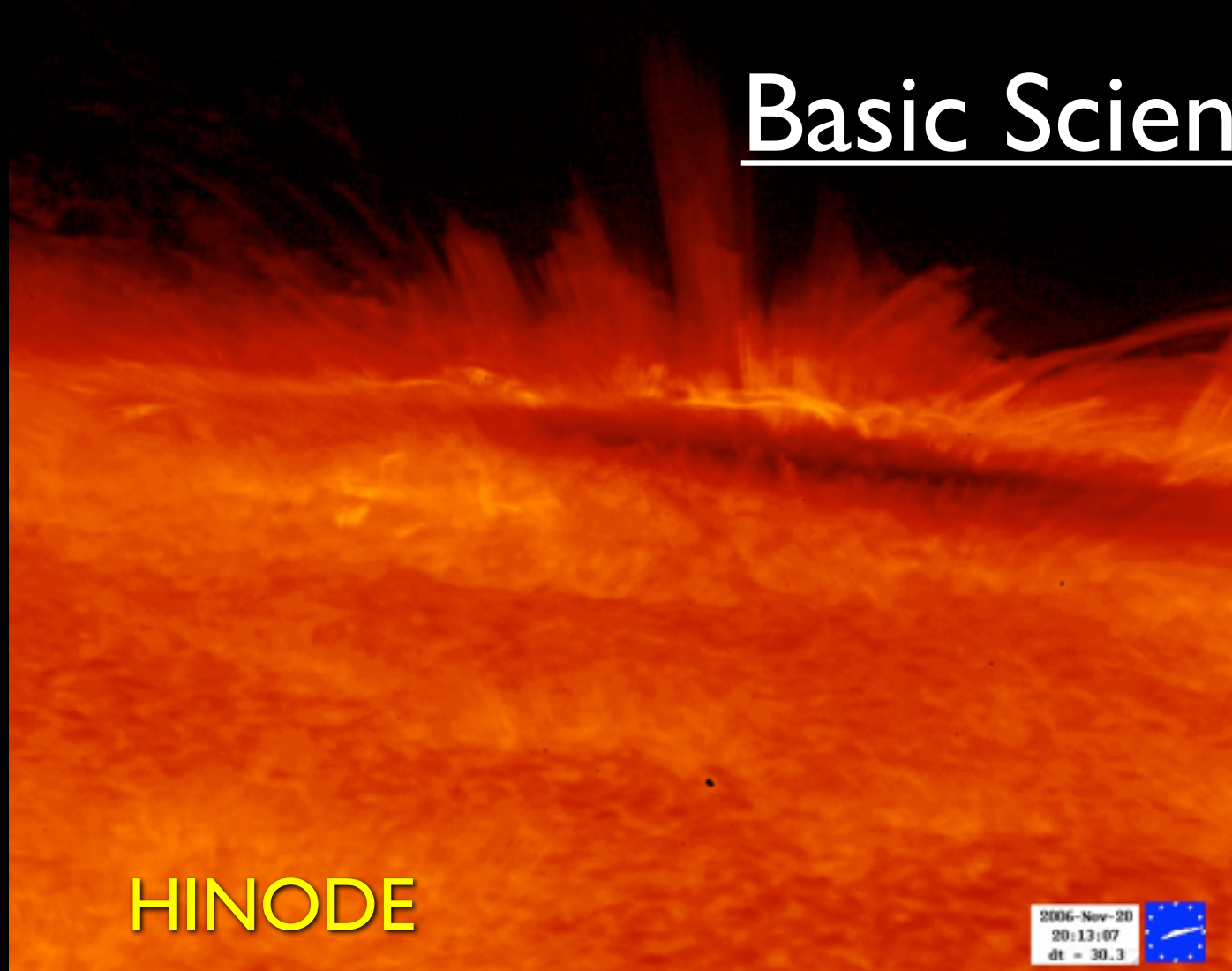
SMEX Announcement of Opportunity	Sep 2007
IRIS downselect, phase A	Jun 2008
IRIS concept study report (CSR) submittal	Dec 2008
IRIS site visit	Mar 2009
IRIS award	Jun 2009
IRIS bridge phase start (abbreviated	Aug 2009
Phase B start	Oct 2009
System Requirements Review (SRR)	Jan 2010
Preliminary Design Review (PDR)	May 2010
Critical Design Review (CDR)	Dec 2010
Mission Operations Review (MOR)	Dec 2011
Systems Integrations Review (SIR)	Jun 2012
Flight Operations Review (FOR)	Nov 2012
Launch	June 27 2013

IRIS

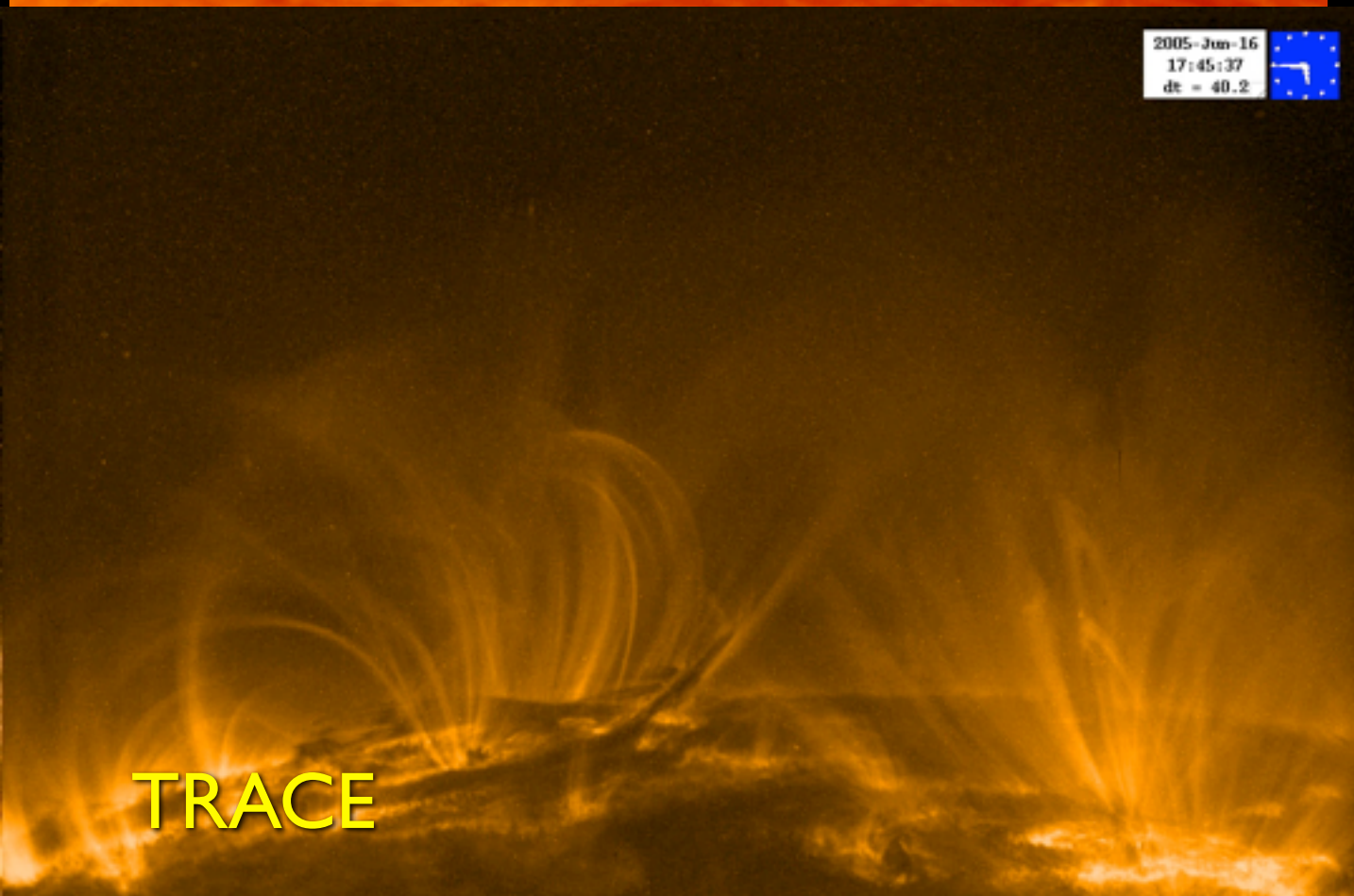


- NASA SMEX mission. Selected June 2009
- developed at LMSAL under the direction of PI Alan Title with major contributions from SAO, MSU, UiO, LSJU, NASA Ames and LMSES (spacecraft)
- 26 June 2013: Pegasus launch into Sun-synchronous polar orbit (620-670 km)

Basic Science Goals



HINODE



TRACE

- A. The types of non-thermal energy that dominate in the chromosphere and beyond.
- B. How the chromosphere regulates the mass and energy supplied to the corona and heliosphere.
- C. The ways that magnetic flux and matter rise through the lower atmosphere, and role of flux emergence in powering flares and mass ejections.

IRIS observables

UV slit-jaw Images

Si IV (65,000K)

C II (30,000K)

Mg II h/k (10,000K)

Mg II h/k wing (6,000K)

Realistic Radiative

3D MHD models...

...to guide interpretation

UV Spectra

Far-UV 12.5 mÅ pixels

Near-UV 25 mÅ pixels

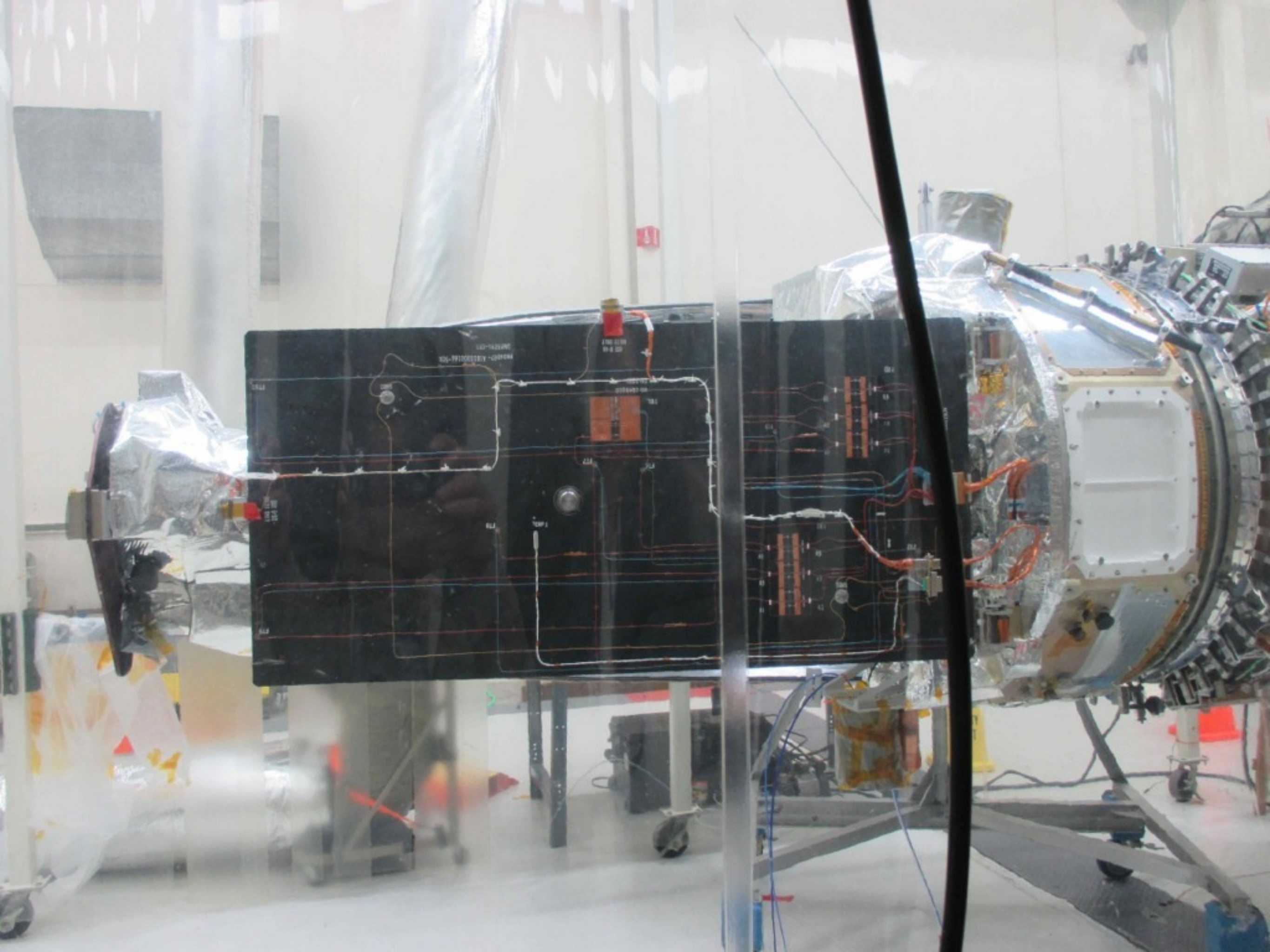
20 cm UV telescope:

1/6 arcsec pixels

Observable	Wavelength range (Å)	Spectral Dispersion (mÅ)	Spectral Resolution	Spatial range (arcsec)	Spatial pixel size (arcsec)	Spatial Resolution (arcsec)	Effective Area (cm ²)
Spectrograph FUV 1	1331.6-1358.4	12,98	28-33mÅ	0.33x175	0,16	0,33	2,1
Spectrograph FUV 2	1380.6-1406.8	12,72	28-33mÅ	0.33x175	0,16	0,33	2,5
Spectrograph NUV	2782.6-2833.9	25,46	55-80mÅ	0.33x175	0,16	0,4	0,27
Slitjaw C II	1335		40Å	175 x 175	0,16	0,33	0,6
Slitjaw Si IV	1400		40Å	175 x 175	0,16	0,33	0,6
Slitjaw Mg II h/k	2796		4Å	175 x 175	0,16	0,4	0,007
Slitjaw Mg II wing	2830		4Å	175 x 175	0,16	0,4	0,006

2790 2800 2810 2820 2830









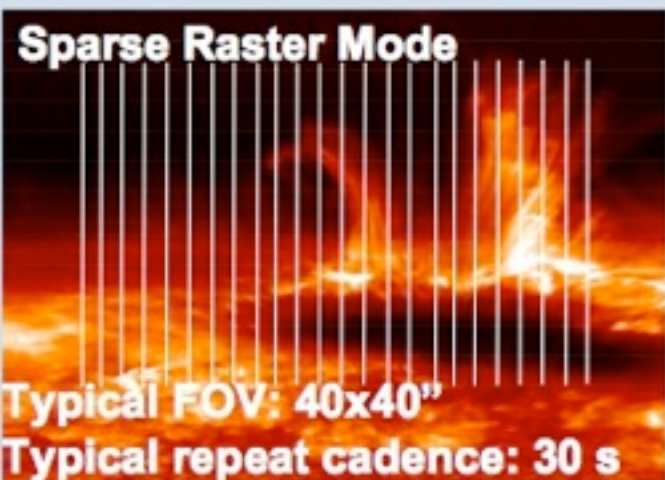
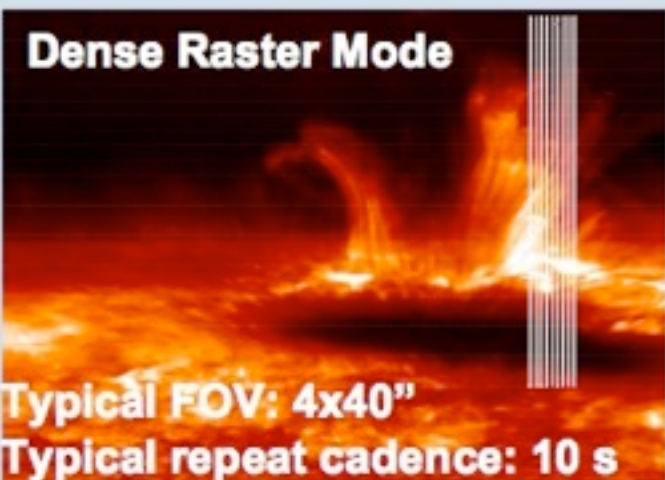
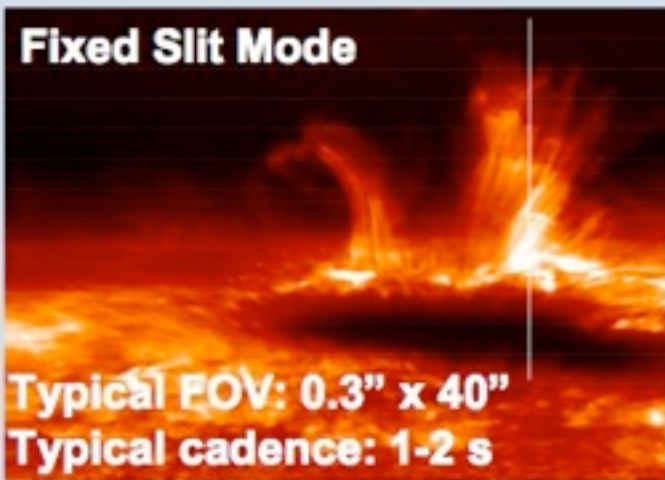
Pegasus/WIRE Mission
March 4, 1999

Presented To:
VAFB Operations

For Your Dedication to Total Mission Success



IRIS spectra and slit-jaw imaging cover the photosphere, chromosphere, transition region and corona - 4,500 to 10,000,000 K



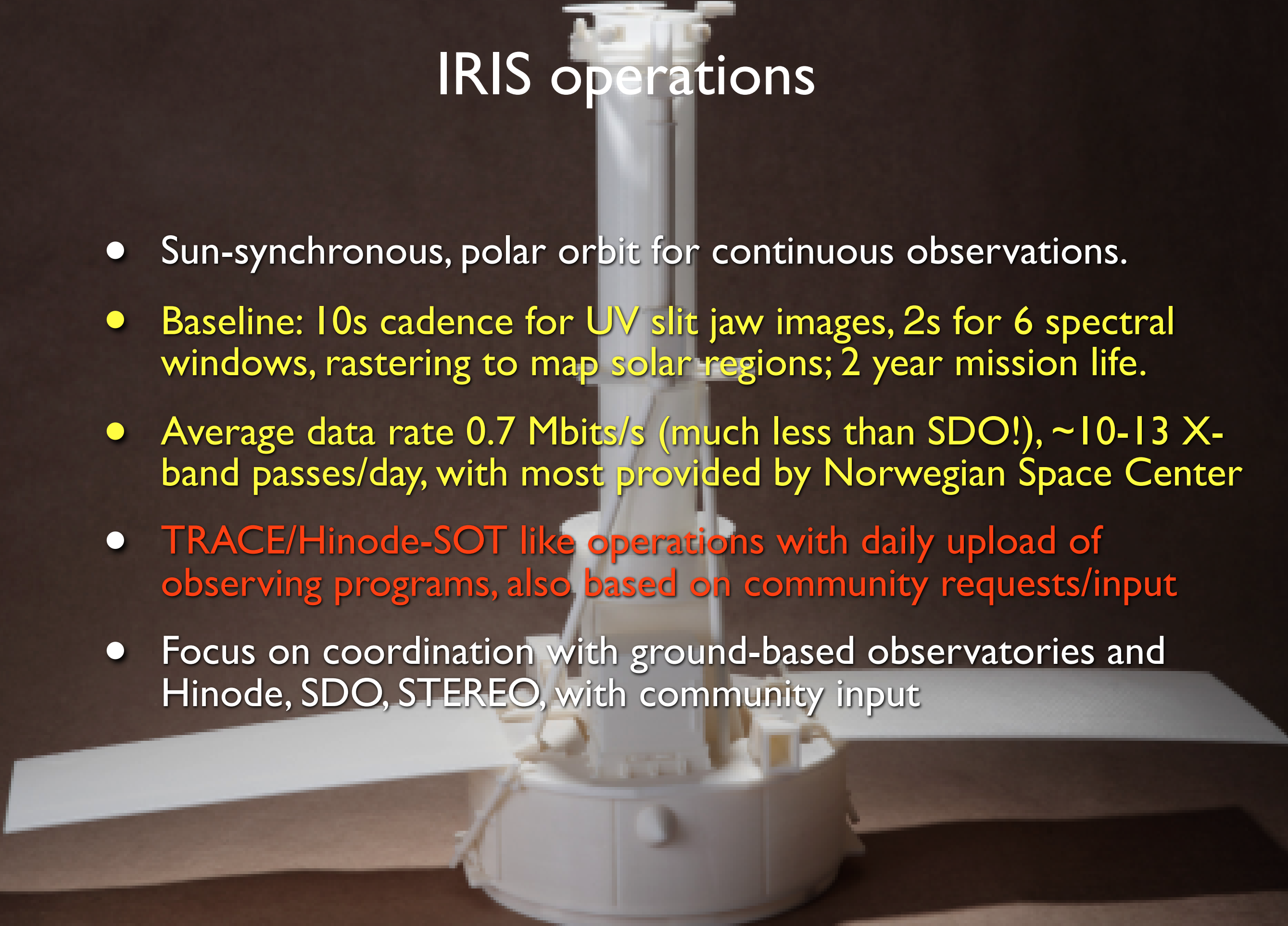
Ion Spectrum	λ	$\Delta\lambda$	Log T	Estimated Count Rate (e-/s/line/spatial pixel)			Detector
	Å	mÅ	K	Quiet Sun	Active Region	Flare	
UV Spectra (effective area 2.1-2.4 cm ² for FUV, 0.27 cm ² for Mg passband, continuum is 1 Å) †: Count rates for Mg II wing, h and k are in e-/s/spectral pixel/spatial pixel							
Mg II wing	2820	25	3.7-3.9	3800 [†]	13500 [†]	13500 [†]	3
O I	1356	12.5	3.8	70	190	480	1
Mg II h	2803	25	4.0	1500 [†]	5800 [†]	22000 [†]	3
Mg II k	2796	25	4.0	1900 [†]	7800 [†]	16000 [†]	3
C II	1335	12.5	4.3	780	5000	52000	1
C II	1336	12.5	4.3	1070	6600	64000	1
Si IV	1403	12.5	4.8	220	4000	4e6	2
Si IV	1394	12.5	4.8	490	8000	1e7	2
O IV	1401	12.5	5.2	60	300	5e5	2
O IV	1400	12.5	5.2	15	90	1e5	2
Fe XII	1349	12.5	6.2	23	60	580	1
Fe XXI	1354	12.5	7.0	10	45	5e4	1
UV Slit-Jaw Images				Estimated Count Rate (e-/s/pixel)			
Effective area 0.006 cm ² with 4 Å FWHM filter for Mg II; 0.6 cm ² with 40 Å FWHM for far-UV.							
Mg II wing	2831		3.7-3.9	3600	8200	8200	4
Mg II k	2796		4.0	900	4200	10000	4
C II	1335		4.3	650	2100	21000	4
Si IV	1400		4.8	500	2000	4e5	4

IRIS data



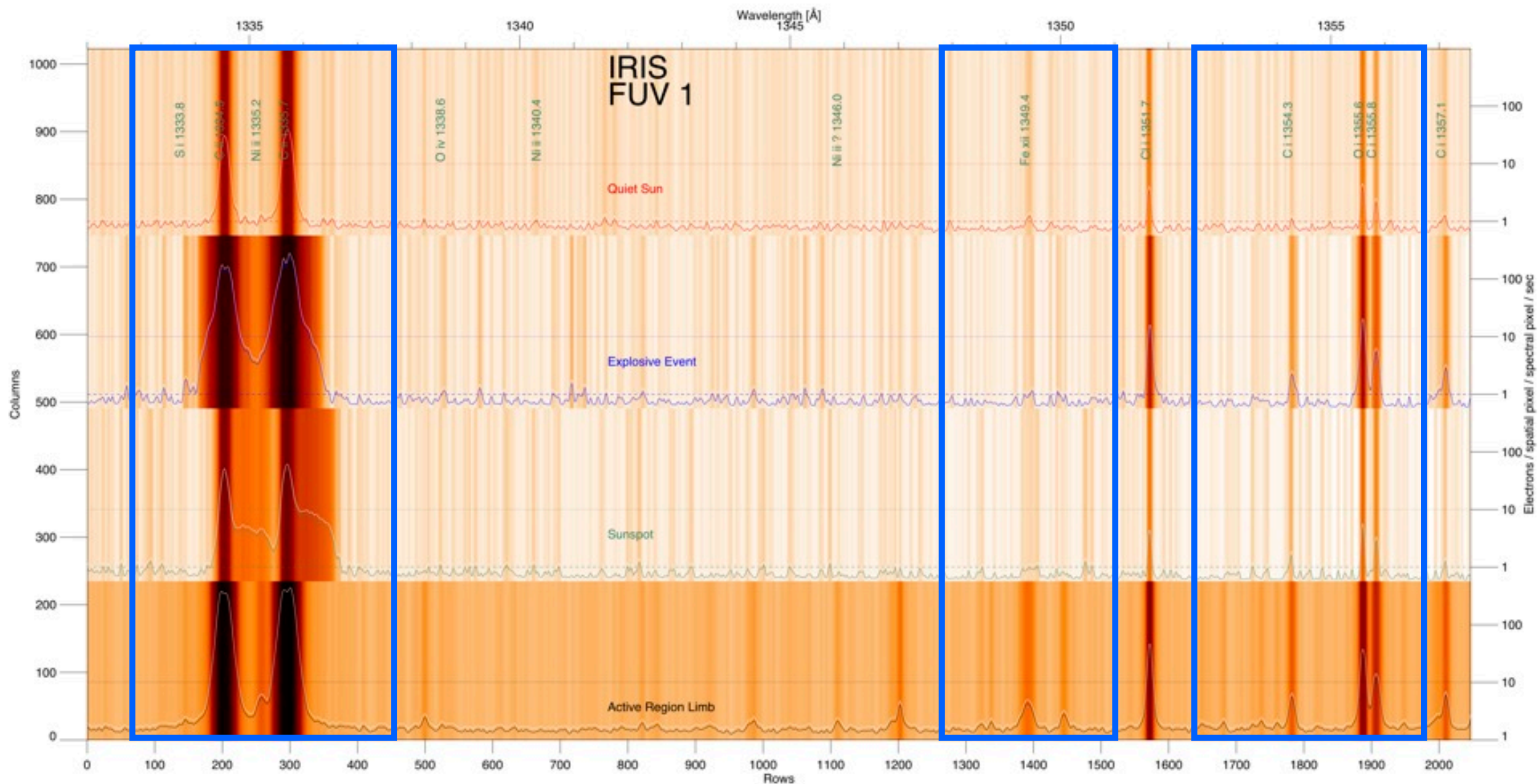
- Public data policy (see TRACE/SDO): IRIS observations are available within a day of observing
- IRIS data are available from SDO/JSOC and included in the Hinode data center in Oslo
- Quicklook software tailored for IRIS data are available in solarsoft
- IRIS data center:
 - includes IRIS data at level2
 - makes available several numerical simulations (physical variables) and synthetic IRIS observables (both optically thick and thin) for various magnetic field configurations
 - will include whatever high-quality, co-aligned ground-based datasets that are obtained during IRIS-led coordinated campaigns

IRIS operations

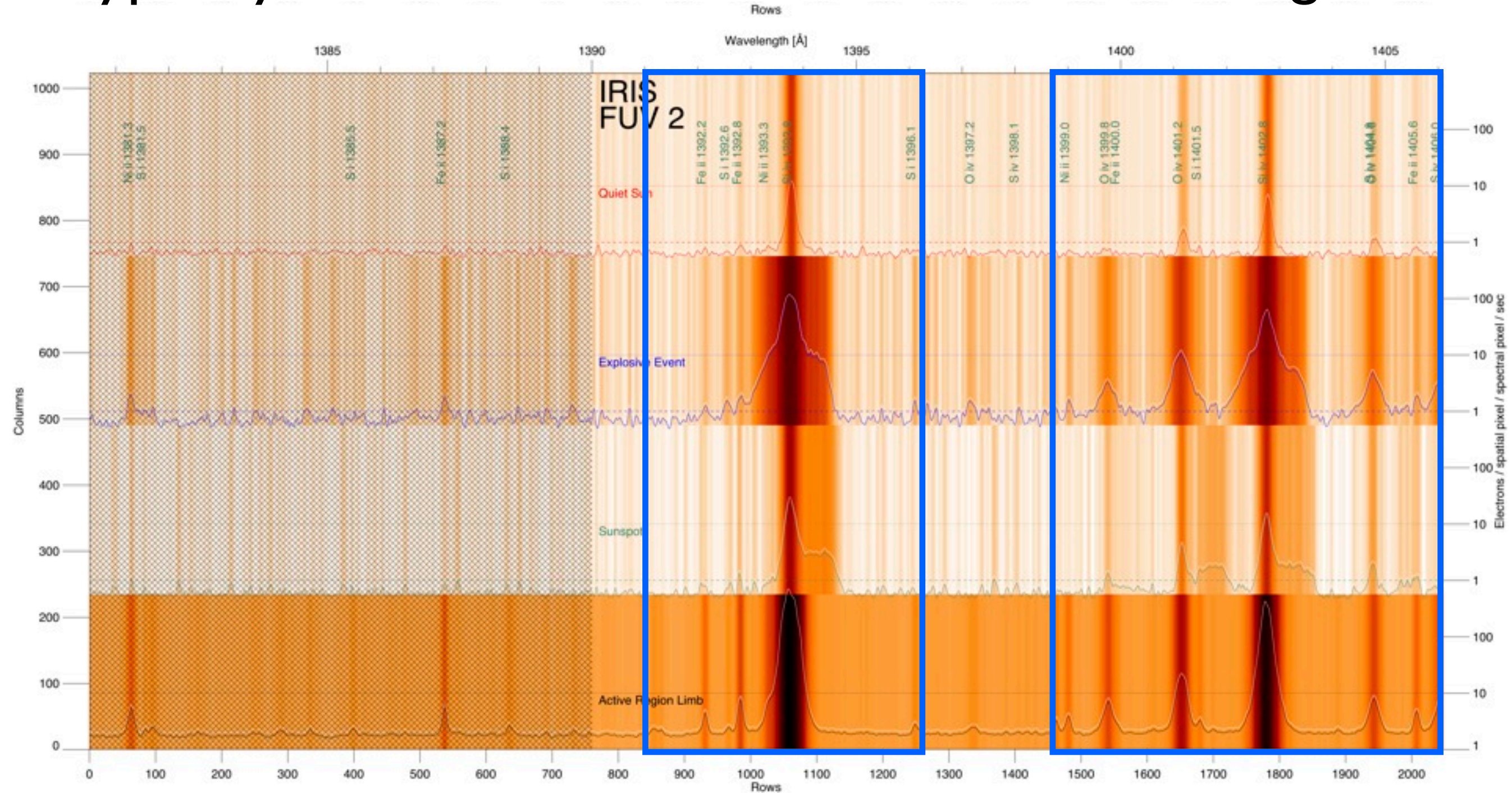


- Sun-synchronous, polar orbit for continuous observations.
- Baseline: 10s cadence for UV slit jaw images, 2s for 6 spectral windows, rastering to map solar regions; 2 year mission life.
- Average data rate 0.7 Mbits/s (much less than SDO!), ~10-13 X-band passes/day, with most provided by Norwegian Space Center
- TRACE/Hinode-SOT like operations with daily upload of observing programs, also based on community requests/input
- Focus on coordination with ground-based observatories and Hinode, SDO, STEREO, with community input

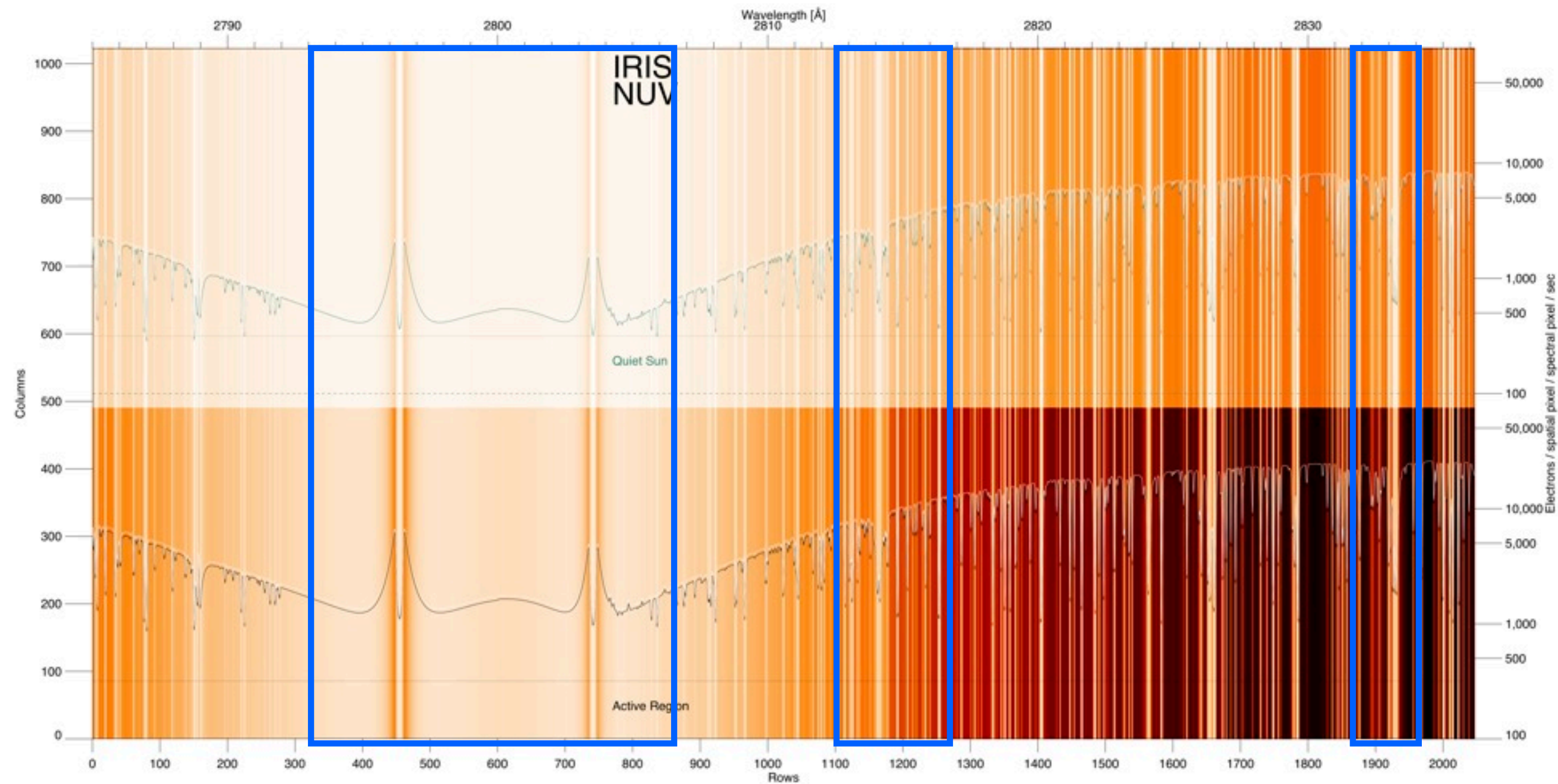
IRIS will rarely read out **full** FUV spectra:
typically 4-6 3-4Å wide windows focused on bright lines

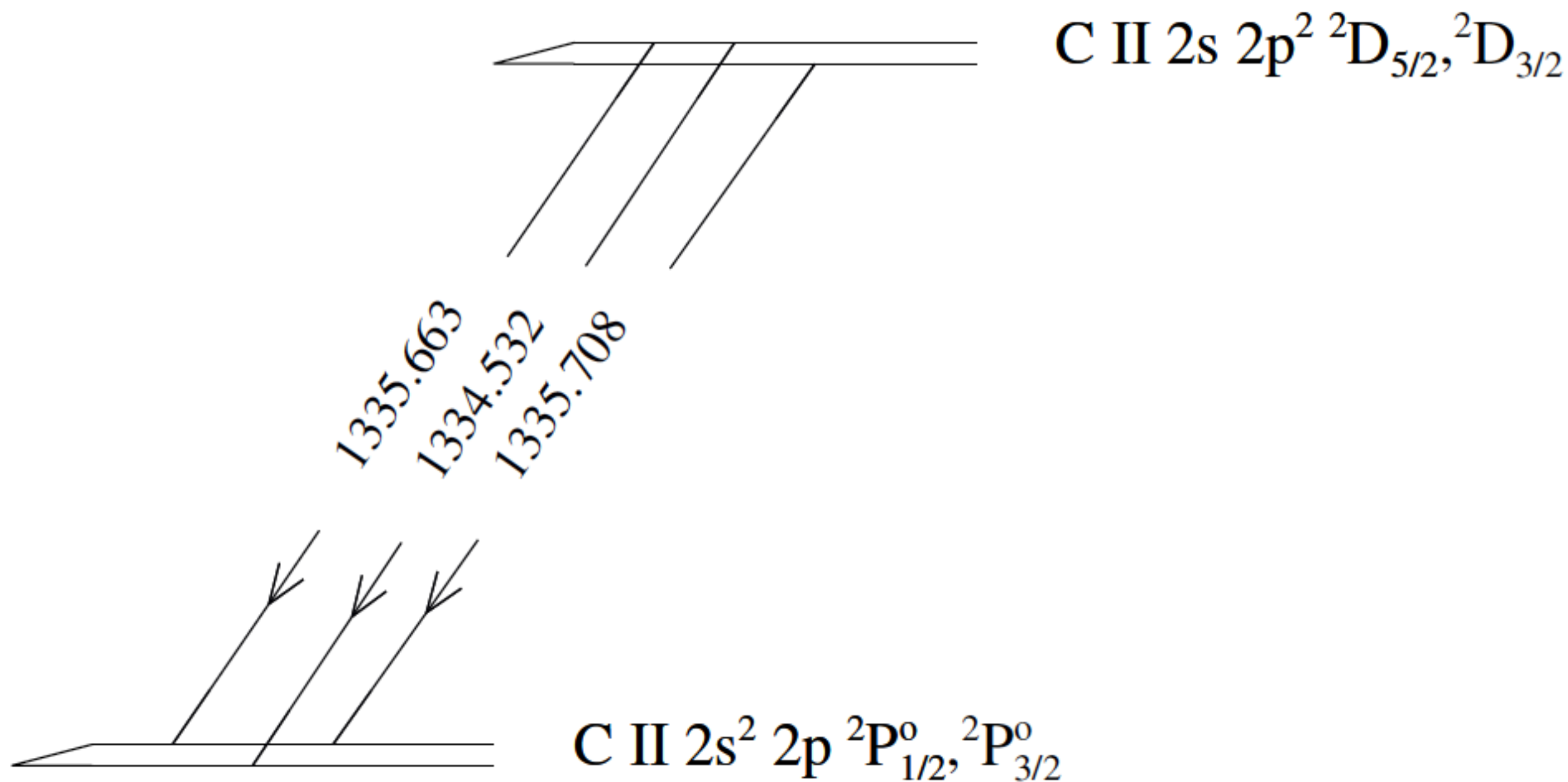


IRIS will rarely read out **full** FUV spectra:
typically 4-6 3-4Å wide windows focused on bright lines

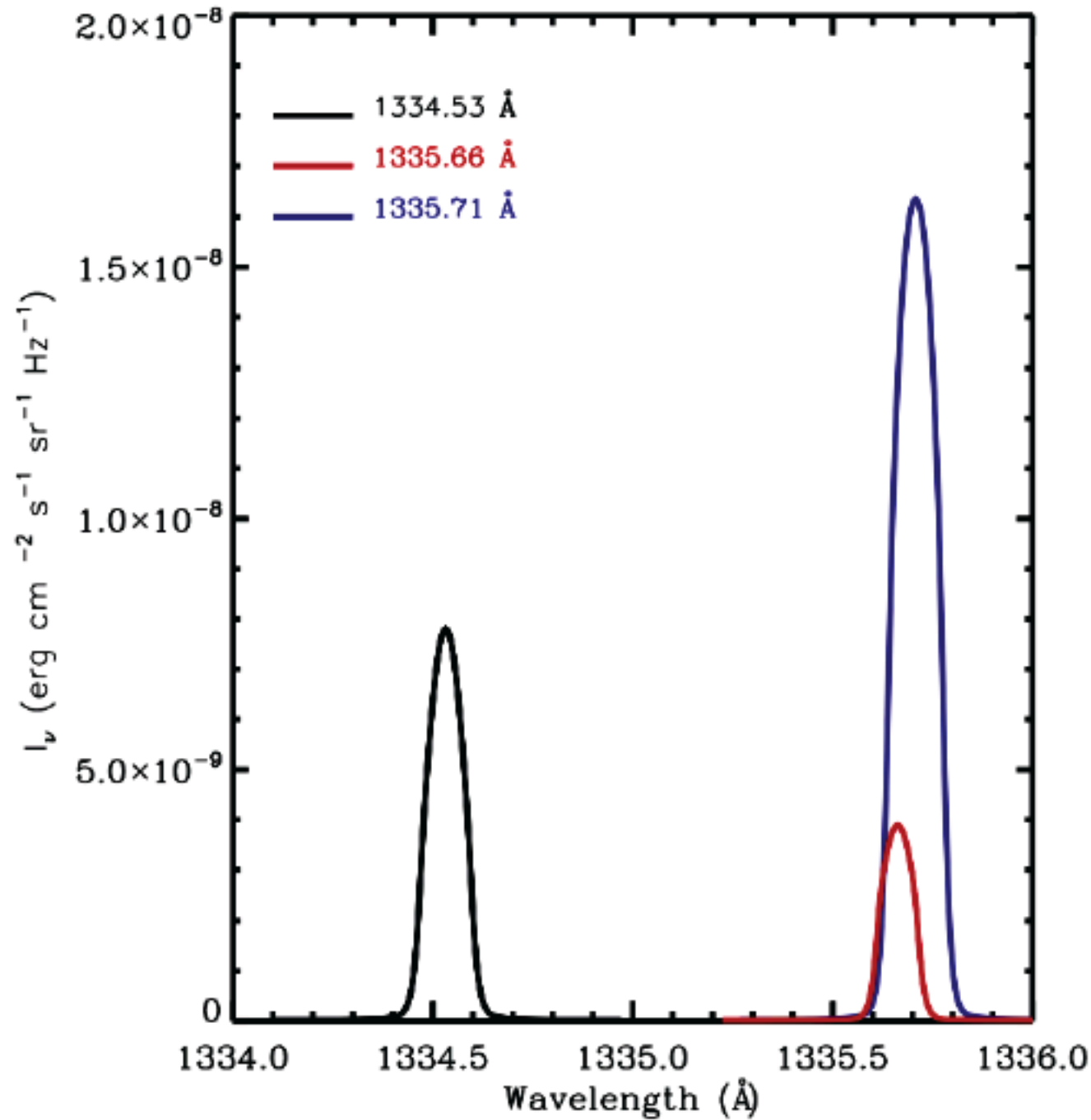


IRIS will rarely read out **full** NUV spectra: typically 2-3 2-13Å wide windows focused on regions of interest





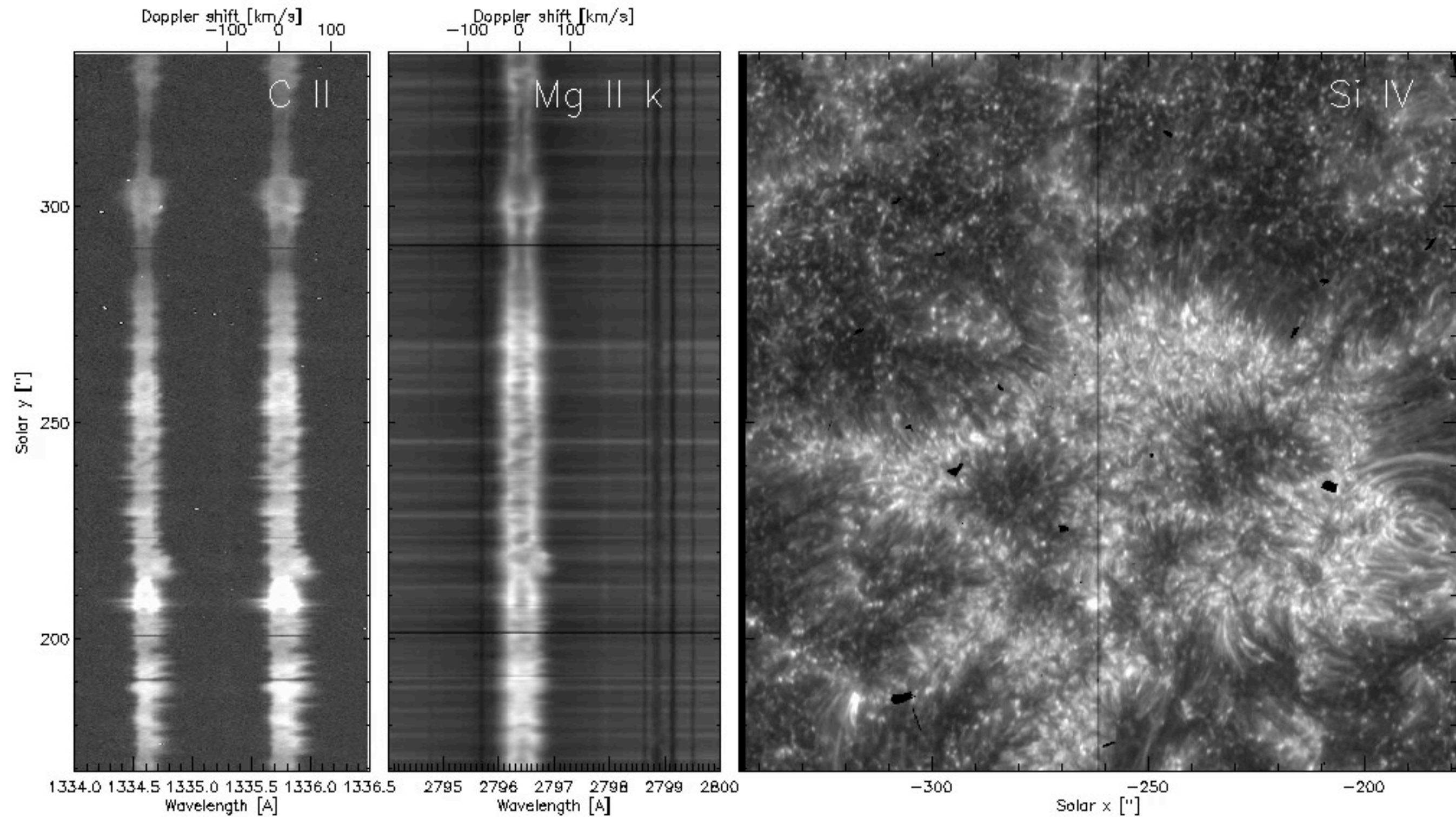
C II 1335 multiplet



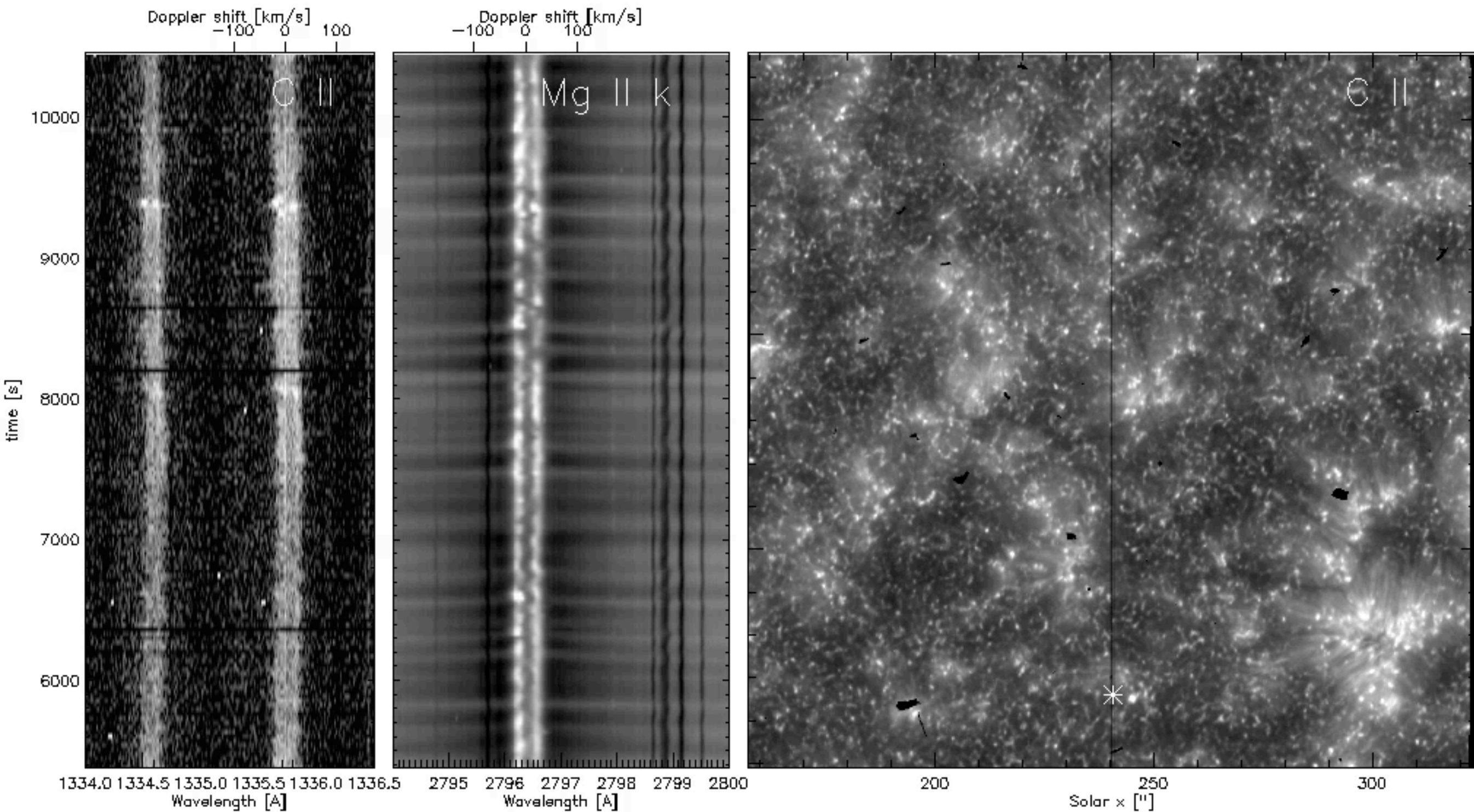
Wavelength ($\text{\AA}$)	J_u	J_l	gf
1334.5323	3/2	1/2	0.257
1335.6625	3/2	3/2	0.0512
1335.7077	5/2	3/2	0.464

IRIS observations

30s exposures, 400 step raster

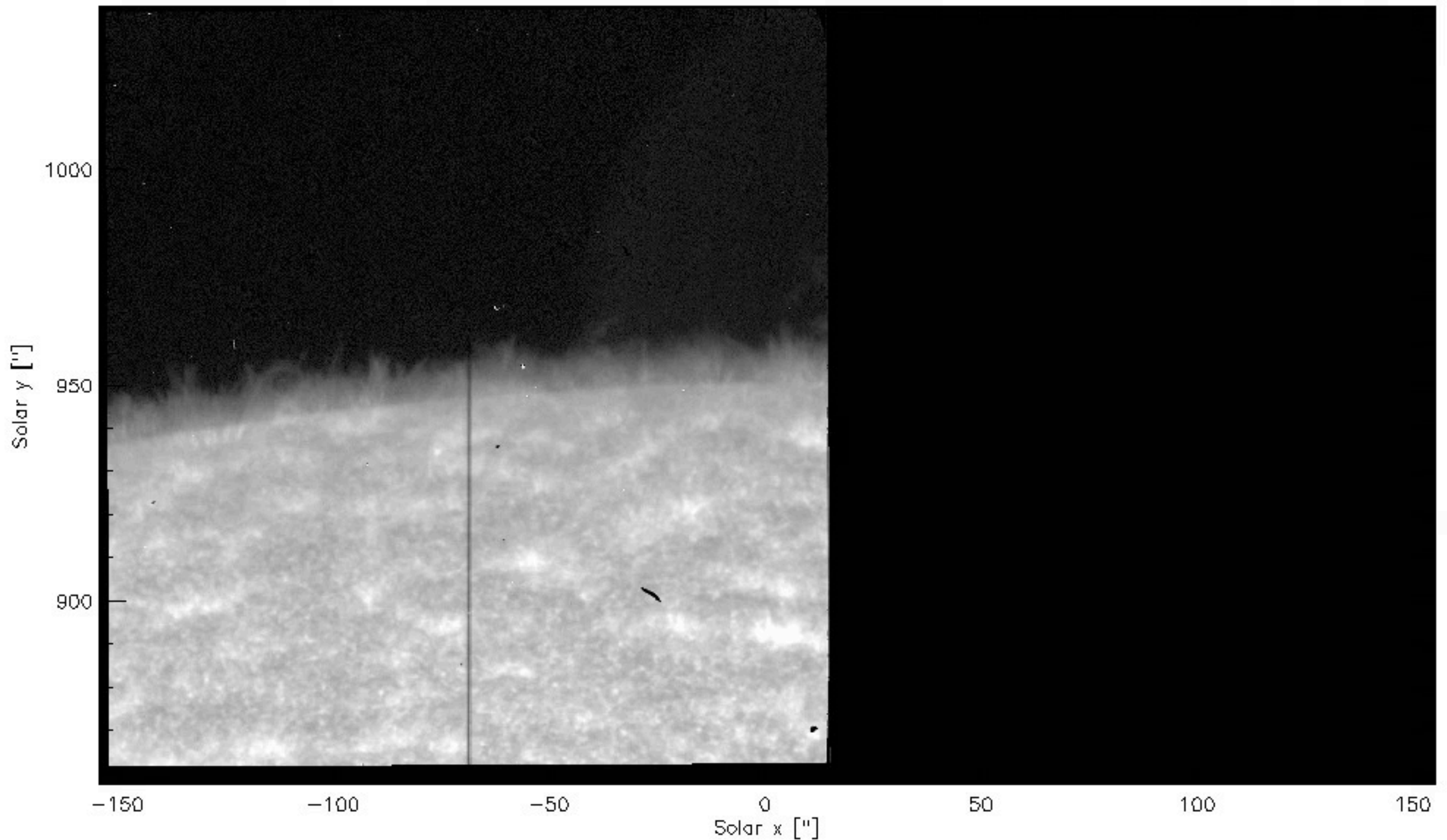


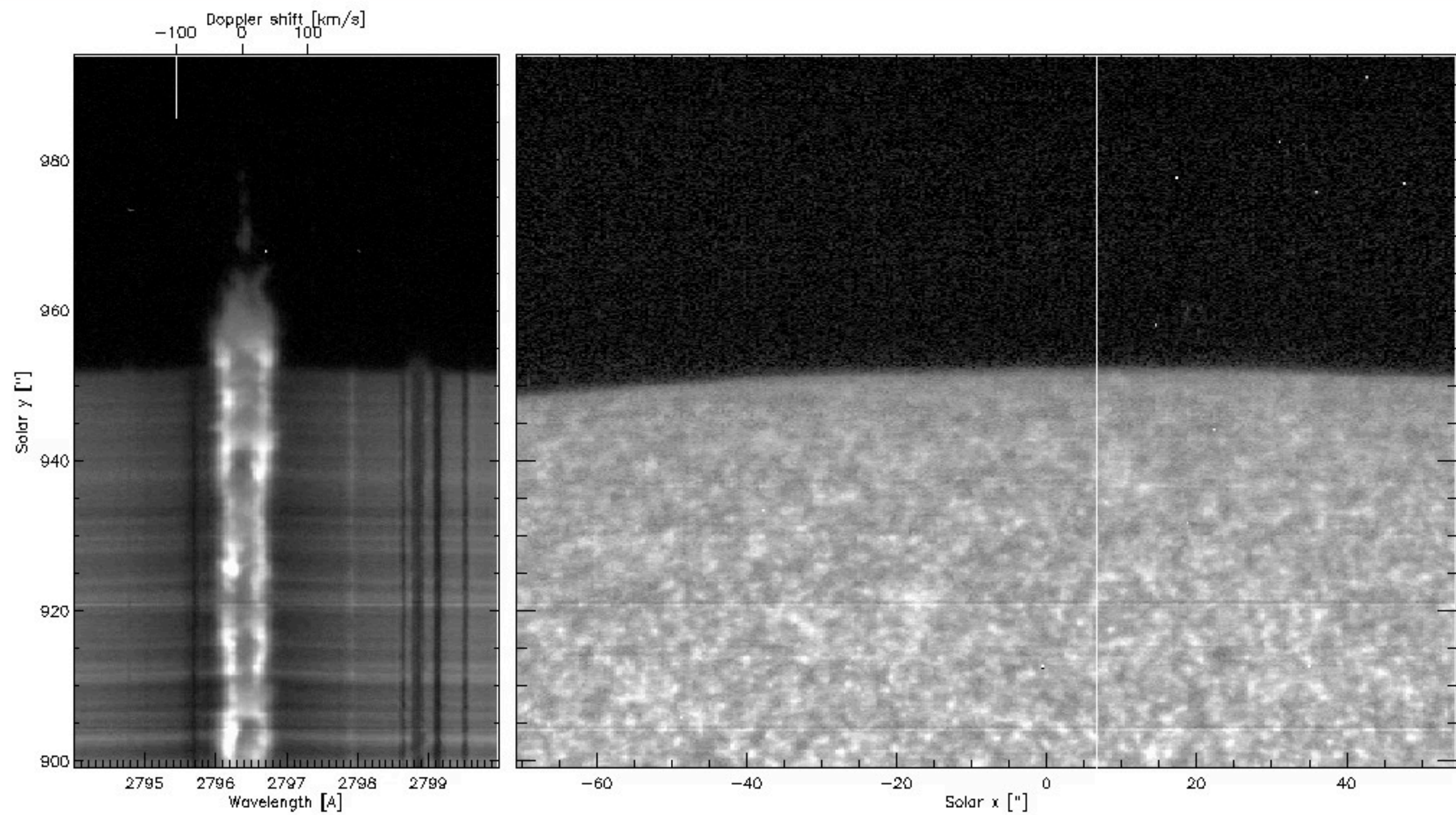
Temporal behaviour



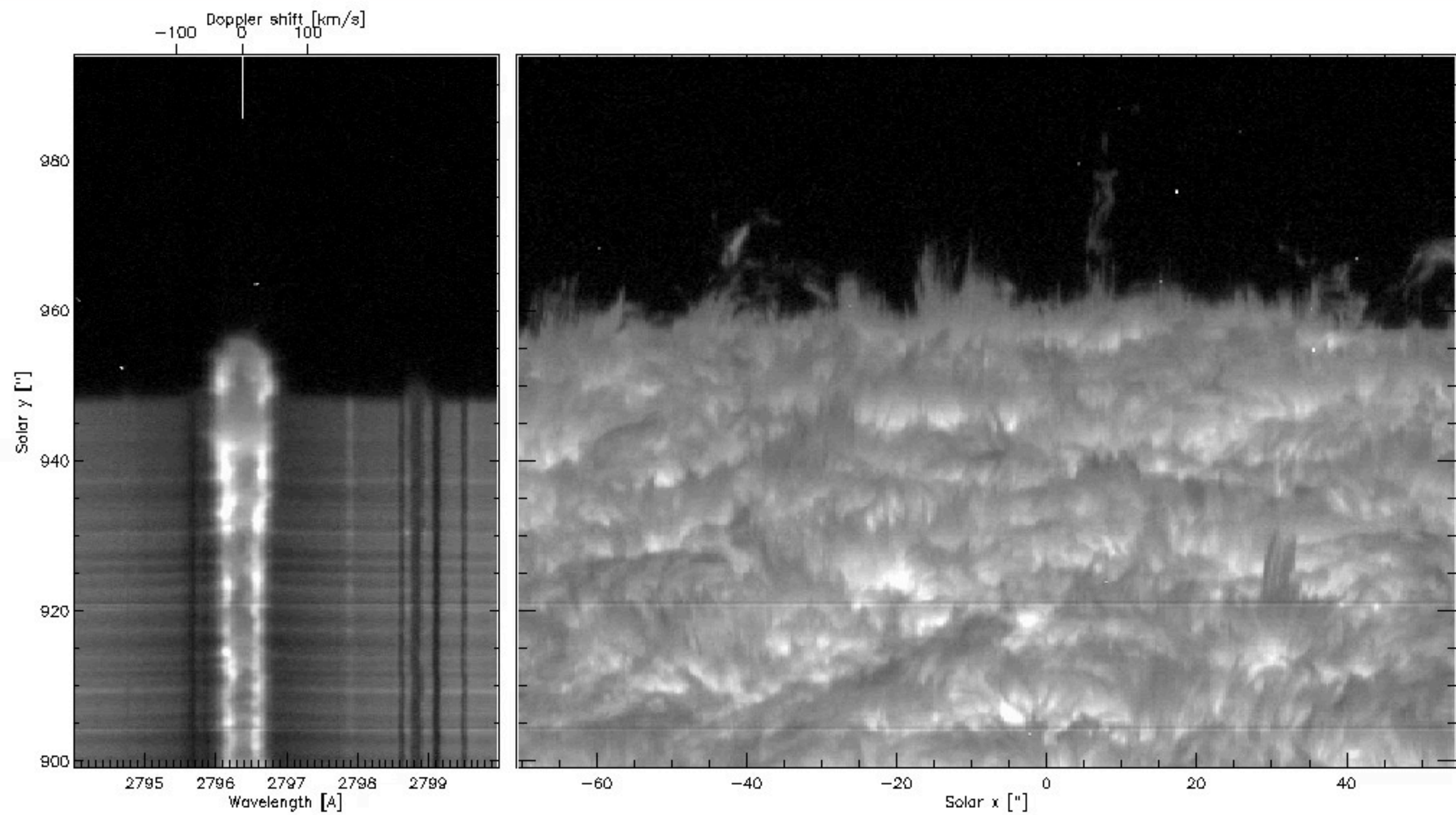
Diagnostics of spicules

8s exposures, 400 step raster, 9s between raster steps





20131009_131001_3800259146



20131009_131001_3800259146

Mg II 280nm diagnostics

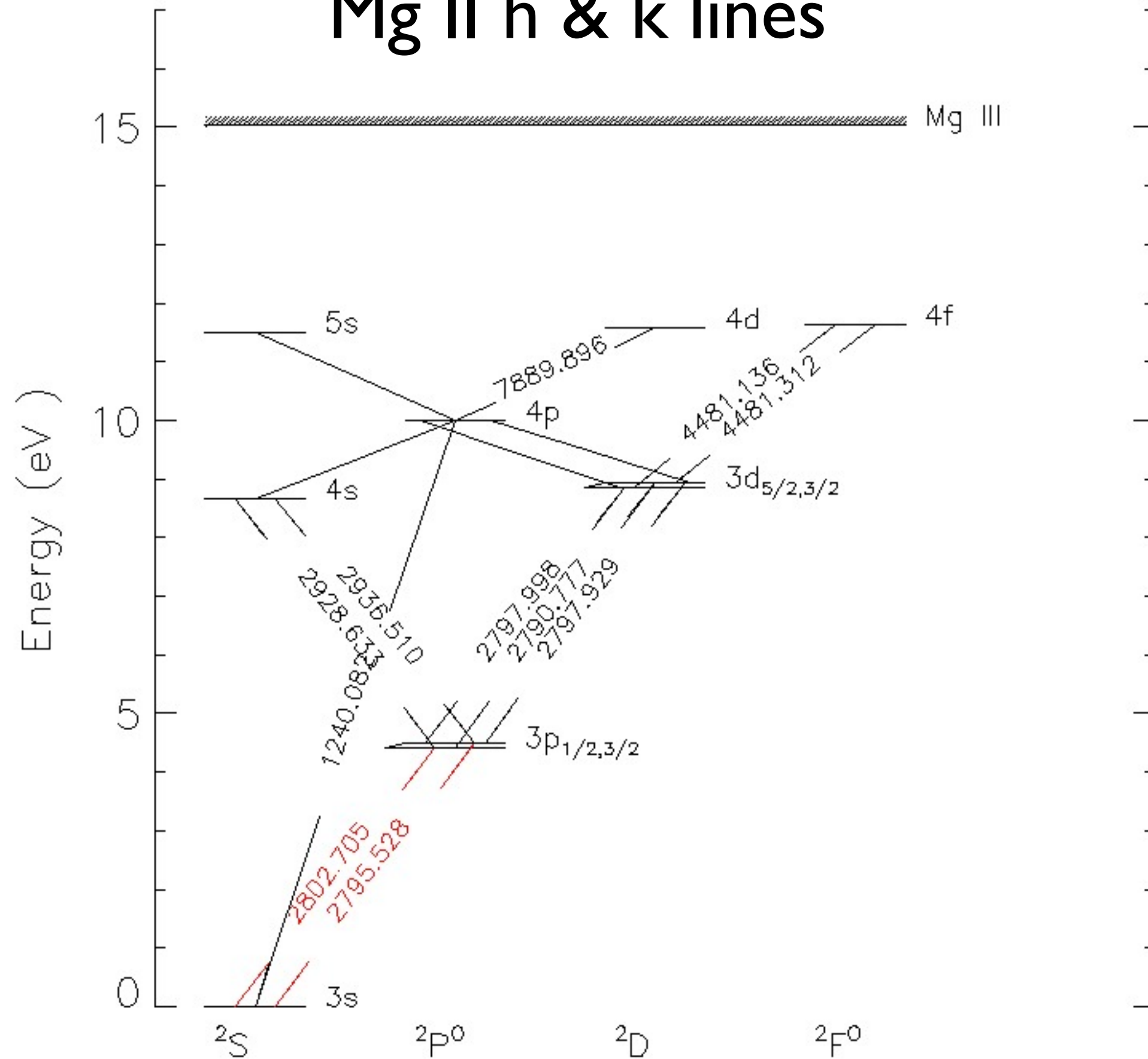
Recent papers (2013)

Leenaarts, Pereira, Carlsson, Uitenbroek, De Pontieu (in various permutations):

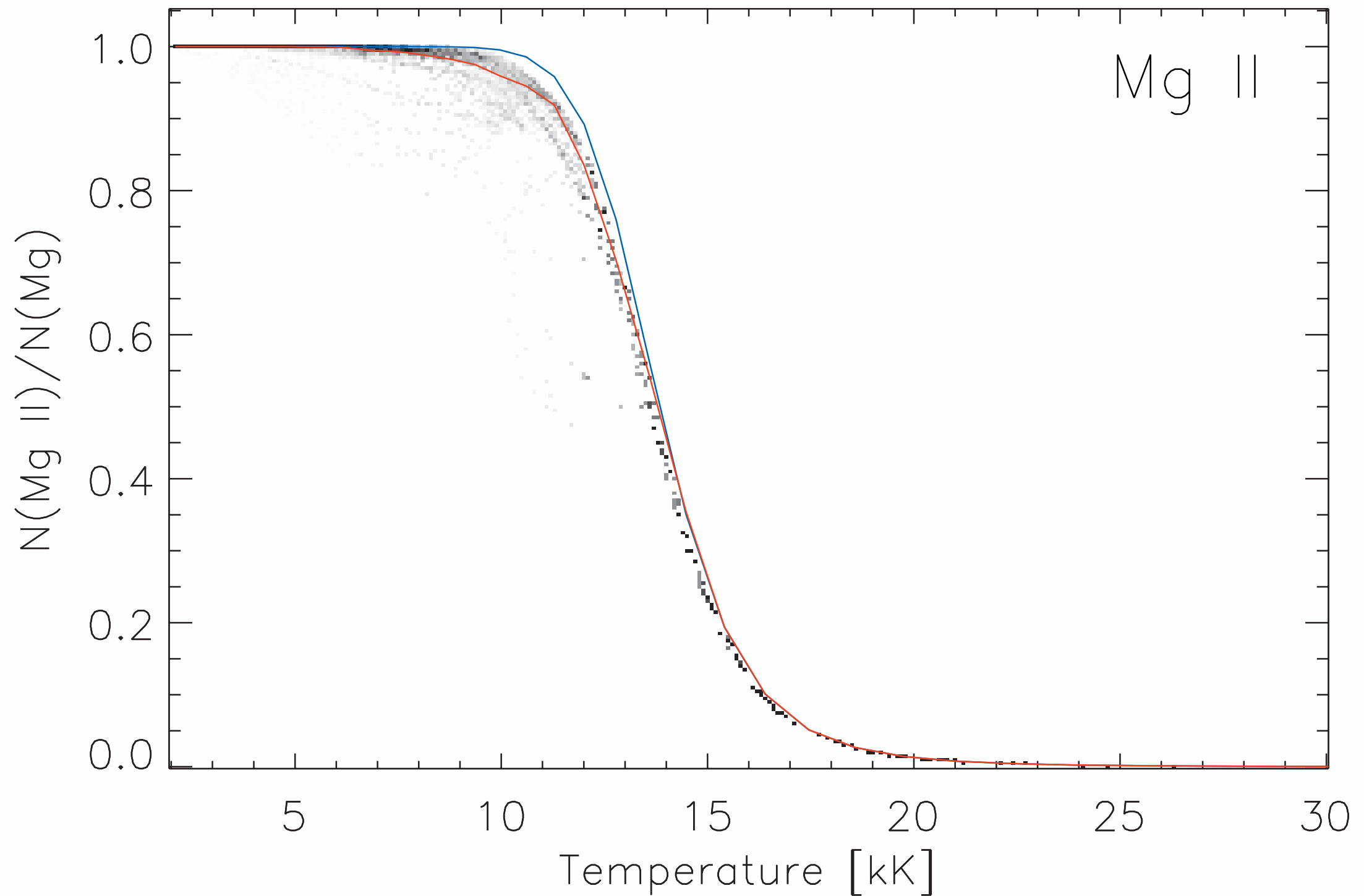
The Formation of IRIS Diagnostics:

- I. A Quintessential Model Atom of Mg II and General Formation Properties of the Mg II h&k Lines
- II. The Formation of the Mg II h&k Lines in the Solar Atmosphere
- III. NUV Spectra and Images

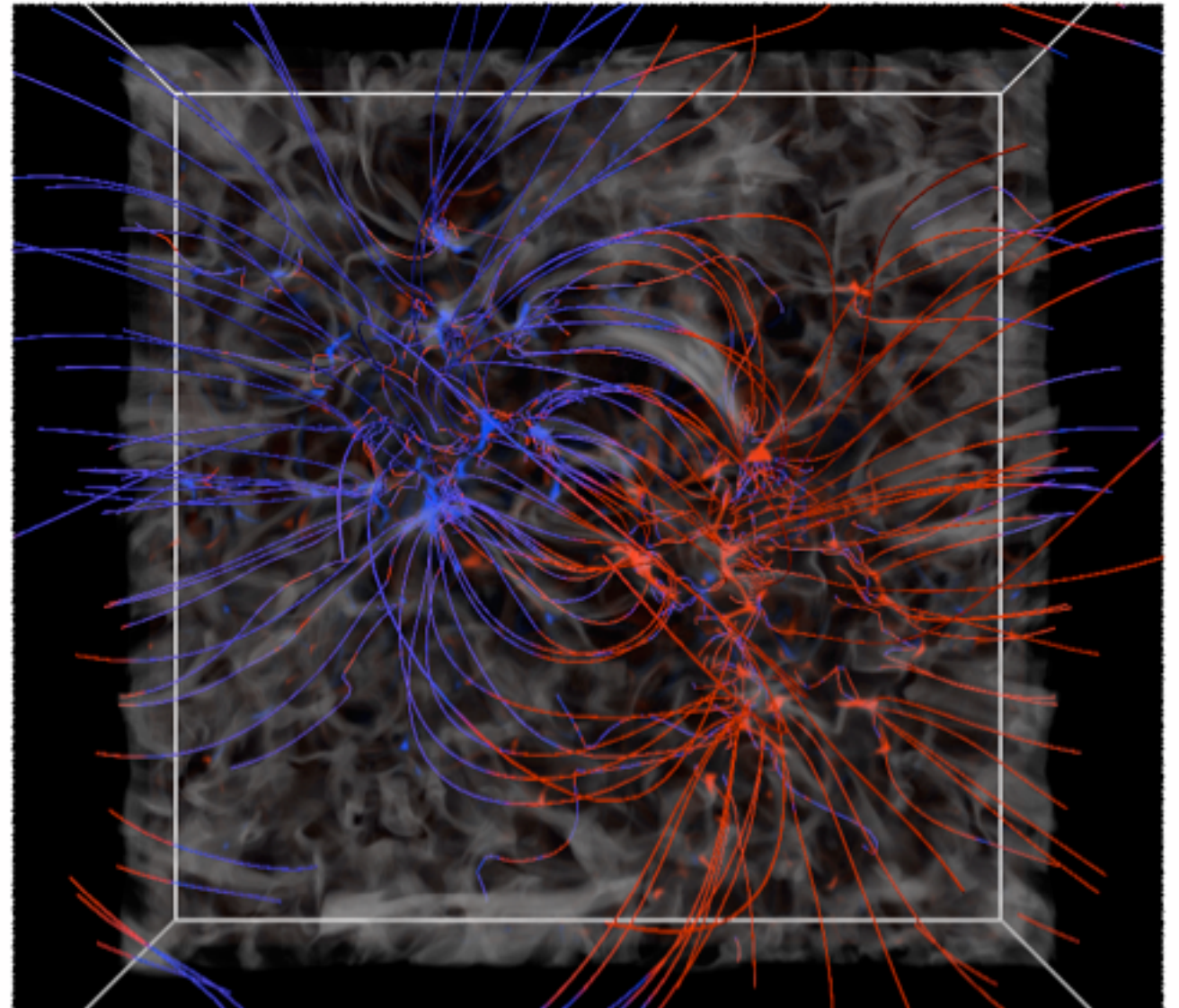
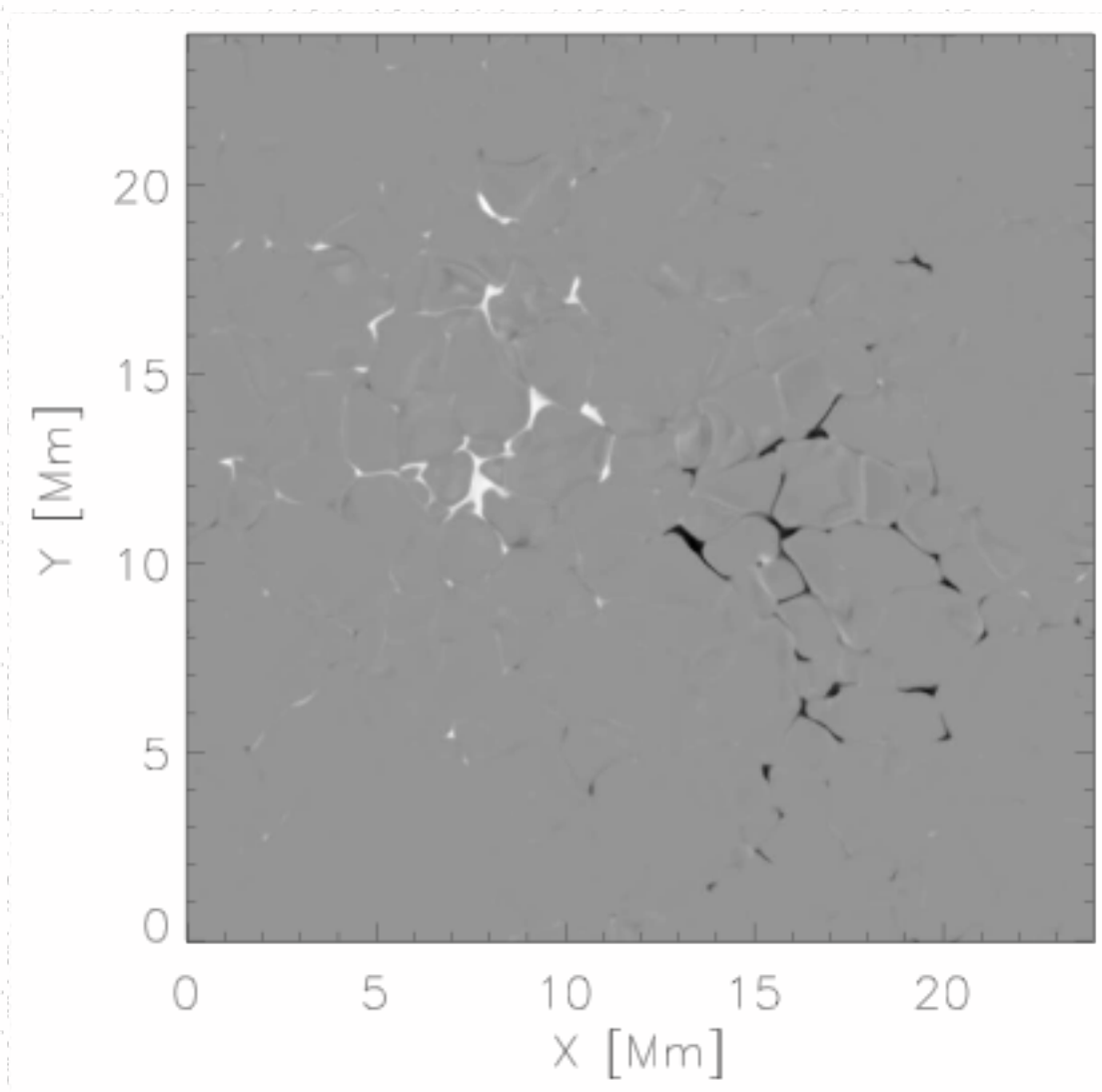
Mg II h & k lines



Mg has 18 times the abundance of Ca
formed 3 scale-heights higher up

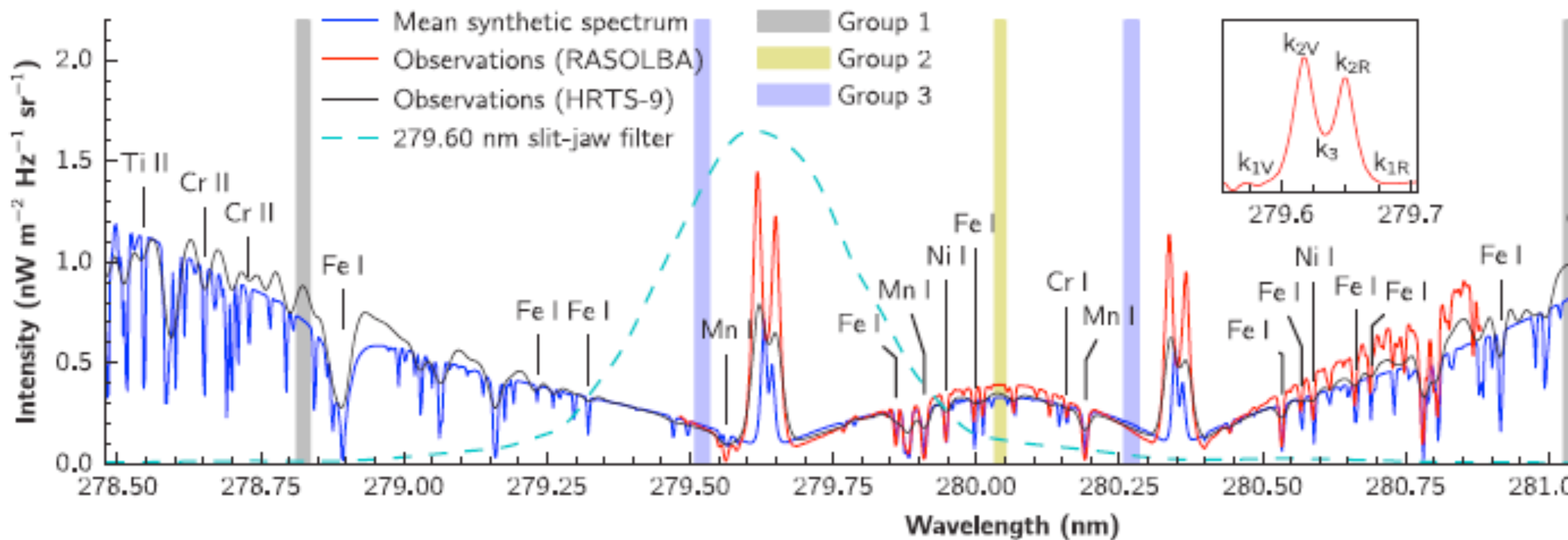


Bifrost model

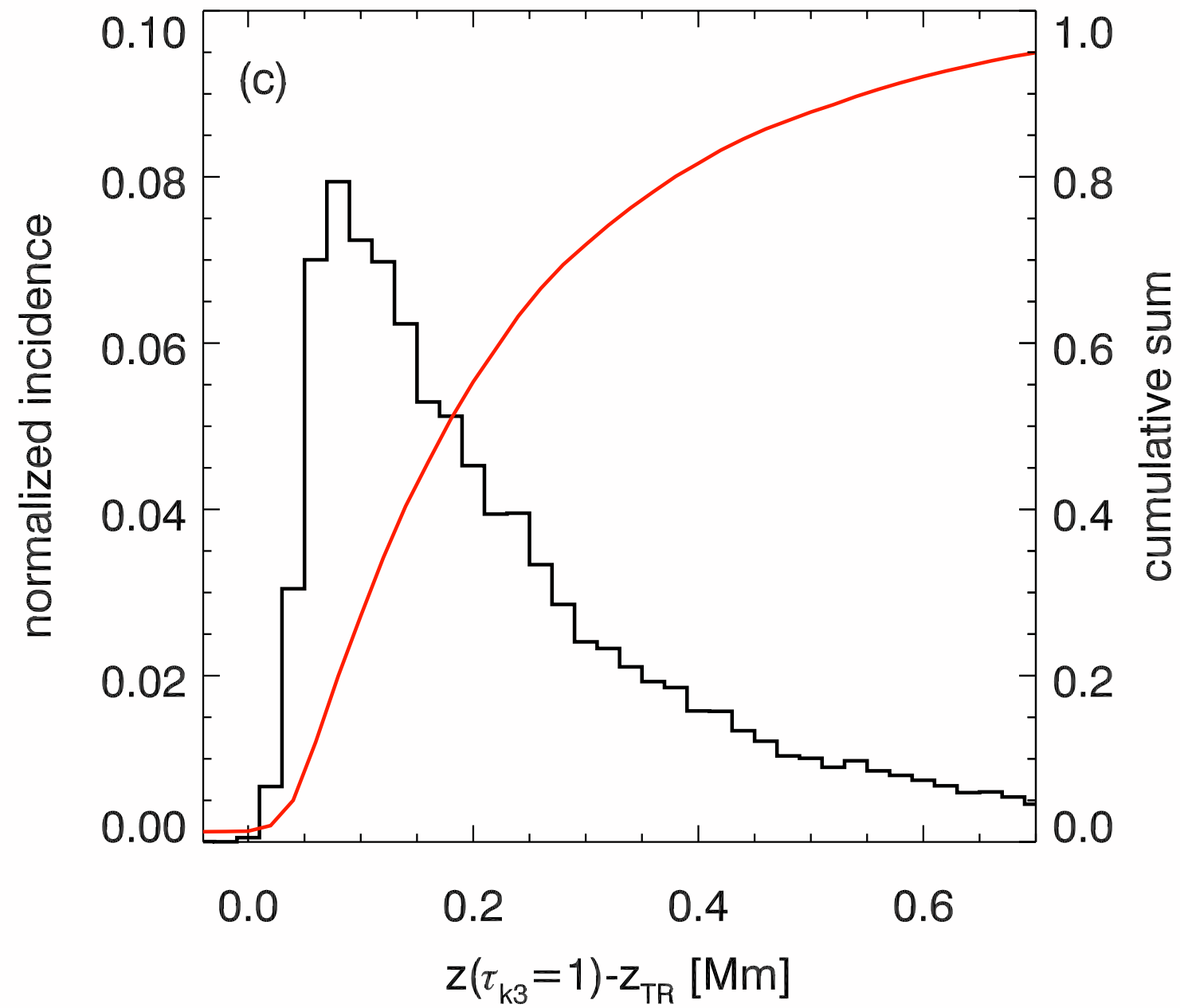


Made available at <http://sdc.uio.no/search/simulations>

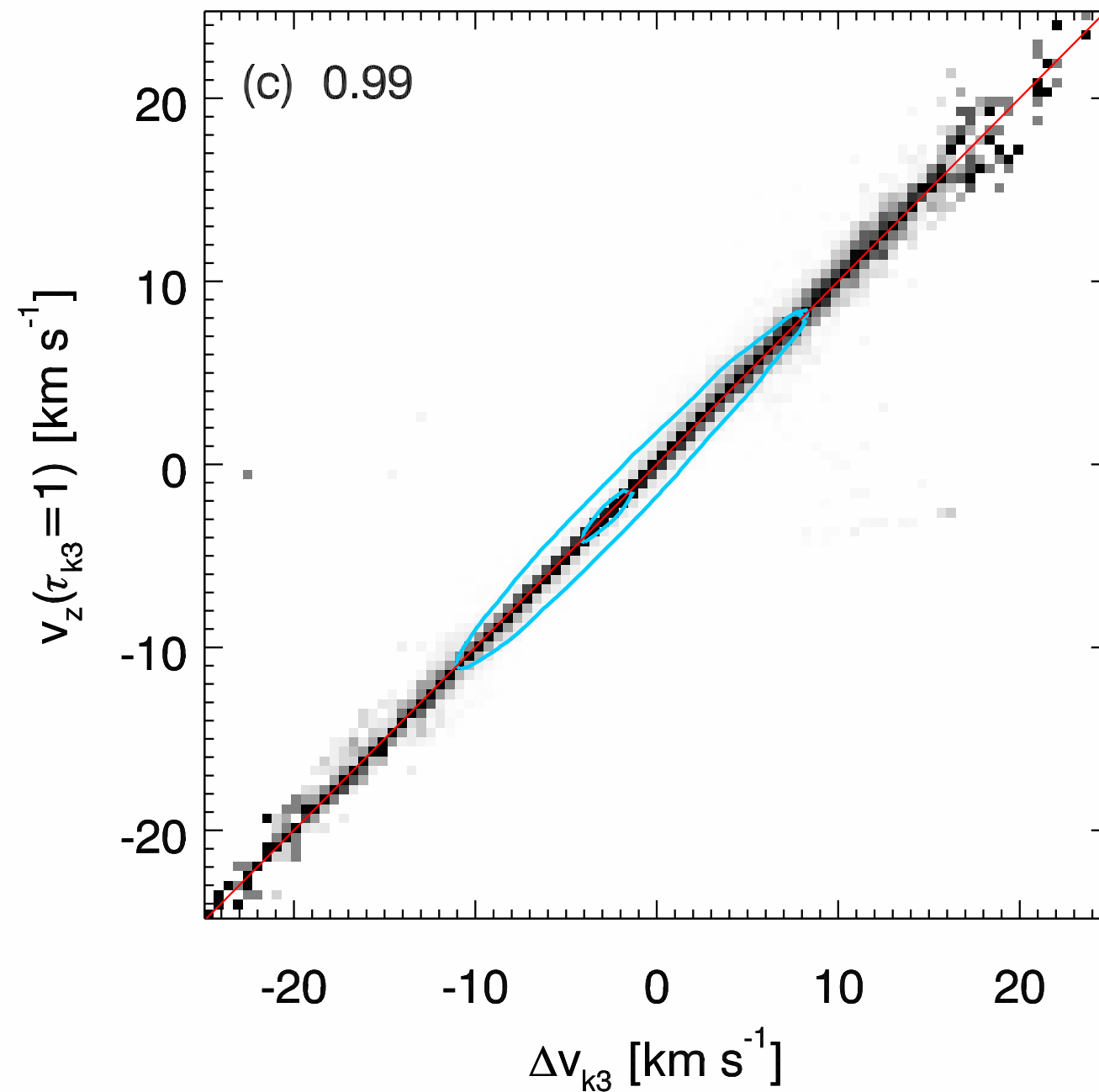
Observables: intensity and Doppler-shift of features



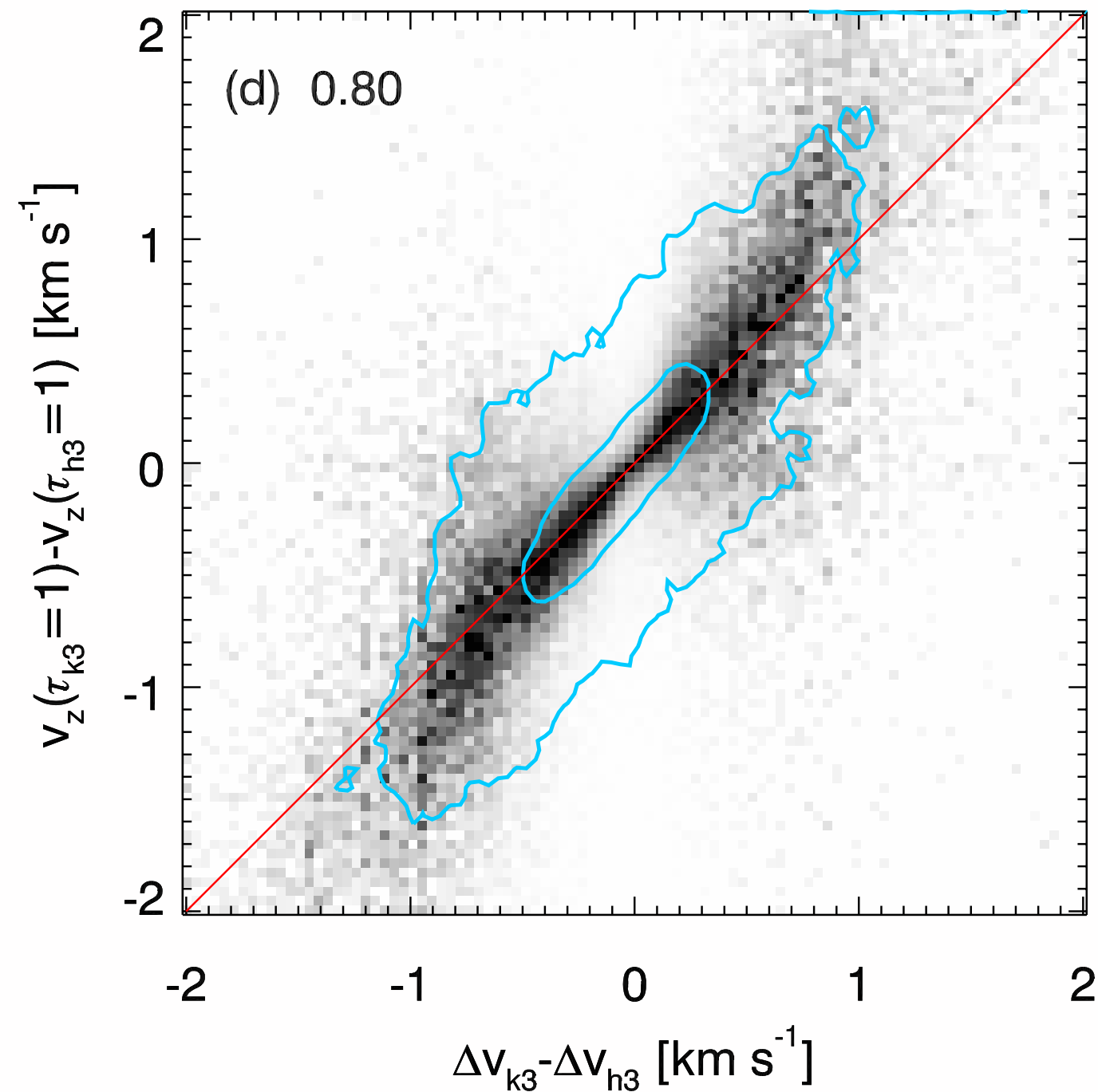
Mg II h&k: line core forms 200 km below the TR



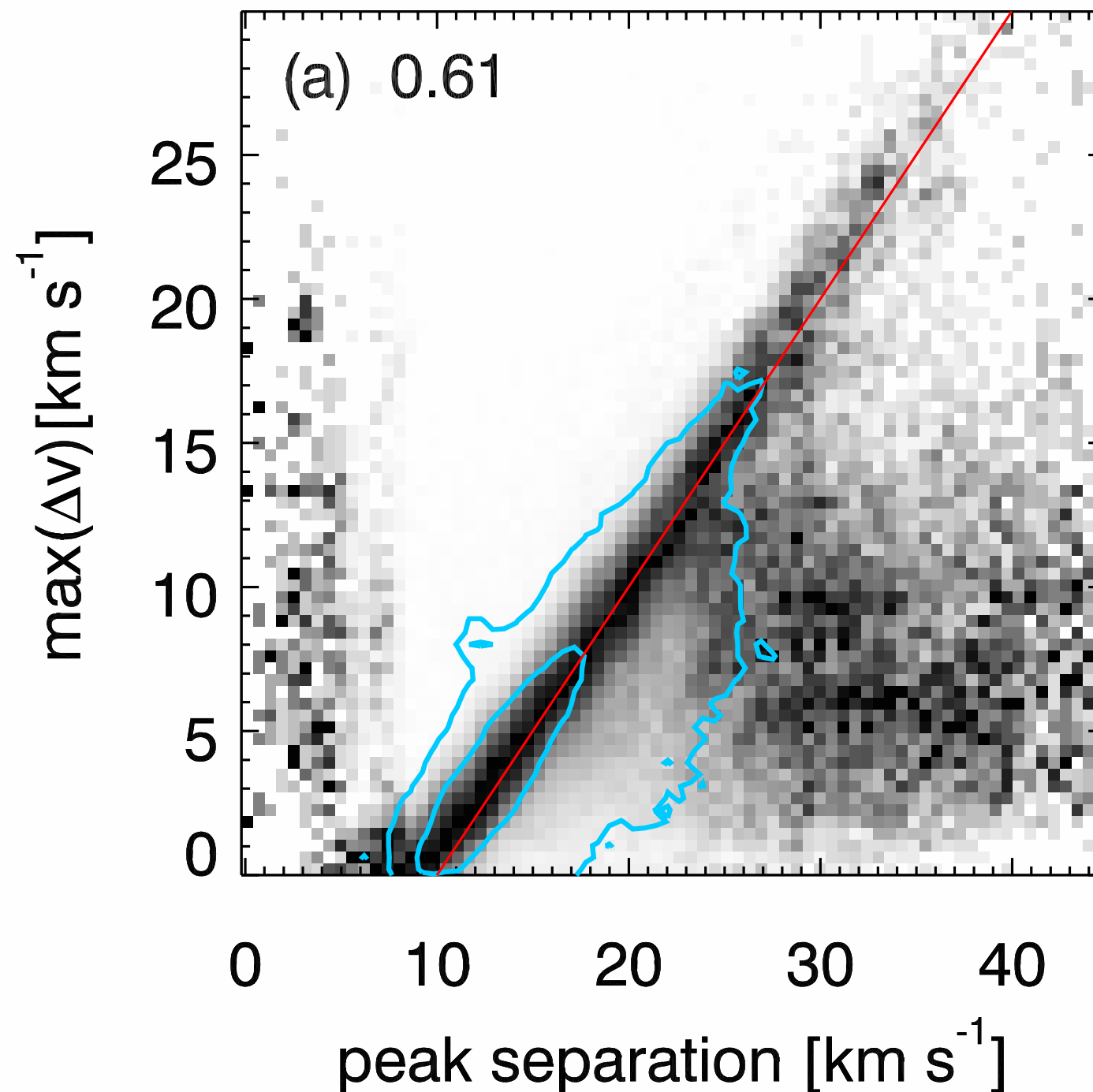
Mg II h&k: h3/k3 minimum Dopplershift correlates with $v_z(\tau=1)$



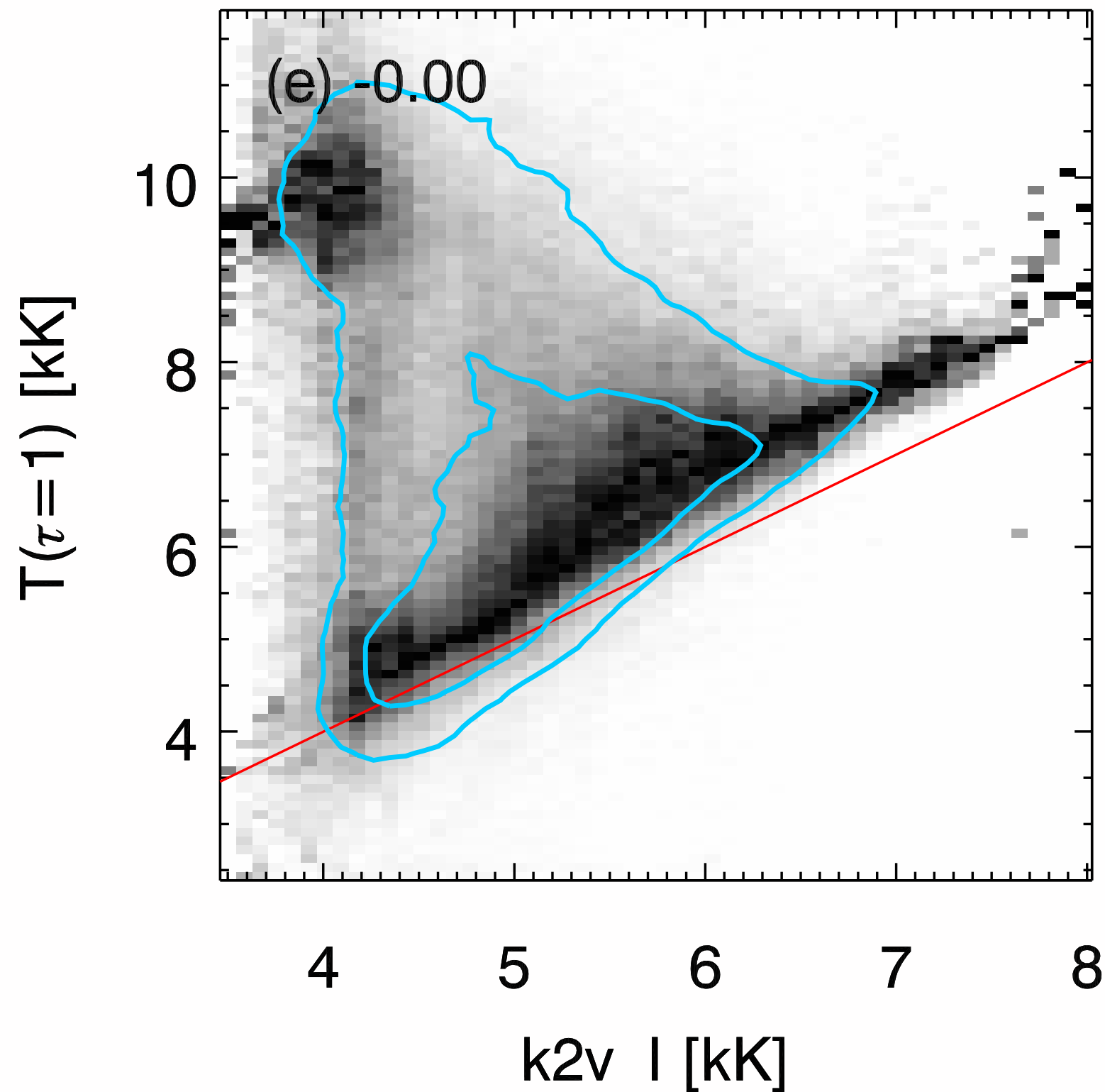
Mg II h&k: h3-k3 Dopplershift measures velocity gradient



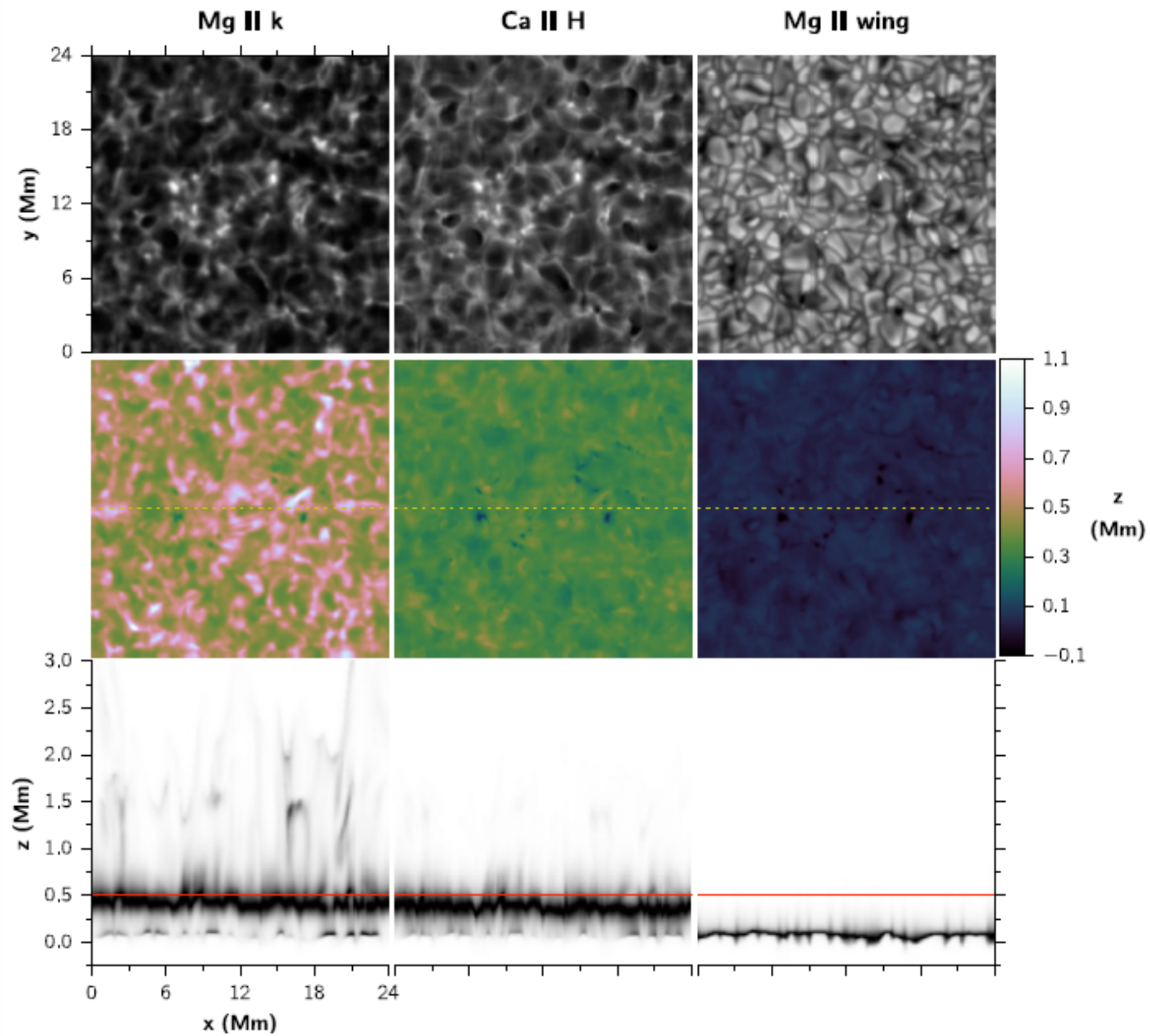
Mg II h&k: peak separation measures velocity extremes



Mg II h&k: peak intensity measures temperature

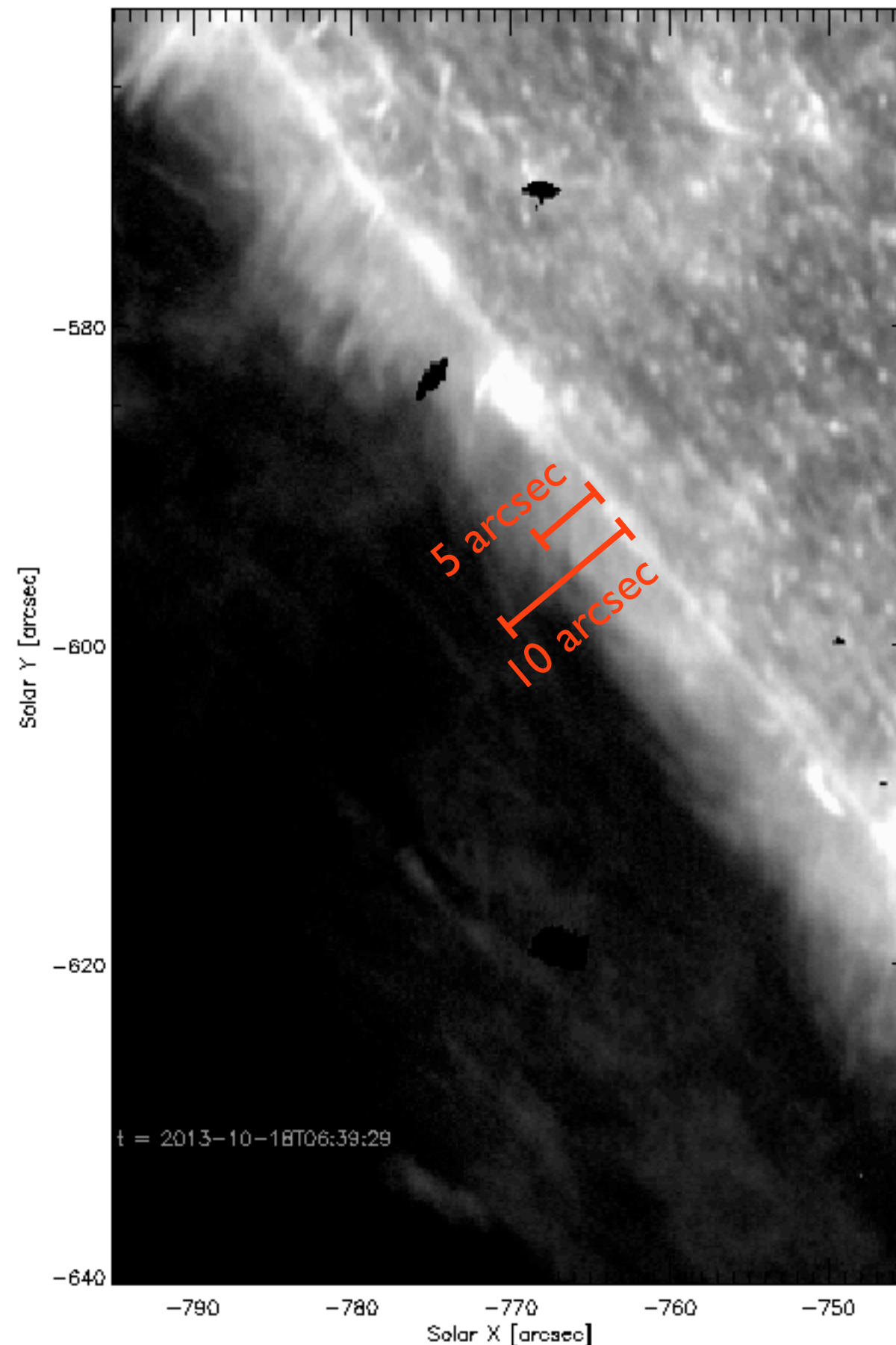


Wide band filters



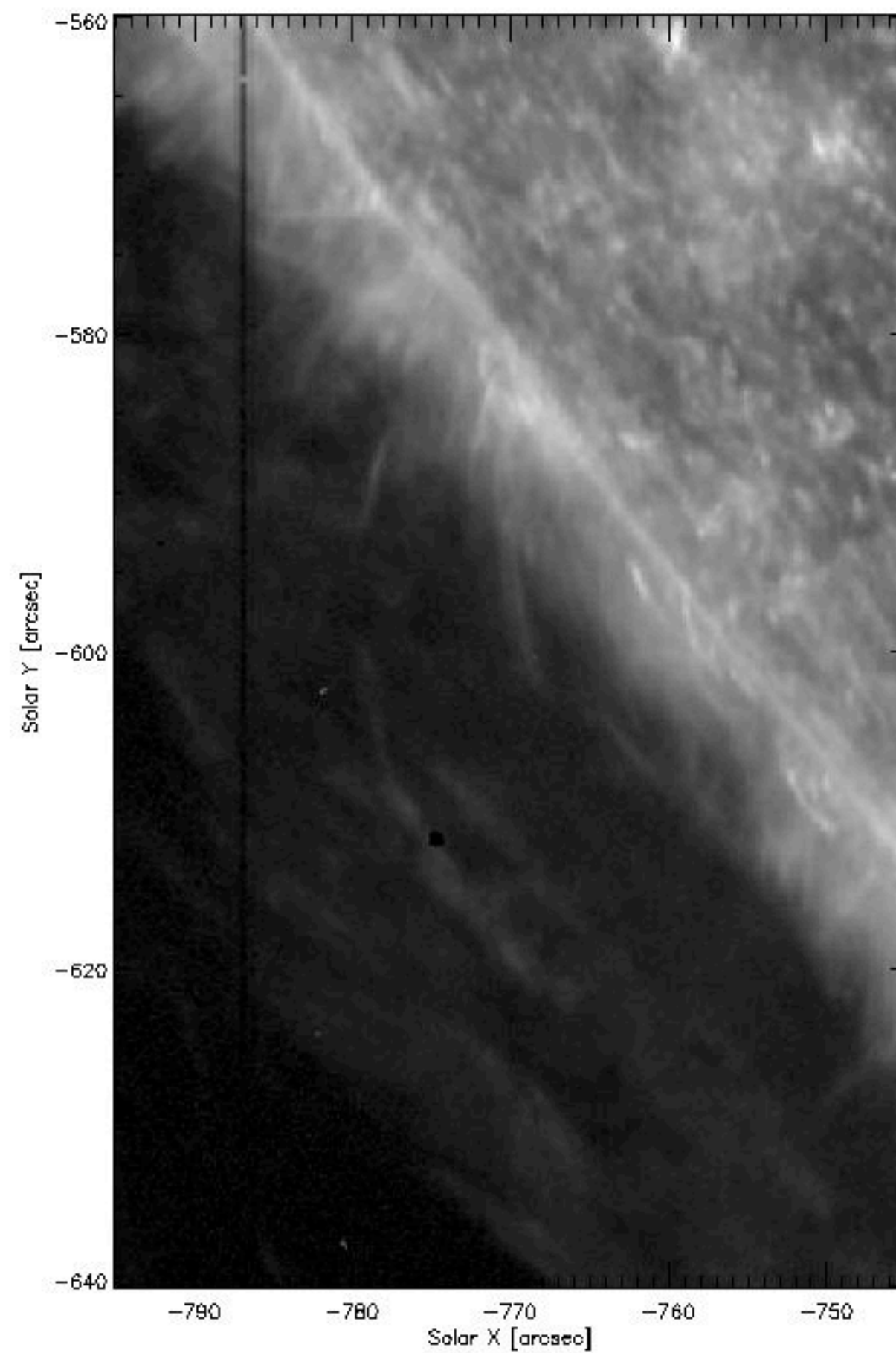
First Comparison between IRIS Data and Numerical Models

There are
many
low lying,
short lived,
presumably
cool,
loops in the
C II '1330'
and Si IV
'1400' slit jaw
images.

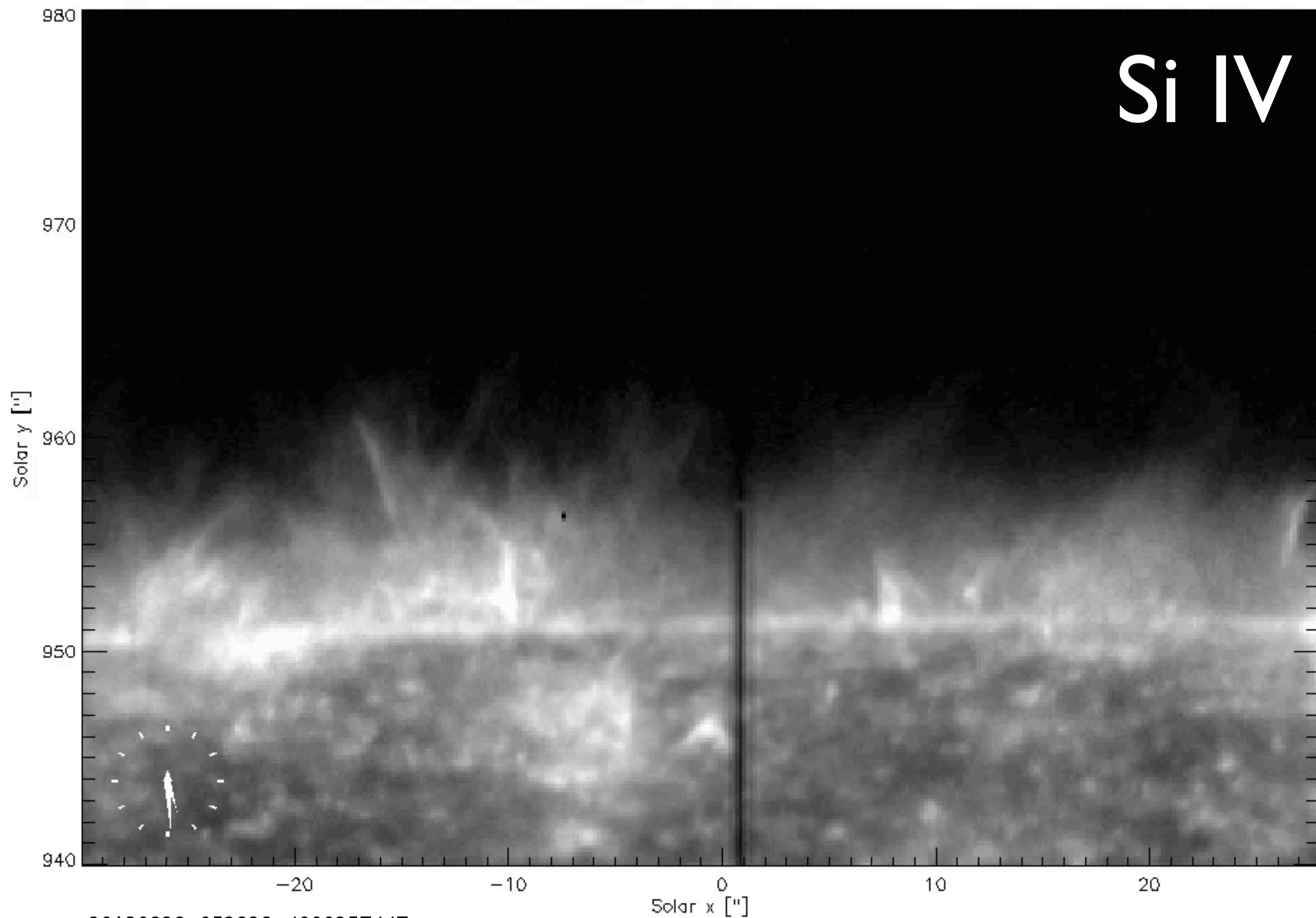


UFS

Viggo Hansteen
et al (in prep)

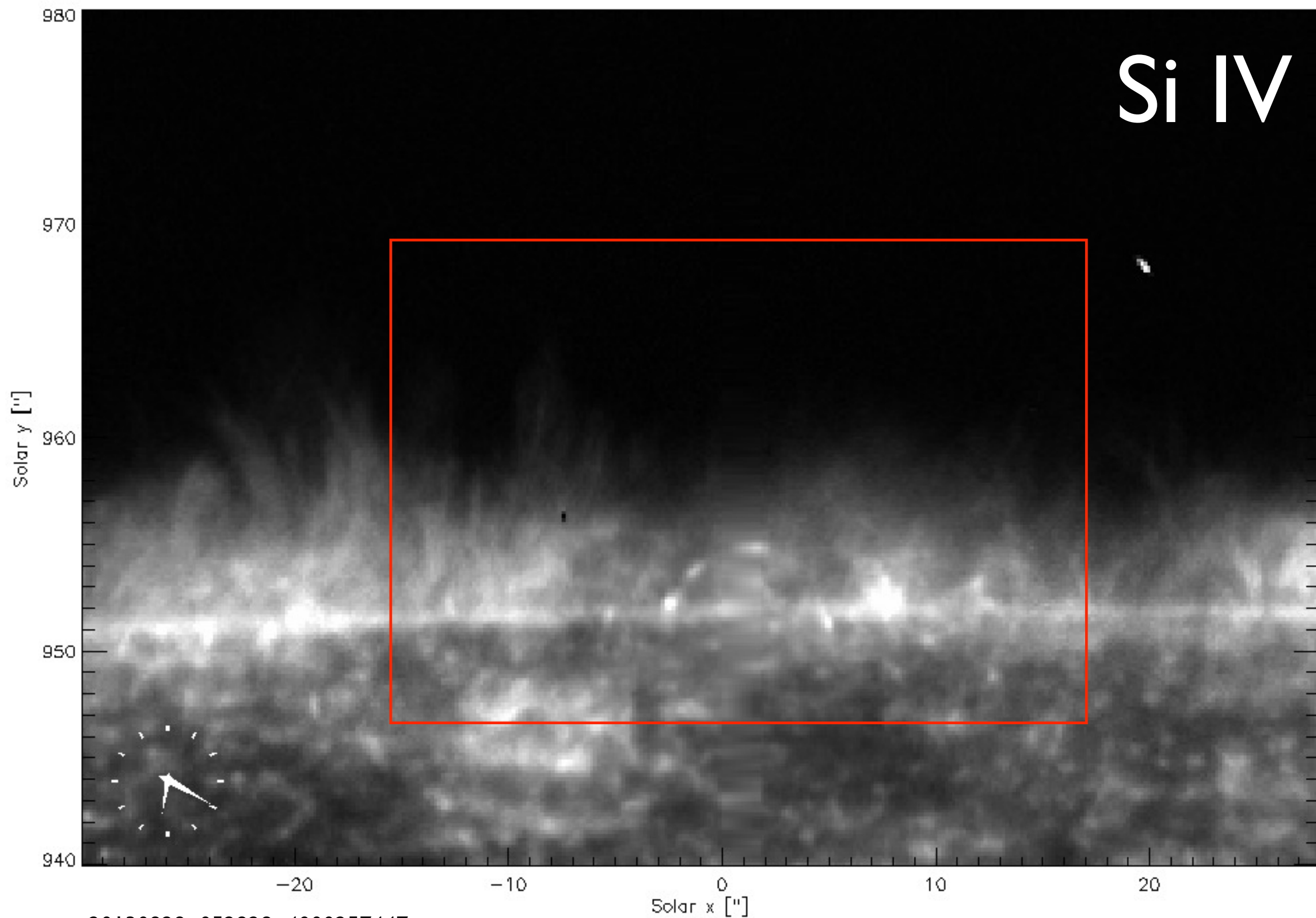


Si IV

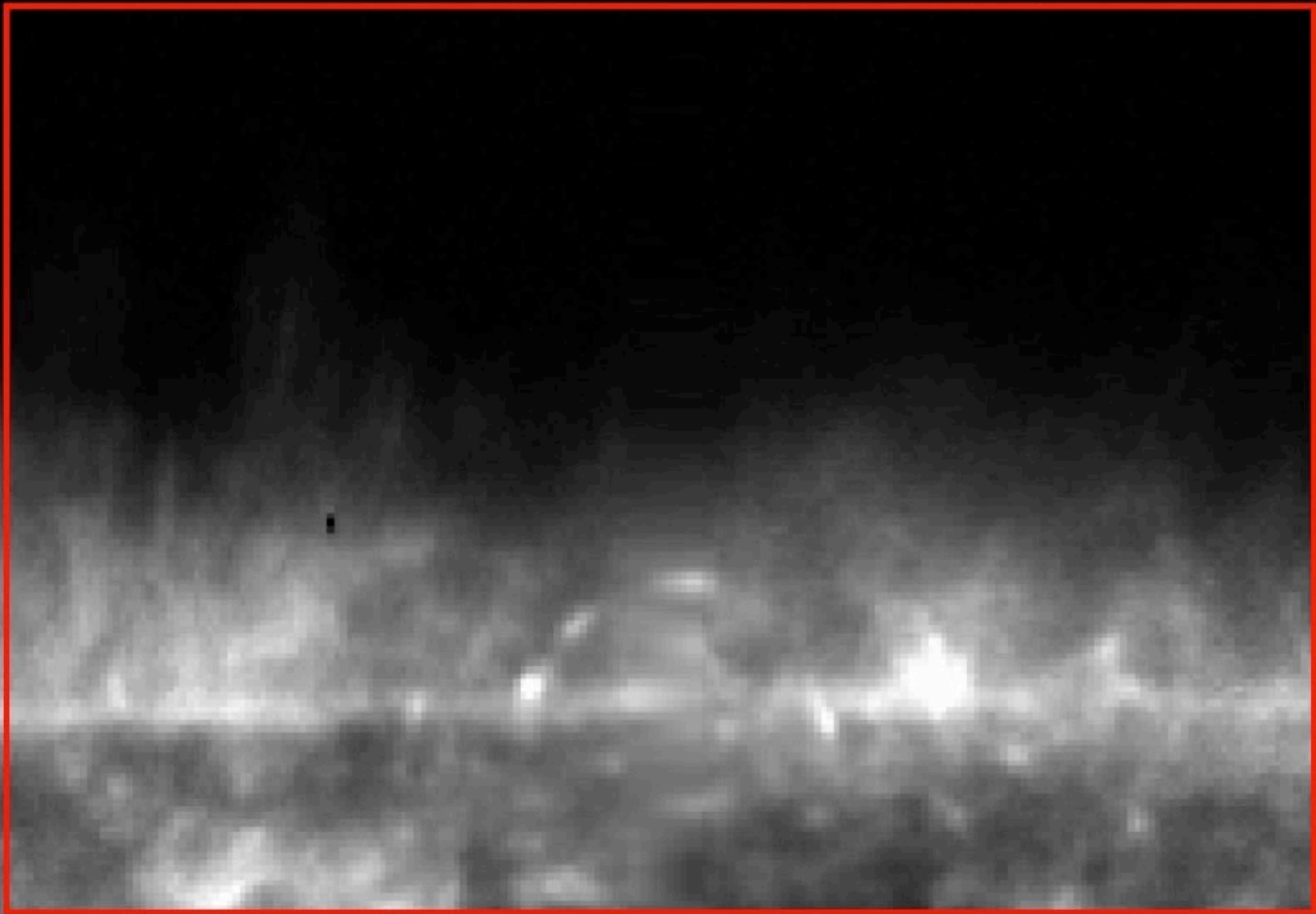


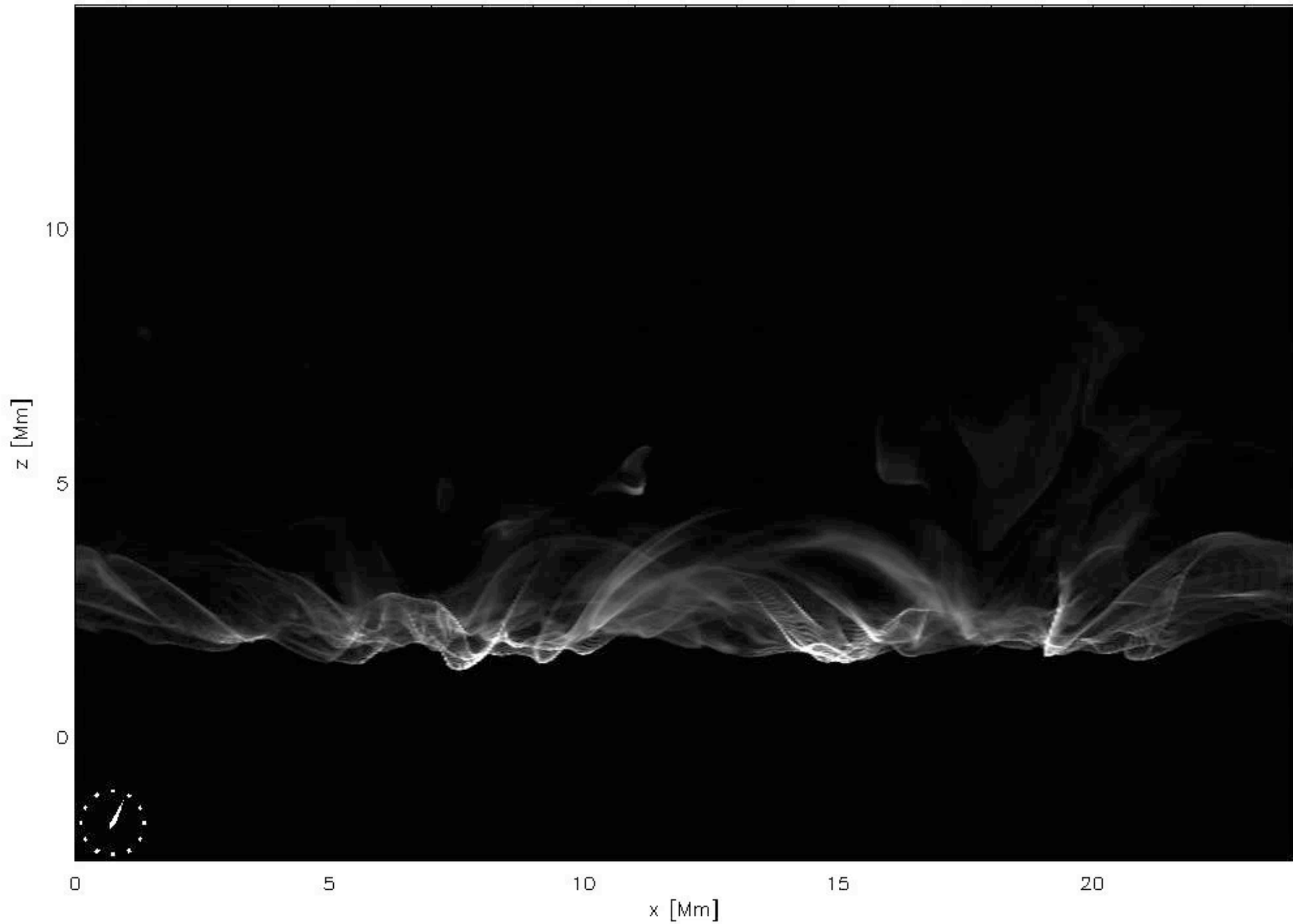
20130929_052928_4000257447

Si IV

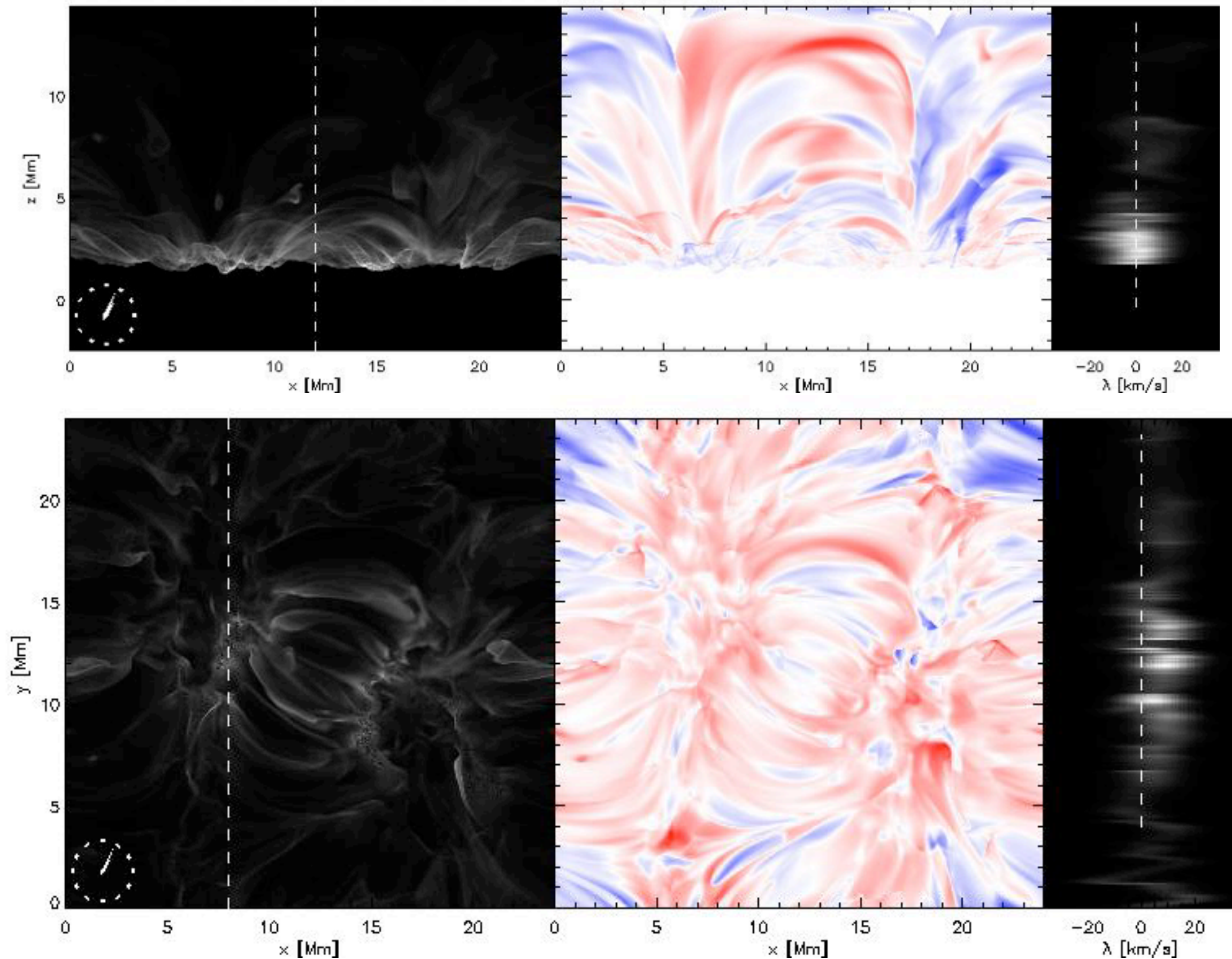


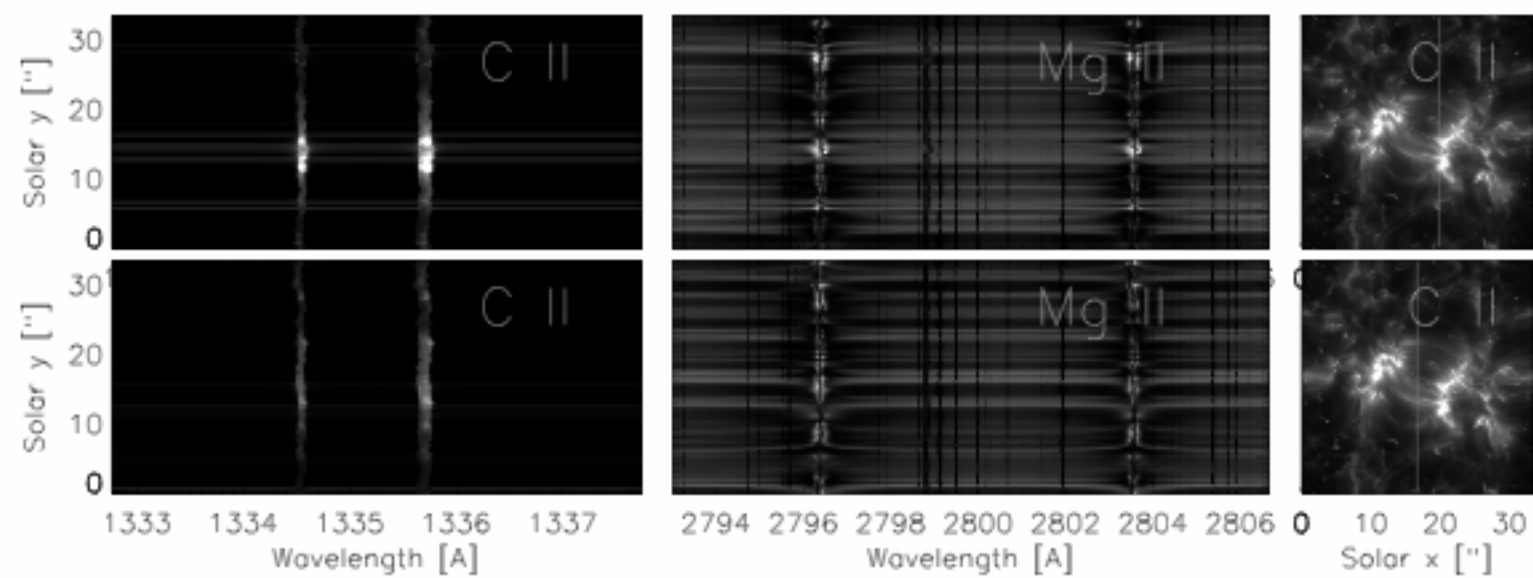
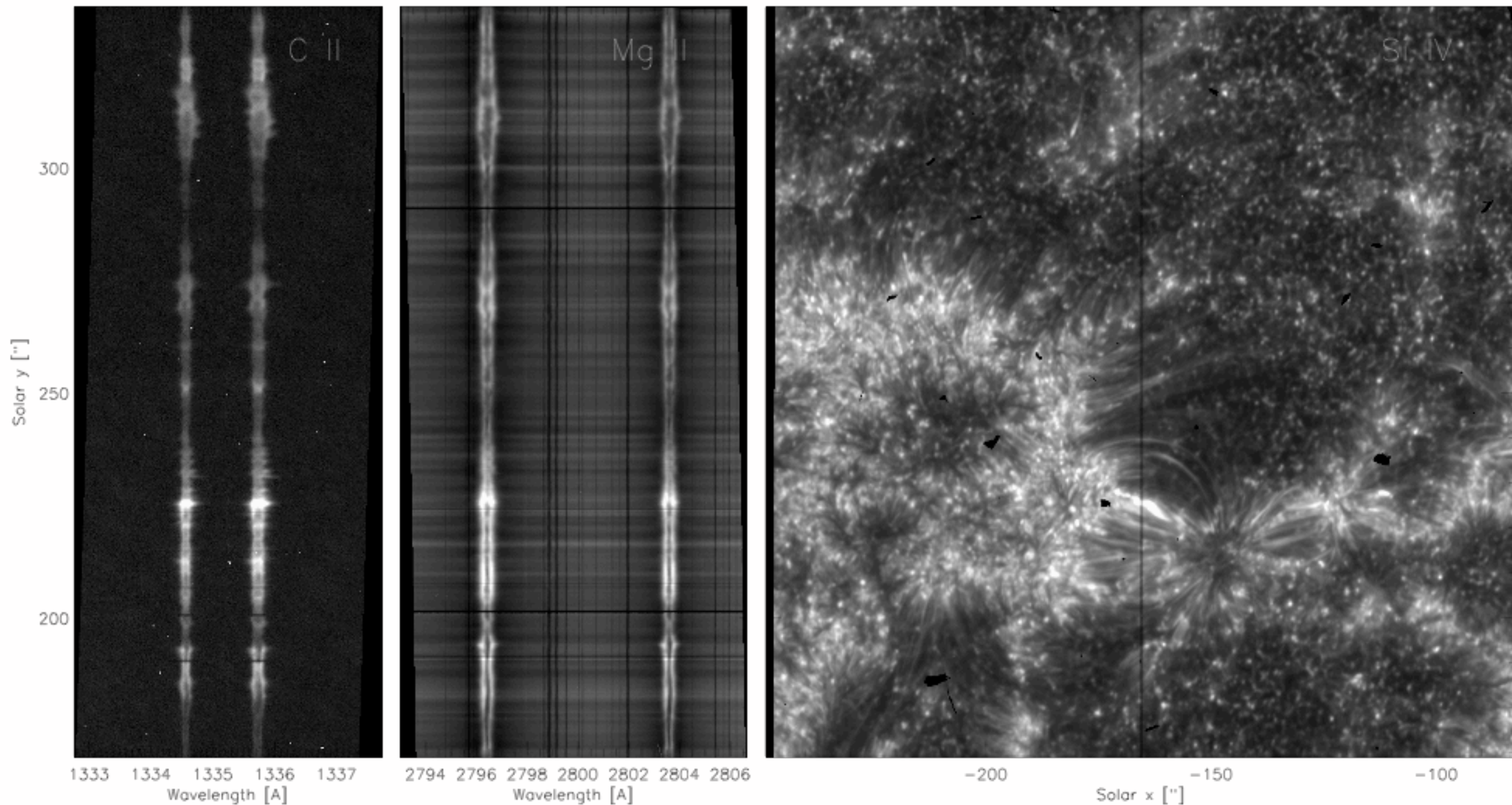
20130929_052928_4000257447

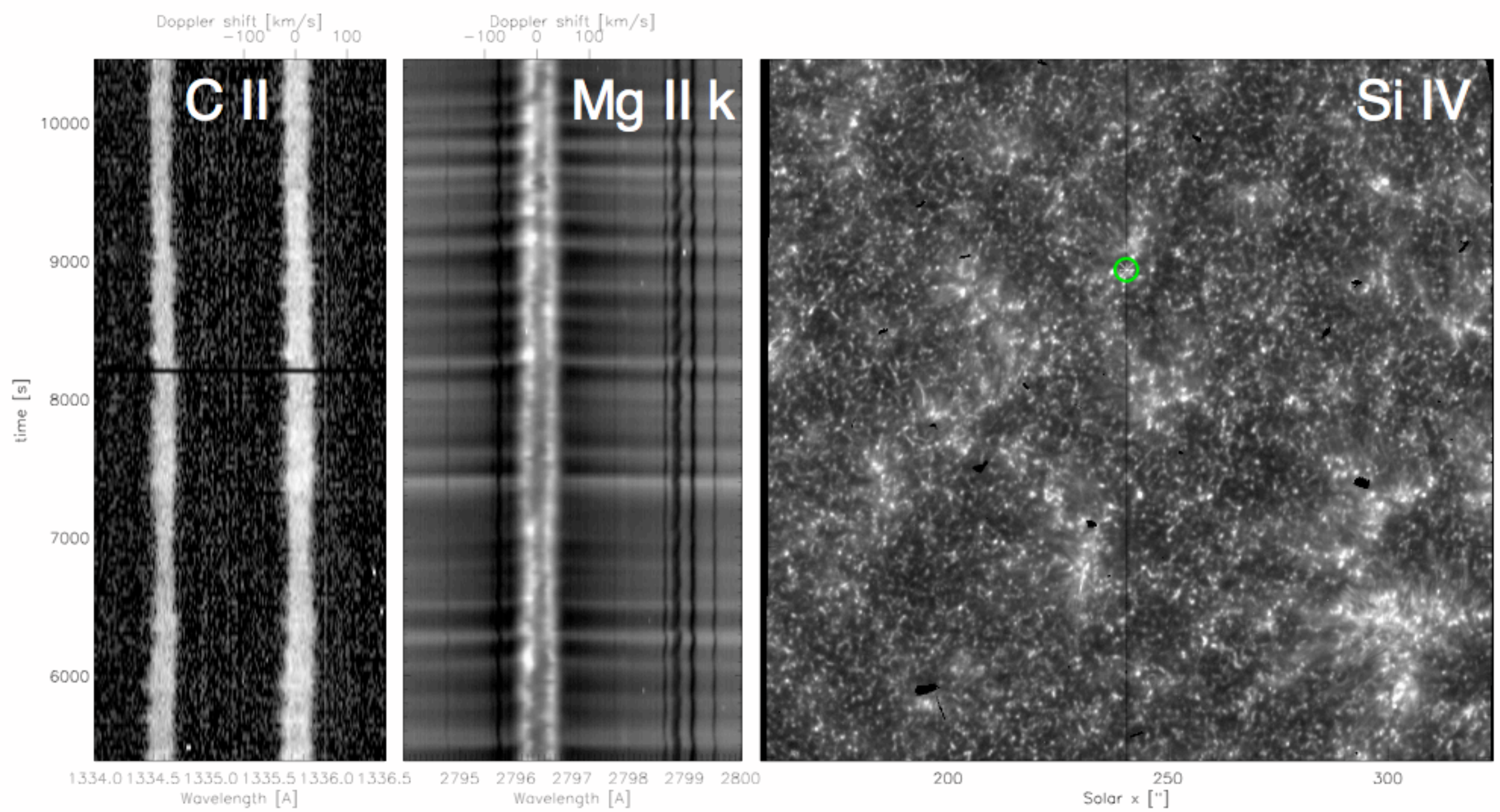


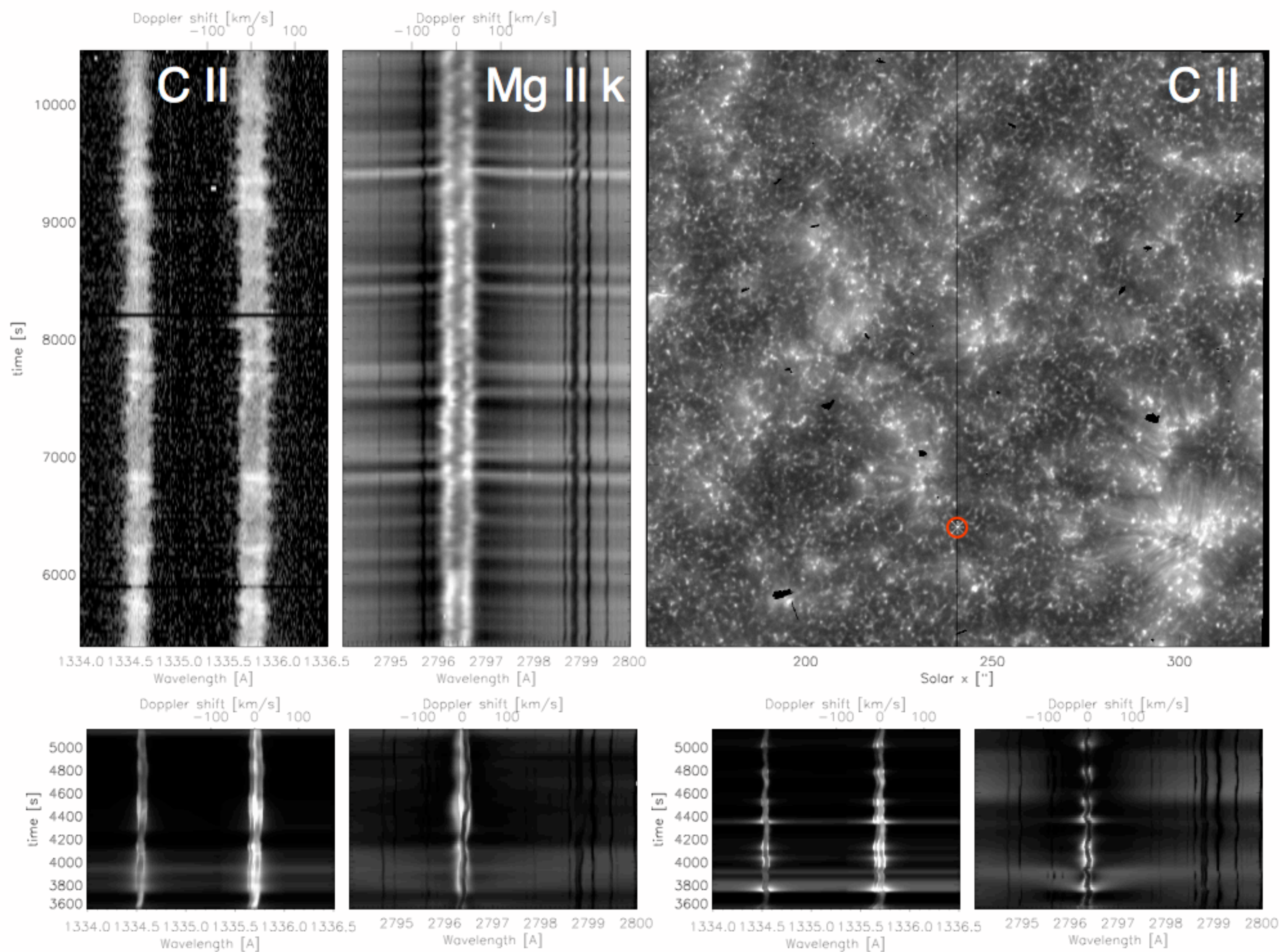


BIFROST simulated Si IV 1393 Å emission









Differences simulations/reality

- simulations show narrower profiles and too little emission on average
- not enough small scale dynamics in simulations - need higher resolution + ion-neutral effects + ?
- not enough chromospheric heating - lacking small scale magnetic field + ion-neutral effects + ?

MULTI

MULTI

<http://folk.uio.no/matsc/mul23>

- ID
- Statistical equilibrium
- given atmosphere $\{T, N_e, V_z, V_{mic}\}(x)$
- one element at a time
- continuum opacity in LTE
- Complete Redistribution
- Hydrostatic equilibrium can be solved for

MULTI documentation

in <http://folk.uio.no/matsc/mul23>

multi_manual.pdf

report33.pdf

mul23.pdf

idldoc.pdf

multi_exercises.pdf

quick start manual

version 1.0 documentation

version 2.3 documentation

IDL routines documentation

exercises

MULTI

Input files

ATMOS	atmospheric structure
DSCALE	depth discretization
ABUND	abundances
ABSDAT	background opacities
ATOM	atomic data
INPUT	switches, run-parameters

Output

IDL files
JOBLOG
OUT

ATMOS

```

VAL3C
MASS SCALE
*
* LG G
  4.44
*
* NDEP
  52
*
*LG CMASS      TEMPERATURE      NE      V      VTURB
  -5.279262E+00  4.470000E+05  1.205000E+09  0.      1.128000E+01
  -5.270430E+00  1.410000E+05  3.839000E+09  0.      9.870000E+00
  -5.269783E+00  8.910000E+04  5.961000E+09  0.      9.820000E+00
  -5.268492E+00  5.000000E+04  9.993000E+09  0.      9.760000E+00
. . .
*
* HYDROGEN POPULATIONS
* NH(1)      NH(2)      NH(3)      NH(4)      NH(5)      NP
  2.3841E+03  7.9839E-04  2.0919E-04  2.3110E-04  2.9470E-04  1.0030E+09
  5.3401E+04  1.8790E-02  7.4560E-03  8.1751E-03  1.0430E-02  3.1990E+09
  2.4030E+05  7.5740E-02  2.9400E-02  3.1550E-02  4.0101E-02  5.0310E+09
. . .
```

DSCALE

```
* DEPTH SCALE FROM DSCAL2  
DSCAL2 ON equidistant  
MASS SCALE
```

```
* NDEP      lg(Tau_500[1])  
80          -6.672232  
           -5.225000  
           -5.213486
```

...

ABUND

H	1.000E+00		
HE	1.000E-01		
SI	3.548E-05	from Grevesse	1989
MG	3.802E-05	from Grevesse	1989
AL	2.951E-06	from Grevesse	1989
FE	4.677E-05	from Grevesse	1989
C	3.631E-04	from Grevesse	1989
NA	1.514E-06		
S	1.622E-05		
K	1.122E-07		
CA	2.138E-06		
NI	1.202E-07		
CR	2.951E-07		
N	8.511E-05		
O	5.888E-04		
NE	3.236E-04		
SC	1.259e-09	from Grevesse	1989
TI	9.772e-08	from Grevesse	1989
V	1.000e-08	from Grevesse	1989
MN	2.455e-07	from Grevesse	1989
CO	8.318e-08	from Grevesse	1989

ABUND

H	12.00	abundances from
HE	10.93	Asplund, Grevesse, Sauval, Scott 2009, ARAA 47, 481
SI	7.51	
MG	7.60	
AL	6.45	
FE	7.50	
C	8.43	
NA	6.24	
S	7.12	
K	5.03	
CA	6.34	
NI	6.22	
CR	5.64	
N	7.83	
O	8.69	
NE	7.93	
SC	3.15	
TI	4.95	
V	3.93	
MN	5.43	
CO	4.99	

ABSDAT

```

      21
H  HE  C   N   O   NE  NA  MG  AL  SI  S   K   CA  SC  TI  V   CR  MN  FE  CO  NI
      1.008      4.003      12.01      14.01      16.00      20.18
      23.00      24.32      26.97      28.06      32.06      39.10
      40.08      45.0       47.9       50.9       52.01      54.9
      55.85      58.9       58.69
      2         3         4         4         4         4         4         4
      4         4         4         4         4         4         4
      2         1
H  I
13.595      2  11.0      2
H  I
...
/CA  II  3P6  4S  2SE      CA  III  GROUND  TERM      P.JUDGE  /  COMPILATION
  2          0.000      2.0
      ILOGL=1      KVADL=0      MINEX=0      MAXEX=0      NLATB= 11
      510.         600.         750.         850.         950.         1000.
      1020.        1026.        1030.        1035.        1045.
      ILOGT=0      KVADT=0      MINET=0      MAXET=0      NTETB= 1      ITETA=0
1.557E-19  1.836E-19  2.101E-19  2.183E-19  2.142E-19  2.122E-19
2.101E-19  2.081E-19  2.060E-19  2.060E-19  2.040E-19
...
```

ATOM

```
CA II
* ABUND    AWGT
   6.36    40.08
*NK NLINE NCONT NRFIX
   6      5      5      0
*      E      G      LABEL      ION
   0.00000  2.00000  'CA II 3P6 4S 2SE      '      2
 13650.248  4.00000  'CA II 3P6 3D 2DE 3/2'      2
 13710.900  6.00000  'CA II 3P6 3D 2DE 5/2'      2
 25191.535  2.00000  'CA II 3P6 4P 2PO 1/2'      2
 25414.465  4.00000  'CA II 3P6 4P 2PO 3/2'      2
 95785.470  1.00000  'CA III GROUND TERM      '      3
* J  I      F      NQ  QMAX  Q0 IW      GA      GVW      GS
  4  1  3.1600E-01 101  300.  3. 0  1.42E08  234.223  3.0E-06
  5  1  6.3700E-01 101  300.  3. 0  1.46E08  234.223  3.0E-06
  4  2  4.7300E-02 101  150.  1. 0  1.42E08    2.04  3.0E-06
  5  2  9.6000E-03 101  150.  1. 0  1.46E08    2.01  3.0E-06
  5  3  5.7400E-02 101  150.  1. 0  1.46E08    2.01  3.0E-06
* UP  LO      F      NQ  QMAX      Q0
   6  1  2.036E-19  5  -1.      0.0
 1044.2    2.0360E-19
   911.7    2.1400E-19
   850.0    2.1720E-19
   750.0    2.1030E-19
   600.0    1.8200E-19
*
. . .
GENCOL
TEMP
  7      2000.      3000.      6000.      12000.      24000.      48000.      96000.
OHMEGA
  2  1  5.60e+00  5.60e+00  5.60e+00  5.60e+00  5.60e+00  5.60e+00  5.60e+00
OHMEGA
. . .
```

INPUT

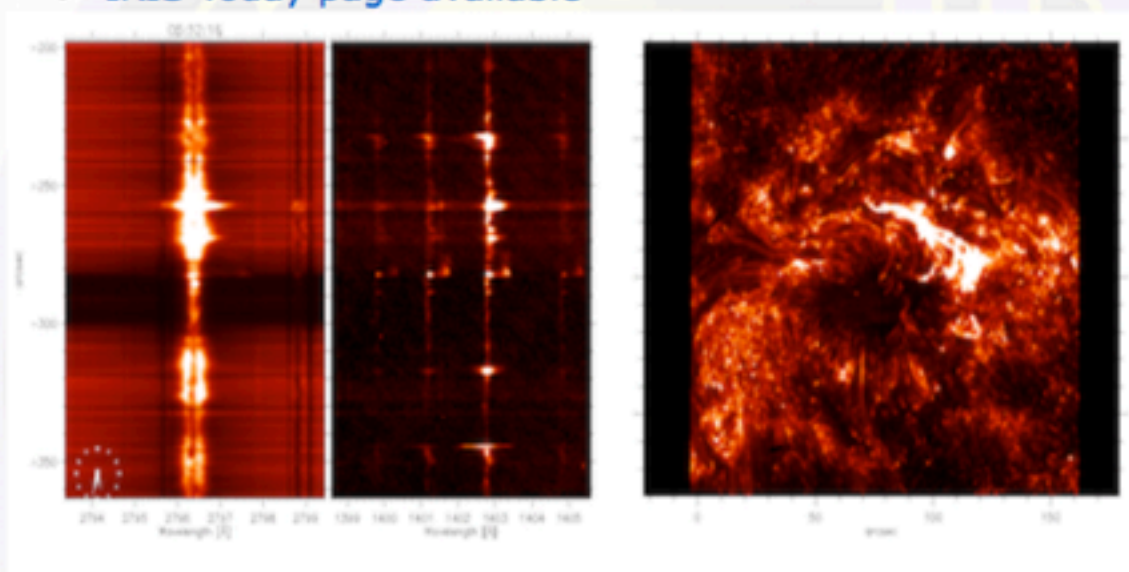
DIFF=2.0,ELIM1=0.1,ELIM2=0.001,QNORM=12.85,THIN=0.1,
IATOM2=0,ICONV=1,IHSE=0,ILAMBD=2,IOPAC=1,ISTART=1,ISUM=0,
ITMAX=40,ITRAN=0,NMU=5,
IWABND=0,IWATMS=0,IWATOM=0,IWCHAN=0,IWDAMP=0,IWEMAX=1,IWEQW=0,
IWEVEC=0,IWHEAD=0,IWHSE=0,IWLGMX=1,IWLINE=0,IWLTE=0,IWN=0,IWNIIT=0,
IWOPAC=0,IWRAD=0,IWRATE=0,IWSTRT=0,IWTAUQ=0,IWTEST=0,IWWMAT=0,
IWJFIX=0,IWARN=0,IOPACL=0,ISCAT=0,INCRAD=0,INGACC=0,ICRSW=0,
IOSMET=0,EOSMET=0.5,
IDL1=1,IDLNY=1,IDLCNT=1,IDLOPC=1

Working with IRIS data

<http://iris.lmsal.com>

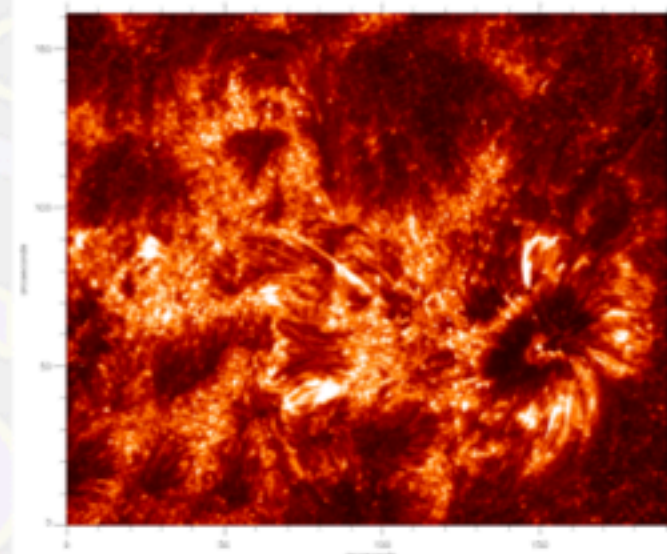
Current News

- **9 December 2013:** [IRIS-related numerical models \(Bifrost\)](#) now available
- **2 December 2013:** [IRIS mission/instrument paper](#) now available
- **31 October 2013:** Calibrated level 2 data now available:
 - See our [Press page](#) for details.
 - Find the data [at LMSAL](#) or [at University of Oslo](#)
 - [Technical documentation](#) updated and available
 - [IRIS Today page](#) available



Previous IRIS News

- **1 October 2013:** [Quicklook slit-jaw movies](#) available
- **24 July 2013:** [First Light Press Release](#)



- **27 June 2013:** IRIS launched



- **19 June 2009:** NASA announces [selection of IRIS](#).

IRIS mission/instrument paper

Operations/Planning

- [ITN 1 - IRIS Operations Overview](#)
- [ITN 2 - Manual for Table Creator](#)
- [ITN 3 - Manual for Timeline Tool](#)
- [ITN 4 - Manual for Synthetic Observations Tool](#)
- [ITN 5 - Operations Under Roll Conditions](#)
- [ITN 6 - AEC Operations](#)
- [ITN 7 - Compression Approach](#)
- [ITN 8 - Checklist for IRIS planner](#)
- [ITN 9 - Periodic Calibration Activities](#)

Data Flow

- [ITN 10 - General Approach to Data Flow and Archiving](#)
- [ITN 11 - Definition of Data Levels](#)
- [ITN 12 - Definition of Keywords](#)
- [ITN 13 - VSO and IRIS](#)

Calibration

- [ITN 14 - Dark Current/Offset](#)
- [ITN 15 - Despiking](#)
- [ITN 16 - Flat-field](#)
- [ITN 19 - Geometric Calibration](#)
- [ITN 20 - Wavelength Calibration](#)
- [ITN 21 - Recasting into Level 2/3 Data](#)
- [ITN 22 - Co-alignment, Plate Scale Analysis](#)
- [ITN 23 - MTF/PSF Determination](#)
- [ITN 24 - Stellar Calibration](#)
- [ITN 25 - Gain Determination](#)

Data Analysis

- [ITN 26 - User Guide To Data Analysis](#)
- [ITN 27 - Quicklook Tools Manual](#)
- [ITN 28 - IRIS IDL Data Structure](#)
- [ITN 29 - Deconvolution Approach](#)
- [ITN 30 - 60 Day Observing Plan](#)
- [ITN 31 - IRIS science planning: tables, linelists, targets](#)
- [SolarSoft Tree and UVSP Database](#)

Numerical Modeling

- [ITN 33 - General Overview of Numerical Simulations](#)
- [ITN 34 - Numerical Simulations Quicklook Tools](#)
- [ITN 35 - Numerical Simulations Synthetic Observables](#)
- [ITN 36 - RH 1.5 D Manual](#)
- [ITN 37 - How to Derive Physical Information from Mg II h/k](#)

IRIS Technical Notes List (ITN)

Talks & Posters

- [Invited Talks at the SDO-4/IRIS/Hinode Workshop - March 2012](#)
- [IRIS Talk Hinode 5 Meeting Keynote \(430 MB\) PDF \(36 MB\)](#)
- [IRIS Poster](#)
- [FUV Camera View](#)
- [NUV Camera View](#)

Concept Study Report

- [Executive Summary](#)
- [Science Goals](#)
- [Instrument Description](#)

Operations

[Table Creator](#)

[Timeline](#)

[Simulator](#)

- [IDL code](#)
- [Data \(large\)](#)
- [Data \(small\)](#)

Calibration / Data production

Level 1.5: [iris_prep.pro](#)

Level 2: [iris_level1to2.pro](#)

Level 3: [iris_make_fits_level3.pro](#)

Quicklook

Level 2: [iris_xfiles.pro](#)

Level 3: [crispex.pro](#)

Simulations

Quicklook: [br_xmhd.pro](#)

Radiative Transfer: Multi3d

Radiative Transfer: [RH 1.5d](#) (please acknowledge Han Uitenbroek and Tiago Pereira)

Documentation

[ITN 33 - General Overview of Numerical Simulations](#)

[ITN 34 - Numerical Simulations Quicklook Tools](#)

[ITN 35 - Numerical Simulations Synthetic Observables](#)

[ITN 36 - RH 1.5 D Manual](#)

[ITN 37 - How to Derive Physical Information from Mg II h/k](#)

Bug Tracking

[LMSAL DAI Tool](#) (IRIS team only)



A User's Guide To IRIS Data Retrieval, Reduction & Analysis

Tuesday, February 25, 2014

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This guide will evolve and be frequently updated, especially during the early phases of the mission. Please visit [IRIS Technical Note 26](#) frequently for updated PDF files. Email [Scott McIntosh](#) with questions and changes and we will respond as fast as possible.

The IRIS solarsoft tree is frequently updated by the science team. We strongly recommend that the user keeps a current version of the software tree on their local machine (or systemwide installation). Execute the following command from inside the solarsoft IDL session:

```
IDL> ssw_upgrade, /spawn, /passive, /iris
```

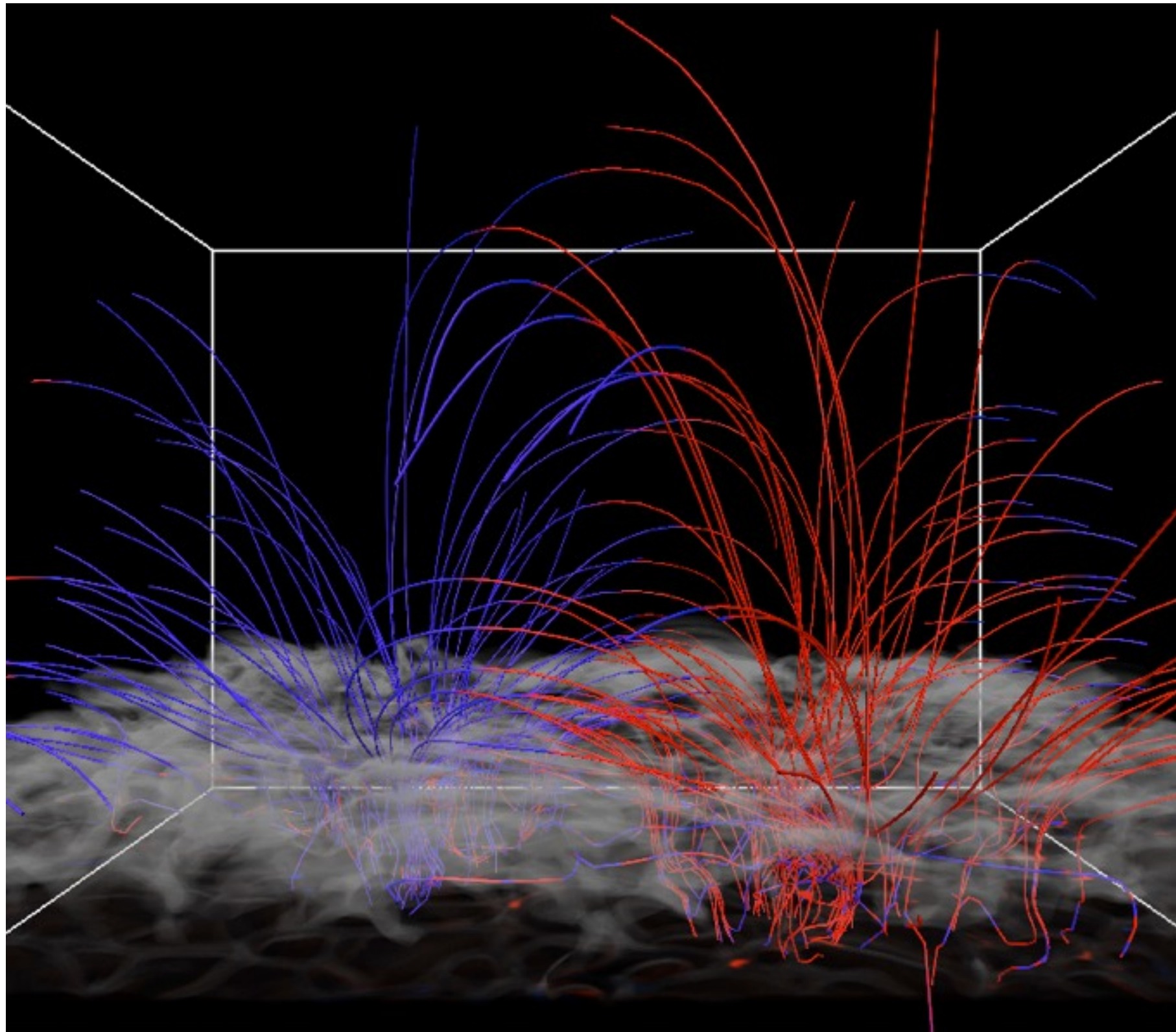
10/15/2013 - see the [IRIS known data issues](#) section.

Public release of Bifrost simulations

“enhanced network” simulation

<http://sdc.uio.no/search/simulations>

IRIS Technical Note 33; Carlsson et al 2014



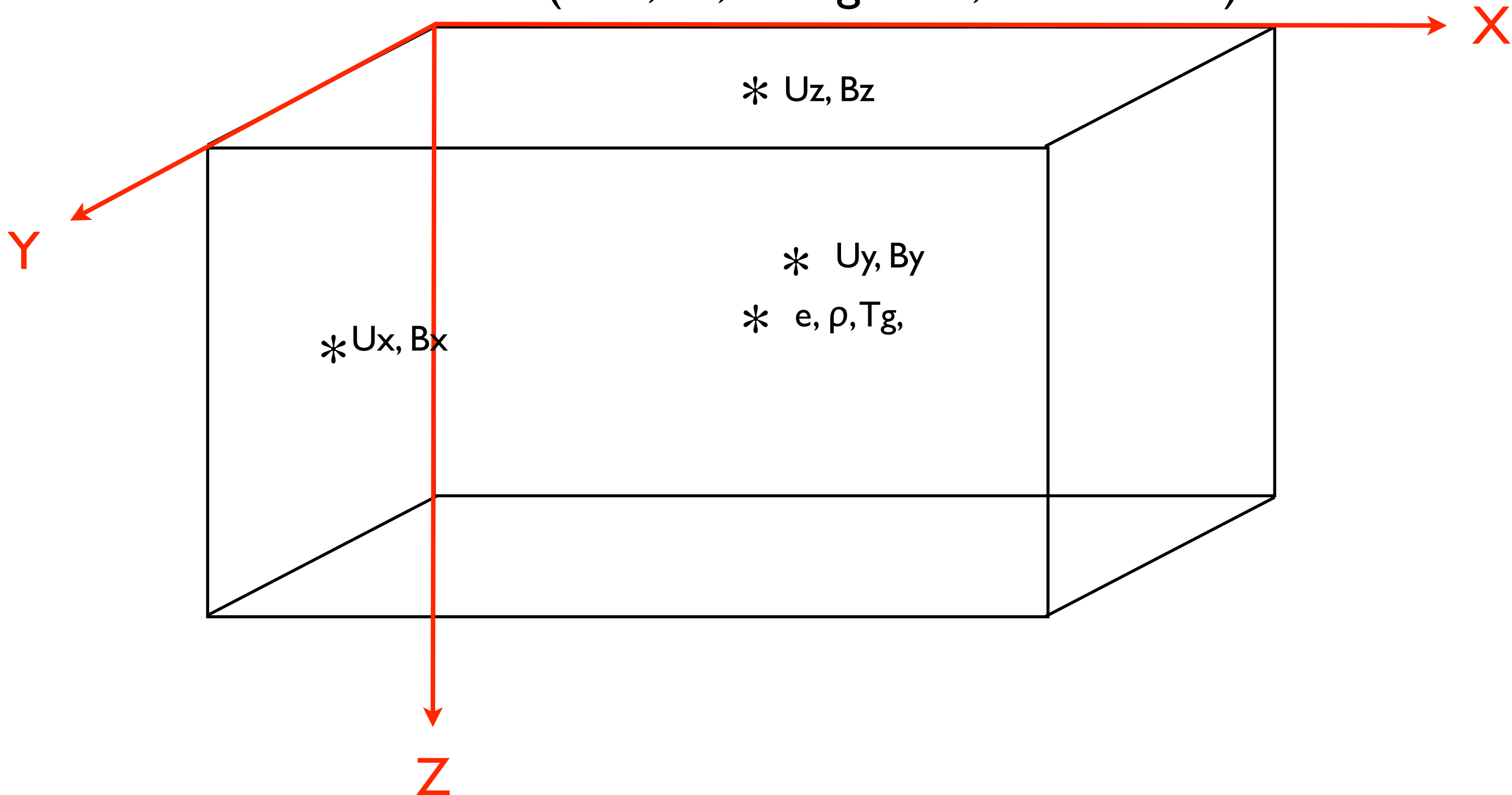
Corona

Transition region
Chromosphere
Photosphere
Convection zone

Bifrost coordinate system

Variables on staggered grid

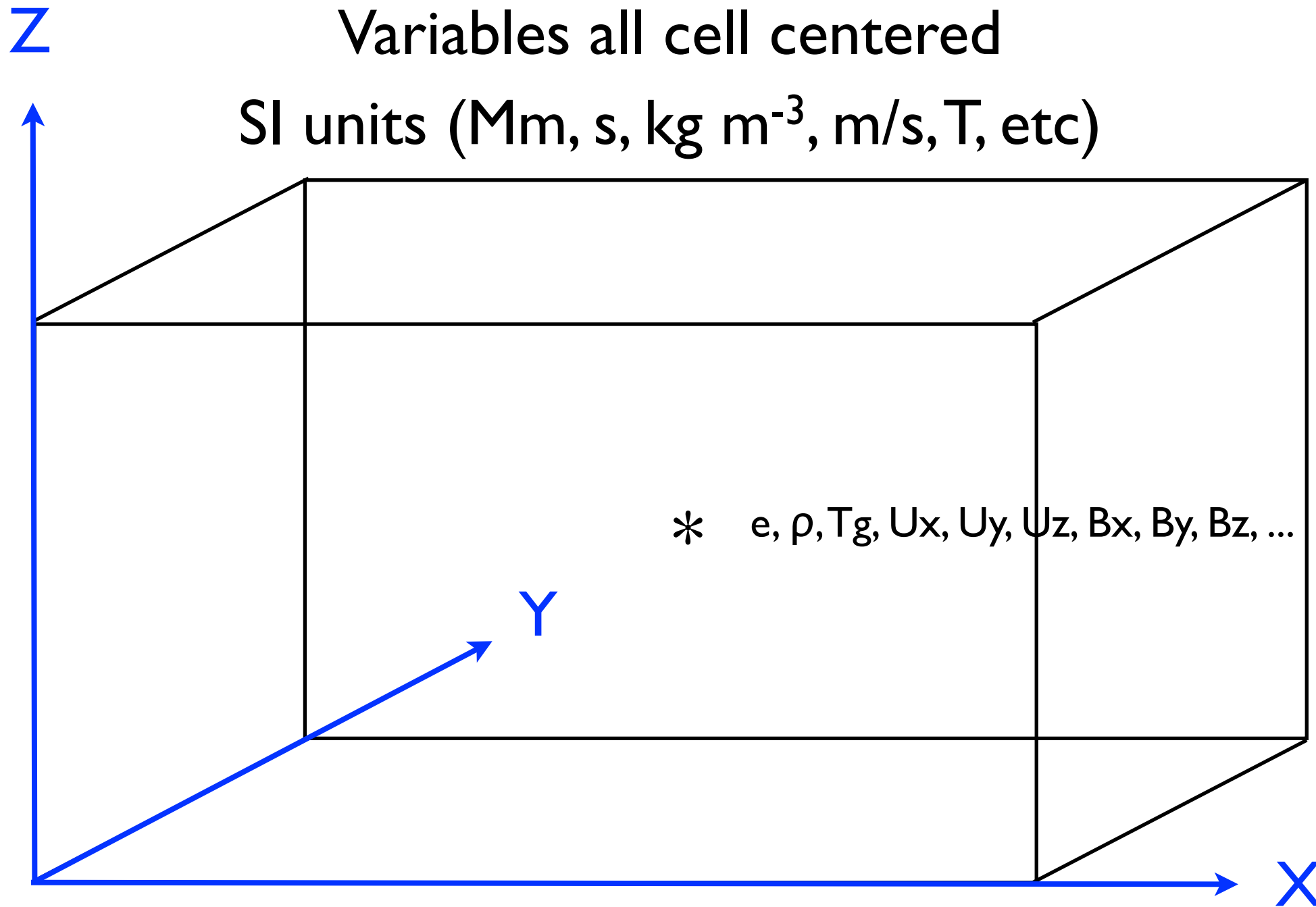
Internal units (Mm, hs, 10^{-7} g cm $^{-3}$, Mm/hs etc)



FITS files

Variables all cell centered

SI units (Mm, s, kg m⁻³, m/s, T, etc)



Format

- Level 2: $D(x,y,z)$ one file per variable per timestep (481 MB)
- Level 3: $D(x,y,z,t)$ one file per variable (76 GB)
- Level 2 $\rightarrow$ Level 3 with provided SW
- Level 3 transpose ($D(z,t,x,y)$) with provided SW

```
it=385+indgen(157)  
br_make_fits_level3,'en024048_hion',it,'lgtg'  
br_transpose_fits_level3,'BIFROST_en024048_hion_lgtg_im.fits'
```

Variables

- $e, U_x, U_y, U_z, \rho, B_x, B_y, B_z$
- T_g, P_g, N_e

en024048_hion: 83 | GB

FITS

BIFROST_en024048_hion_lgtg_385.fits

```
SIMPLE = T / Written by IDL: Fri Jul 12 22:13:21 2013
BITPIX = -32 / Number of bits per data pixel
NAXIS = 3 / Number of data axes
NAXIS1 = 504 /
NAXIS2 = 504 /
NAXIS3 = 496 /
EXTEND = T / FITS data may contain extensions
INSTRUME= 'Bifrost ' / Data generated by the Bifrost code
OBJECT = 'en024048_hion' / Bifrost run name
BTYPE = 'lg(tg) ' / Data variable
BUNIT = 'K ' / Data unit
CDELT1 = 0.0476190 / [Mm] x-coordinate increment
CDELT2 = 0.0476190 / [Mm] y-coordinate increment
CDELT3 = 0.0971498 / [Mm] (non-uniform) z-coordinate increment
CRPIX1 = 1 / Reference pixel x-coordinate
CRPIX2 = 1 / Reference pixel y-coordinate
CRPIX3 = 1 / Reference pixel z-coordinate
CRVAL1 = 0.00000 / [Mm] Position ref-pixel x-coordinate
CRVAL2 = 0.00000 / [Mm] Position ref-pixel y-coordinate
CRVAL3 = -2.44401 / [Mm] Position ref-pixel z-coordinate
CTYPE1 = 'x ' / [Mm] Label for x-coordinate
CTYPE2 = 'y ' / [Mm] Label for y-coordinate
CTYPE3 = 'z ' / [Mm] Label for z-coordinate
CUNIT1 = 'Mm ' / Unit for x-coordinate
CUNIT2 = 'Mm ' / Unit for y-coordinate
CUNIT3 = 'Mm ' / Unit for z-coordinate
RUNID = 'Bifrost_cb24bih' / Run ID for identification of input files
ELAPSED = 3850.00 / [s] Time of snapshot
DATA_LEV= 2 / Data level
ZTAU51 = 0.0613866 / [Mm] Average height of tau(500nm)=1
ORIGIN = ' ITA/Oslo' / Origin of data
COMMENT Variables from .idl file:
...
```

Documents

- Paper describing simulation characteristics (in prep)
- ITN 33 giving technical details
 - format, keywords, auxiliary software

Enhanced network

en024048_hion (1600s)

- 24x24x17 Mm (2.5 Mm below, 14.5 Mm above $z=0$)
- 504x504x496 grid
- 48 km horizontal, 19-97 km vertical
- polarities separated by 8 Mm
- $\langle |B| \rangle = 30-50$ G

<http:sdsc.uio.no/search/simulations>

Radiative transfer products

- NUV passband
 - Mg II h&k + background lines
 - 252 x 252 grid, vertical rays
 - FITS files
 - intensity as function of wavelength
 - $z(\tau_v=1)$ as function of wavelength
- ITN 35 describes format, approximations etc

New models

- Higher resolution: 48, 31, 16 km
- Coronal hole at 31 km resolution
- Salt-and-pepper field
- flux emergence
- generalized Ohm's law
- larger Box, small active region